

A Method for Rapid Matching Based on Second Order Partial Derivative

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Abstract

Our goal is to enhance matching speed which is important for image engineering. Second Partial Derivative operator in Harris corner detector is directly used to compute the similarity between corners. Then initial matches are obtained. The algorithm is contrasted with normalized cross-correlation and method based on horizontal and vertical gradient. Its computational complexity is reduced and matching speed is improved effectively because this method only adopts the addition and subtraction operations. Experiments on several real images test the matching speed, the matching precision and matching rate of the algorithm. The results demonstrate that the algorithm not only have higher speed but also get higher matching precision and correct matching rate. Even though the stereo image pairs have brightness differences, it still performs rather well.

Keywords: Corner Matching, Gradient Operator, Similarity

1. Introduction

Feature matching is to establish the correspondence between feature points of left and right image in a stereo image pair. It is an important step in computer vision applications, such as stereo vision, motion tracking, and identification. During this process, matching speed is very important for real-time application of image processing.

Corner is a most widely used feature for matching because of its good performance against the change of perspective and easy to detect. The common approach for corner matching is to take a small region of pixels (referred to as a correlation window) from around the detected corner and compare it with a similar region from around each of the candidate corners in the other image [1]. We can find that matching time usually depends on initial matching method. There are several ways based on gray information to complete the initial matching, normalized cross correlation (NCC), sum of squared difference (SSD), and sum of absolute difference (SAD). The most popular measure of similarity is the normalized cross correlation.

Though a lot of algorithms have been presented in the past, establishing good corners correspondences between stereo pairs is still a very challenging task for a number of reasons such as distortion, the difference in lighting condition, and transformations (rotation, translation,

scaling). It is the main object of matching to cost short time and get high matching accuracy at the same time.

In this paper a new corner matching algorithm based on gradient is proposed. Gradient information is widely used in feature matching based on edge, however, corners are also pixels in which gradient change greatly, so that gradient information also can be used in initial matching. In recent years, the horizontal and vertical gradients have been used to measure the similarity between corners [2,3], the horizontal and vertical gradients directly obtained in corner detector need no additional computation, but adopting two gradient operators increases computational complexity. In our algorithm, only one gradient operator, Second Order Partial Derivative, which includes horizontal and vertical gradient information, is found, and it can be directly obtained in corner detector. We replace horizontal and vertical gradient operators with one Second-Order-Derivative operator. It makes our algorithm simple and have high speed. The traditional way to compute the similarity between two corners is normalized intensity cross-correlation. In order to raise computational speed further, we adopt the sum of absolute differences instead of complex normalized cross-correlation. The proposed algorithm not only has high speed but also gets high matching precision and matching rate. Experimental results suggest that it is practicable, effective and robust.

Our proposed method for corner matching is composed of three main steps (1) corner extraction, (2) initial matching based on gradient and (3) matching refinement. In step (2), our algorithm is compared with NICC and GXGY. In the following subsection, each step is described in detail.

2. Corners Extraction

The choice of corner detector has a large impact on the results of a given matching scheme. A number of algorithms for corner extraction have been presented in recent years [4,5]. Because of good performance of the well known Harris corner detector [6], it is chosen to extract interest points in our algorithm. The original Harris corner detector calculates the value of Equation (1):

$$c = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right) \otimes \begin{bmatrix} G_x^2 & G_x G_y \\ G_x G_y & G_y^2 \end{bmatrix} \\ = \begin{bmatrix} G_{xx} & G_{xy} \\ G_{xy} & G_{yy} \end{bmatrix} \quad (1)$$

The operator states a rotational invariance. Here I denotes the gray level, G_x denotes its gradient in x

axis, $G_x = I \otimes \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$; G_y denotes its gradient in

y axis, $G_y = I \otimes \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$. The eigenvalues λ_1

and λ_2 of c are the main curvatures of its auto-correlation.

The corner detector in application is:

$$H = \det(c) - \kappa \times \text{trace}(c) \quad (2)$$

In the above equation, the parameter κ is traditionally set to 0.004, $\det(c) = \lambda_1 \times \lambda_2$, $\text{trace}(c) = \lambda_1 + \lambda_2$.

To avoid large locality excursion of corners detected, we adopt the modified Harris corner detector [7], which is given by

$$M = \frac{\det(c)_{\sigma_{\det}}}{\text{trace}(c)_{\sigma_{\text{trace}}} + \xi} \quad (3)$$

This operator means filtering the numerator with Gaussian function of less σ_{\det} , but filtering the denominator with Gaussian function which has larger σ_{trace} , so we can get accurate localization and much better stability.

3. Initial Matching Based on Second Order Derivative

Initial matching is usually to measure the similarity between two image regions. There are many measures of similarity, of which only a few of most popular are considered here.

1) NICC

The traditional way to compute the similarity between two corners is Normalized Intensity Cross Correlation (NICC) which is computed as follows:

$$\text{NICC}(M, M') = \frac{\sum_{\substack{m \in \text{blockP} \\ m' \in \text{blockQ}}} [i1(m) - \bar{i1}][i2(m') - \bar{i2}]}{\sqrt{\sum_{\substack{m \in \text{blockP} \\ m' \in \text{blockQ}}} [i1(m) - \bar{i1}]^2 \sum_{\substack{m \in \text{blockP} \\ m' \in \text{blockQ}}} [i2(m') - \bar{i2}]^2}} \quad (4)$$

In the above equation, M and M' are two sets of corners to be compared, P and Q blocks (referred to as a correlation window) are two $\omega \times \omega$ windows centered on position of each corner, usually $\omega = 7, 9, 11$ or 13 , m and m' are pixels within P and Q blocks. $i1(m)$ and $i2(m')$ are intensity values, $\bar{i1}$, $\bar{i2}$ are the mean (average intensity values) of the two correlation windows.

Correlation operation includes multiplication and division which cost much time. And Gray correlation has low accuracy which would introduce error matching.

2) GXGY

Two gradient operator G_x and G_y are used to compute the similarity [2,3] which can reduce error matching points between two corners. It is computed as follows:

$$\text{GX}(M, M') = \sum_{\substack{m \in \text{blockP} \\ m' \in \text{blockQ}}} |G_x(m) - G_x(m')| \quad (5)$$

$$\text{GY}(M, M') = \sum_{\substack{m \in \text{blockP} \\ m' \in \text{blockQ}}} |G_y(m) - G_y(m')| \quad (6)$$

$$\text{GXGY} = \text{GX} + \text{GY} \quad (7)$$

G_x and G_y include gray gradient information which can reduce error matching point. And G_x and G_y can be acquired from the procedure of corner extraction, so it will reduce matching time.

3) Algorithm of this paper—GXY

According above analysis, we know that gradient information can get more right matching point. In the Equation (1), Second Order Partial Derivative G_{xy} for each corner has been obtained. And G_{xy} gradient op-

erator contains the horizontal and vertical gradient information, so it is valuable. We describe each corner with G_{xy} .

During the matching process, each corner at (x, y) in the first image is compared with a set of potential corners in the other image, located within a $d_x \times d_y$ rectangular window centered on (x, y) , where d_x and d_y are the maximum expected disparity in horizontal and vertical axes, respectively. Corners are compared using the sum of absolute differences which is computed as follows:

$$GXY(M, M') = \sum_{\substack{m \in \text{blockP} \\ m \in \text{blockQ}}} |G_{xy}(m) - G_{xy}(m')| \quad (8)$$

Only corners that have minimal GXY value with each other are considered as a pair of initial matching corners. Obviously, because of only addition and subtraction operations included the Equation (8) is simpler than that of the Equation (4). So GXY method will cost less time than NICC. And it also has well accuracy than NICC because of using gradient information.

Compared with GXGY, GXGY computes two group of the sum of absolute differences cost two times of time so that computational complexity is increased.

From comparison and analysis in above, we can get conclusion that the method GXY of computing the similarity can reduce computational complexity effectively.

4. Matching Refinement

Based on the result of initial matching, in this section, we use epipolar constraint to remove the outliers.

The epipolar geometry is the intrinsic projective geometry between two views. It is independent of scene structure, and only depends on the internal parameters and relative pose of cameras. This intrinsic geometry is included in the fundamental matrix F . For any pair of corresponding corners x and x' in the two images, this relation should be satisfied:

$$x'^T F x = 0 \quad (9)$$

In this paper, the fundamental matrix is calculated by the eight-point algorithm [8] which needs at least 8 points. We use RANSAC (Random Sample Consensus) algorithm [9] to robustly fit a fundamental matrix to a set of putatively matched corners. Given N matched corner pairs, the RANSAC algorithm involves the random selection p pairs, computation of the fundamental matrix (as described in above section), and determining to what degree all the available matches support the epipolar constraint. After fitting a fundamental matrix, mismatched corners can be rejected effectively so that we

obtain final matching corners from initial matches.

5. Experiments

The proposed algorithm has been extensively evaluated using several groups of image pairs and multi-views. Our experiments are carried out on Pentium 4 with 2.8GHZ processor and 758MB memory, the software used is MATLAB 6.5. The matching results are shown in figures and tables as follows.

GXY denotes the algorithm proposed in this paper; GXGY denotes the algorithm which use the horizontal and vertical gradients to measure the similarity between two corners (Equations (5) (6) (7)), NICC denotes the algorithm which use normalized intensity cross-correlation to measure the similarity between two corners (Equation (4)), other steps and parameters, for example, epipolar constraint and the value of correlation window, in these three algorithms are the same. All views size in this paper is 640×480 .

In order to test the performance of GXY algorithm, we compared GXY with NICC and GXGY. The matching results are showed in following figures. The matching method, the number of corners extracted from the left and right images, the number of initial matches, the number of final matches, the average distance and the matching time are given in the successive columns of the tables. (Figure 1)



(a) GXY



(b) NICC



(c) GXGY

Figure 1. Final matching result and deleted outliers.

Table 1. Experimental result of the first stereo pair.

	GXY	GXGY	NICC
the number of corners extracted	(482,496)	(482,496)	(482,496)
the number of initial matches (initial matching rate)	335(70%)	323(67%)	315(65%)
the number of final matches (final matching rate)	305(91.0%)	289(89.5%)	278(88.3%)
average distance ($\times 10^{-3}$)	2.10	2.30	2.78
matching time (second)	0.20	0.32	0.45



(a)



(b)

(c)



(d)

Figure 2. (a) Shows the second original stereo pair; from (b) to (d): display the left image overlaid with all final matched corners from the right and left images, along with the correspondences (with blue lines). (b), (c) and (d) denote the matching results of GXY, GXGY and NICC method respectively.

The initial matching rate is the percentage of the number of initial matches over the average number of corners extracted from left and right images. The final matching rate is the percentage of the number of final matches over the number of initial matches. The average distance is average distance of all final corner matches to their epipolar lines. In theory, given a corner in the left image, the corresponding corner must lie on the corresponding

epipolar line, in other words, the distance of accurate matches to their corresponding epipolar lines is equal to zero, but in practice because of noise and computational error there is deviations. The smaller average distance indicates the higher matching precision. The matching time of algorithm is the time of initial matching, but corner extraction time and matching refinement time are not included. The shorter matching time indicates the higher matching speed.

The matching results in Table 1 shows that GXY algorithm obtains more final matches, higher final matching rate, smaller average distance and shortest matching time, its matching time is about half of the two other algorithms. If more corners are extracted in our experiment, its good performance at matching speed will be more obvious.

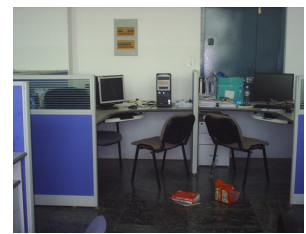
In addition, the second stereo image pair that has brightness differences is given in Figure 2. The matching result is shown in Table 2.

Table 2. Experimental result of the third stereo pair.

	GXY	GXGY	NICC
the number of corners extracted	(527, 606)	(527, 606)	(527, 606)
the number of initial matches (initial matching rate)	407(72%)	402(71%)	385(68%)
the number of final matches (final matching rate)	402(98.8%)	385(96.0%)	364(95.0%)
average distance ($\times 10^{-3}$)	2.30	2.45	2.79
matching time (second)	0.22	0.39	0.53



(1)



(2)



(3)



(4)

Figure 3. Origin views.

Table 3. Test results of four views.

	GXY	GXGY	NICC
the number of corners extracted	299, 284 278, 290	299, 284 278, 290	299, 284 278, 290
the number of initial matches (initial matching rate)	1-2: 243 (83%) 2-3: 210 (87%) 3-4: 193 (93%)	1-2: 237 (81%) 2-3: 204 (88%) 3-4: 184 (94%)	1-2: 223 (77%) 2-3: 188 (86%) 3-4: 166 (92%)
the number of final matches (final matching rate)	1-2: 241 (99%) 2-3: 207 (99%) 3-4: 190 (99%)	1-2: 233 (98%) 2-3: 195 (96%) 3-4: 180 (98%)	1-2: 219 (98%) 2-3: 179 (95%) 3-4: 163 (98%)
average distance ($\times 10^{-3}$)	2.46	2.48	2.54
matching time (second)	0.42	0.79	1.28

The matching result of the second stereo pair illustrates that GXY algorithm still has better performance in the presence of brightness differences.

Multiple views are also used to test algorithm performance in order to show its good matching ability, especially its matching speed. Figure 3 shows image sequence by camera rotation. The matching process is first to find correspondences of (1) and (2), then using this matching result to find the correspondences of (2) and (3), finally to find the correspondences of (3) and (4).

The matching result shows that GXY operator only cost less time which is about half of GXGY costing time and one-third of NICC costing time. At the same time, GXY can get more matching points and more accurate. Obviously, matching speed of GXY operator shows more superiority.

6. Conclusions

A simple and fast corner matching algorithm based on gradient operator is proposed in this paper. The gradient operator is found in Harris corner detector, it is directly used for initial matching. Because of particularity of gradient information, while computing the similarity between two corners, the sum of absolute differences replaces traditional normalized cross-correlation, the sum of absolute differences only includes addition and sub-

traction operations, it can reduce computational complexity effectively and make the algorithm fast. In the same experimental condition the algorithm proposed in this paper has highest matching rate and matching speed compared with the other two algorithms, even though in the presence of brightness differences it still can show its superiority.

7. References

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