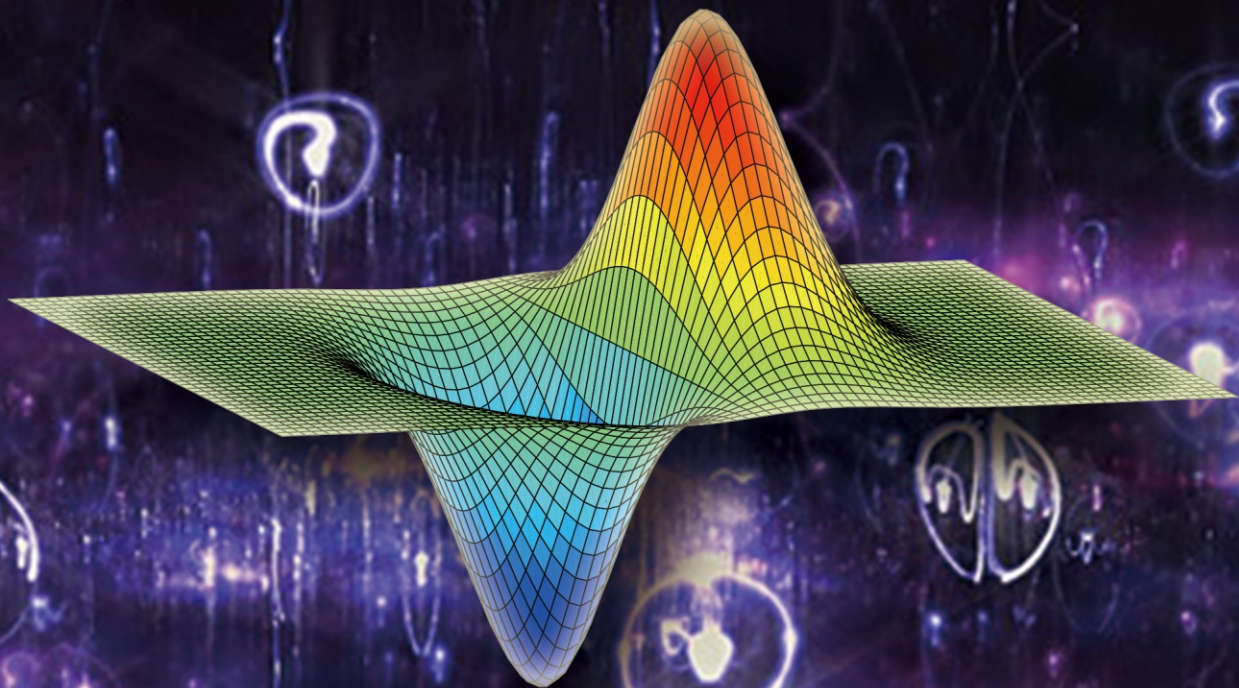


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# Table of Contents

**Volume 13    Number 9**

**September 2023**

## **Generalized Series of Bernoulli Type**

T. Beatty, N. Bianco, N. Legge.....537

## **Polysurfacic Tori or Kideas Inspired by the Möbius Strip Topology**

E. C. Anaxhaoza.....543

## **Lagrangian Formulation of Fractional Nonholonomic Constrained Damping Systems**

O. A. Jarab'ah.....552

## **The Golden Ratio Theorem: A Framework for Interchangeability and Self-Similarity in Complex Systems**

A. Rizzo.....559

## **Some Refinement of Holder's and Its Reverse Inequality**

M. O. Tijani, A. Ojo, O. Akinsola.....597

## **Multiplicity of Solutions for a Class of Noncooperative Elliptic Systems**

X. X. Zhang, G. G. Liu.....610

## **Canonical Treatment of Elliptical Motion**

O. A. Jarab'ah.....620

## **A Key to Solving the Angle Trisection Problem**

L. O. Barton.....625

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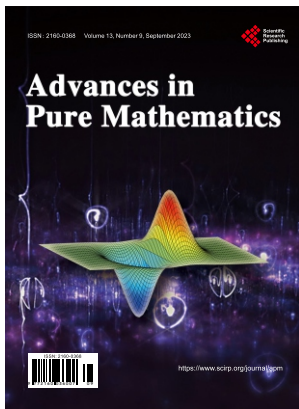
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