

# Advances in Pure Mathematics



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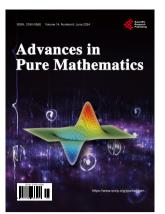
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# **Advances in Pure Mathematics (APM)**

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