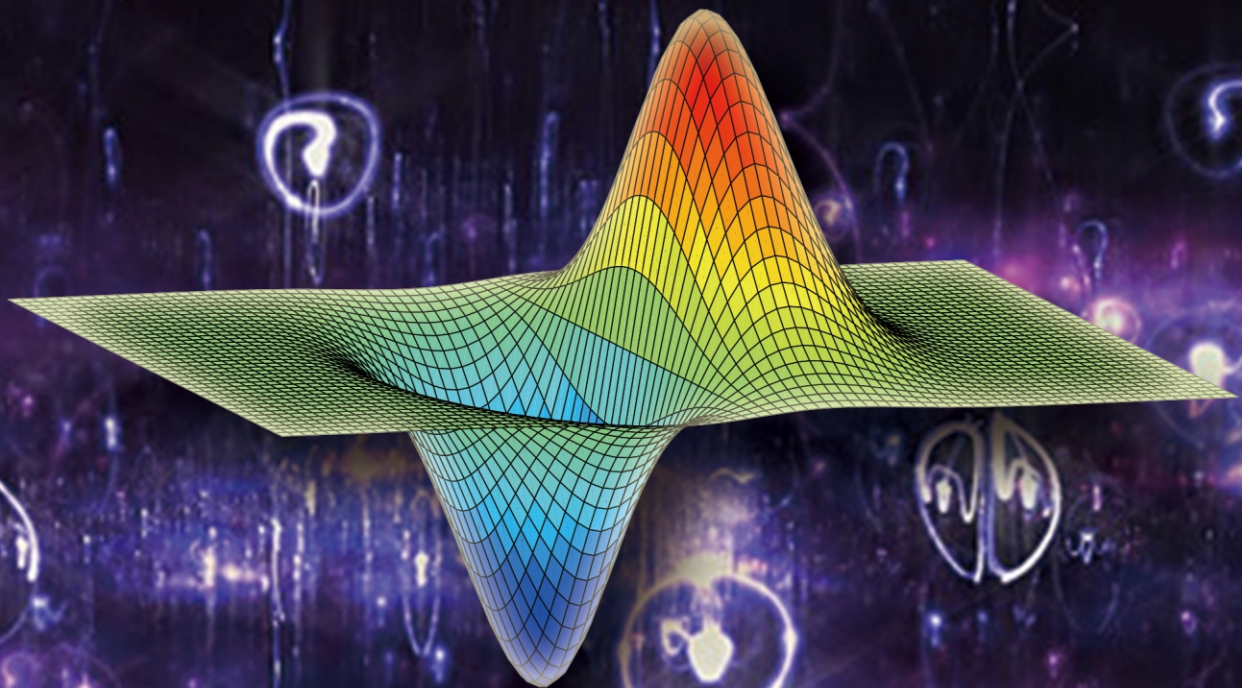


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# Table of Contents

**Volume 9    Number 12**

**December 2019**

**On the Zeros of Euler Product Dirichlet Functions**

D. Ghisa.....959

**Asymptotic Approximation of the Eigenvalues and the Eigenfunctions for the Orr-Sommerfeld Equation on Infinite Intervals**

V. Nijimbere.....967

**Chebyshev Polynomials with Applications to Two-Dimensional Operators**

A. Wünsche.....990

**Gradient Density Estimation in Arbitrary Finite Dimensions Using the Method of Stationary Phase**

K. S. Gurumoorthy, A. Rangarajan, J. Corring.....1034

**Euclid's Fifth Postulate and Convergence of Non-Parallel Straight Lines**

K. Hamiss.....1059

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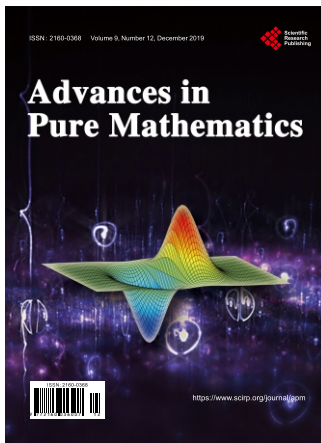
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