

The M2 Money Supply, the Economy, and the National Debt: A Mathematical Approach

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Abstract

The United States dollar was tied to a finite standard dating back to 1792. The dollar has survived multiple wars, armed conflicts short of war, economic recessions, and the Great Depression. At the end of World War II, the dollar, by international agreement, effectively became the world’s reserve currency. Other currencies were fixed to the dollar and the dollar was in turn fixed to the gold standard, that is, the value of a dollar was fixed at thirty-five dollars per ounce of gold. In 1971, the United States government severed the dollar from the gold standard leaving the size of the money supply free of any finite limit. Since that time, the United States money supply, national debt, and stock market indices have experienced exponential growth. The purpose of this paper is to investigate mathematically and model the relationship among these key economic indicators. Our work in this paper allows us to gain some insight into how each of these economic indicators can influence one another while giving us a better idea of how the economy functions. We were allowed to collect data for each of the indicators over a certain period which allowed us to demonstrate that a strong correlation exists among these three indicators. After collecting our data and making some logical assumptions, we modeled the money supply as a function of time. In turn, we modeled the Dow Jones stock market index as a function of the money supply. Finally, we produced a model of the National Debt as a function of the Dow Jones stock market index. From the data, we collected and our economic indicator models, we derived a series of differential equations that would help us observe the exponential growth trend of each graphically. By showing a comparison from our collection of raw data versus our results from our model, we conclude that, under prevailing circumstances, it is reasonable to expect growth in all three indicators and increasing market volatility for some time to come. We have answered the question of whether the monetary and fiscal policies of the past half-century have been of some benefit. However, we question whether this

trend is good for all Americans and whether it is sustainable in perpetuity. This paper concludes with possible areas of interest warranting additional investigation to enable us to better understand the economy and develop effective financial strategies.

Keywords

Mathematical Modeling, Money Supply, Stock Market, National Debt, Exponential Model, Gold Standard, Reserve Currency

1. Introduction

Between the end of World War II and 1971, the value of the dollar was tied to the price of gold. However, the United States took the dollar completely off the gold standard in 1971. Since then, the dollar has operated as a purely fiat currency as its supply is no longer tied to any standard of measure. In the aftermath of this move, the United States' money supply, national debt, and stock market indices have experienced exponential growth. We know from the work of other researchers that the Federal Reserve Bank works to manage the economy and control price inflation by adjusting interest rates and regulating the money supply. Several researchers have studied the effect of the money supply on various aspects of the economy. It is generally agreed that increasing the money supply in a fiat currency system weakens the purchasing power of a unit of currency. One standard used to measure price inflation, *i.e.*, the decline in the purchasing power of the US Dollar relative to goods and services, is the Consumer Price Index (CPI). This measure has some critics. Other authors have instead measured the effect of the changing money supply on the value of the US Dollar relative to a single commodity such as gold or oil. Each of these approaches has merit but is limited in scope to the specific goods or services being considered. In either case, the authors question the wisdom of continually expanding the money supply for years on end. This caused us to opt for a broader approach by testing the mathematical relationship between the M2 Money Supply, the National Debt, and major Market Indices.

Although opinions and methods of analysis vary, it cannot be disputed that the Money Supply, National Debt, and Market Indices are strongly correlated, mathematically speaking. In this paper, we investigate the history and nature of this enduring correlation. In doing so, we will focus on each of our three economic indicators and their relationship with each other. Taking our data and applying it graphically gives us a visual to see the trend of our three economic indicators. Using a series of mathematical modeling techniques, we are able to produce multiple equations that represent our work and data collection and compare our model to the raw data we have collected. Finally, we are able to show how the relationship among the three economic indicators that have some kind of connection or may have some influence in the real world scenarios.

1.1. Problem Statement

The purpose of this paper is to model the mathematical relationship between the money supply, market indices, and the national debt in the United States economy in the era of the fiat US dollar. We will study and investigate a manageable data set that measures M2 Money Stock levels, the Dow Jones Index, and the National Debt as reported at the end of each federal fiscal year from 1969 to 2020 (see **Table 1**). Our data set begins two years before the United States dollar was completely removed from the gold standard. This allows us to establish a baseline prior to the event presently under investigation.

1.2. Literature Review

Adam Smith’s 1776 book, *An Inquiry into the Nature and Causes of the Wealth of Nations*, is lauded as “a seminal book that represents the birth of free-market economics” [1]. According to critics, Adam Smith believed “a nation needed... three elements to bring about universal prosperity” [1]. One of these elements was solid currency [1]. According to one source, “[b]y backing currency with hard metals, Smith hoped to curtail the government’s ability to depreciate money by circulating more of it to pay for wars or other wasteful expenditures” [1]. English-American author Thomas Paine shared this view. In 1786, he opined that while paper could properly be used for writing promissory notes, it would be unwise for one to put any faith in a paper currency that is not backed by specie, *i.e.*, gold or silver coin [2]. Consistent with this view of money, the American currency system was tied to precious metals, namely gold and silver, dating back to 1792 [3]. On July 22, 1946, the United States and 44 other nations entered into an international agreement known as Bretton Woods [3]. According to this agreement, “most currencies of the world were pegged to specific values relative to the US Dollar, and in turn, the United States set the value of the dollar at thirty-five dollars to an ounce of gold. ...Until the 1960s, the governments of the United States and other nations worked together to keep the value of the dollar fixed at thirty-five dollars per ounce...” [3]. In 1971, the United States shifted economic policy to the Nixon-Connally plan, which took the dollar completely off the gold standard [3]. “This move... ended the... period of greatest economic prosperity and productivity in the history of the American dollar. The dollar never regained its historical strength, nor has it since enjoyed the confidence that the world had in it prior to Nixon’s move” [3]. According to author Jack Weatherford, “The United States had moved away from money based on and redeemable in gold to a system of money based solely on the policies of politicians, bureaucrats, and government regulatory agencies.” [3].

In his book, *The History of Money*, written in 1997, Weatherford measured the dollar against the price of gold to illustrate the declining value of the dollar, pointing out that “the dollar has undergone a nearly constant decline in value when measured against gold, ...a home, a car, or any basket of goods.” [3]. By the end of the year 2020, the dollar had become nearly worthless when measured

Table 1. National debt and M2 money supply in \$ billions and S & P 500, Wilshire 5000, and Dow Jones industrial average measured in points 1969-2020.

t	Year	Debt in \$ billions	S & P 500	Willshire 5000	Dow Jones	M2 in \$ billions
0	1969	354	95.52		813.1	582
1	1970	371	84.37	830.3	760.7	611
2	1971	398	97.29	914.2	887.2	693
3	1972	427	109.6	1028.2	953.3	778
4	1973	458	109.8	979.0	947.1	839
5	1974	475	69.44	550.0	607.9	888
6	1975	533	88.57	734.6	793.9	992
7	1976	620	101.9	920.7	990.2	1111
8	1977	699	93.74	887.5	847.1	1246
9	1978	772	100.6	996.1	865.8	1345
10	1979	827	104.5	1101.8	878.6	1454
11	1980	908	130.2	1300.9	932.4	1574
12	1981	998	119.8	1208.4	850	1706
13	1982	1142	132.7	1235.8	896.3	1858
14	1983	1377	167.7	1757.9	1233.1	2083
15	1984	1572	164.8	1698.1	1206.7	2244
16	1985	1823	186.2	1871.2	1328.6	2456
17	1986	2125	237.4	2360.5	1767.6	2668
18	1987	2350	280.2	3171.0	2596.3	2800
19	1988	2602	277.4	2706.7	2112.9	2957
20	1989	2857	347.4	3426.7	2692.8	3093
21	1990	3233	307.12	2946.5	2452.5	3255
22	1991	3665	386.88	3744.0	3016.8	3355
23	1992	4065	412.5	4024.4	3271.7	3410
24	1993	4410	463.9	4601.8	3555.1	3452
25	1994	4693	463.81	4605.8	3843.2	3486
26	1995	4974	582.92	5806.6	4789.1	3602
27	1996	5225	701.46	6765.7	5882.2	3754
28	1997	5413	951.16	9180.2	7945.3	3963
29	1998	5526	1032.47	9346.8	7842.6	4257
30	1999	5656	1300.01	11,713.8	10,337	4557
31	2000	5674	1390.14	13,613.3	10,650.9	4842

Continued

32	2001	5807	1076.59	9563.0	8847.56	5336
33	2002	6228	854.63	7773.6	7591.93	5644
34	2003	6783	1038.73	9649.7	9275.06	6060
35	2004	7379	1117.21	10,895.5	10,080.3	6332
36	2005	7932	1191.96	12,289.3	10,568.7	6591
37	2006	8507	1363.38	13,346.0	11,679.1	6931
38	2007	9008	1539.66	15,362.0	13,895.6	7389
39	2008	10,025	968.8	11,875.4	10,850.7	7846
40	2009	11,910	1067.66	10,945.2	9712.28	8432
41	2010	13,562	1171.58	12,020.9	10,788.05	8688
42	2011	14,790	1207.22	11,842.1	10,913.38	9540
43	2012	16,066	1437.82	15,044.2	13,437.13	10,200
44	2013	16,738	1720.03	17,982.4	15,129.67	10,833
45	2014	17,824	1937.27	20,760.5	17,042.9	11,492
46	2015	18,151	2024.81	20,119.3	16,284.7	12,153
47	2016	19,573	2143.02	22,578.7	18,308.15	13,031
48	2017	20,245	2557	26,238.5	22,405.09	13,716
49	2018	21,516	2785.46	30,258.6	26,458.31	14,229
50	2019	22,719	2977.68	30,351.9	26,916.83	15,023
51	2020	26,945	3418.7	34,480.2	27,781.7	18,648

against gold [1]. See the **Figure 1**. "The ounce of gold that had cost \$35.00 in 1971 had increased to approximately \$400.00 by 1995" [3].

The value of the dollar continued to decline relative to gold through the year 2020 when gold was trading at approximately \$1800.00 per ounce [4]. This is illustrated in **Figure 2**.

The Nixon Administration's decision to sever the value of the dollar from the price of gold is not without controversy. In his 2017 thesis, "Quantitative Easing: Money Supply and the Commodity Prices of Oil, Gold, and Wheat," Aaron Kasteler criticized the Federal Reserve Bank's management of the money supply [5]. He pointed out that since abandoning the gold standard in 1971, the government has consistently failed to balance its spending with its tax revenues [5]. Consistent with Weatherford's assessment of the declining value of the dollar, Kasteler posed the important question of whether continually increasing the money supply could be good for the American people [5]. He questioned how average working citizens benefit from having their savings constantly and consistently devalued by the Federal Reserve Bank's expansive monetary policies [5]. These are a few of the many unanswered questions about the eventual fate of the dollar and the economy of the United States. However, the 1971 move away

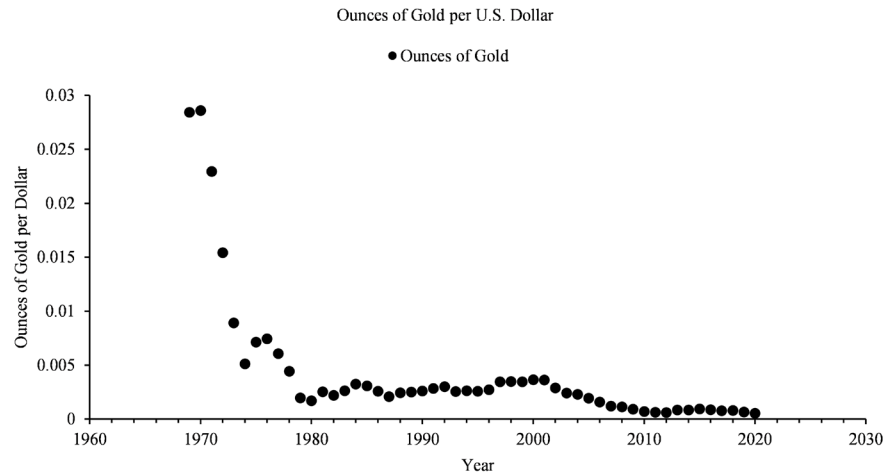


Figure 1. Change in the number of ounces of gold that can be purchased for one US Dollar from 1969-2020.

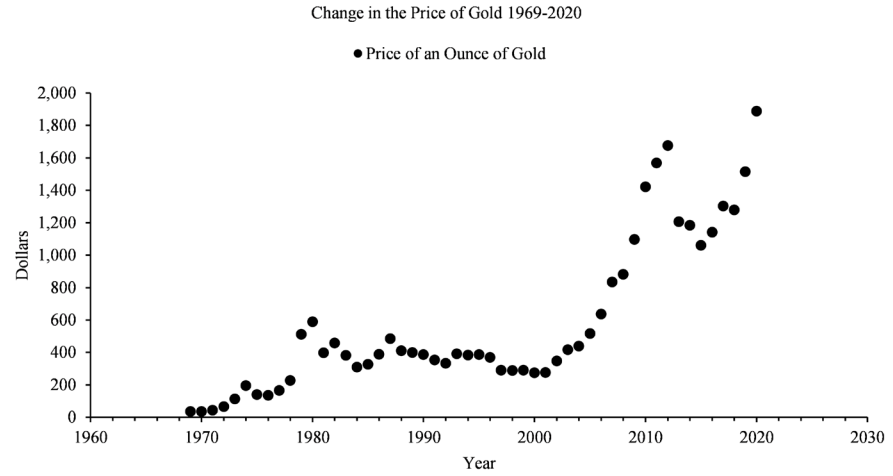


Figure 2. The price of an ounce of gold 1969-2020.

from the gold standard unquestionably constituted a fundamental change to the United States’ monetary system. This change set the monetary system afloat in uncharted waters, the navigation of which is of worldwide importance because “[t]he [world] market has enthroned the US dollar as the international reserve currency” effectively making the US Federal Reserve Bank and the US Treasury the international lender of last resort [6].

1.3. Data Collection and Investigation

Our data collection efforts revealed that following the change in economic policy in 1971, the total national debt soared from approximately \$398 billion in 1971 to roughly \$26.945 trillion at the end of the fiscal year 2020 [7]. During this period, the Dow Jones Industrial Average (DJIA)¹ increased from 887.2 points to

¹“The DJIA is calculated by adding up all the stock prices of its 30 components and dividing the sum by the divisor... The Dow Divisor maintains continuity by factoring in the many changes that take place within the market... [and] was 0.147 as of Sept. 2019.” [12]

27,781.7 points [8]. The M2 Money Stock also expanded from \$692.5 Billion to \$18.6483 Trillion [9] [10] [11]². During this era, at no time did the National Debt or the M2 Money Supply decrease from the end of one fiscal year to the end of the next. However, the Dow Index has fluctuated wildly at times. The largest relative annual increase in the Dow was between the end of the fiscal year 1986 and the end of the fiscal year 1987 when the Dow gained 46.9%; the largest relative annual decrease came between the end of the fiscal year 1972 and the end of the fiscal year 1973 when the Dow decreased by 35.8% [8] (see **Table 2**).

Graphs of these three data sets measured from 1969-2020 as reported as near as possible to the last day of each fiscal year exhibit exponential growth curves which are displayed in **Figures 3-5**.

All three data sets could be modeled individually with differential equations of the form $dy/dt = r(t)$, which can be solved analytically resulting in a solution of the form $y = Ce^{rt}$ [13]. A graph comparing the raw data for the M2 Money Supply, Dow Jones Index, and National Debt, measured at the end of each fiscal year suggests that the data grow proportionally to each other (see **Figure 6**).

After assembling the raw data (see **Table 1**), we investigated the correlation

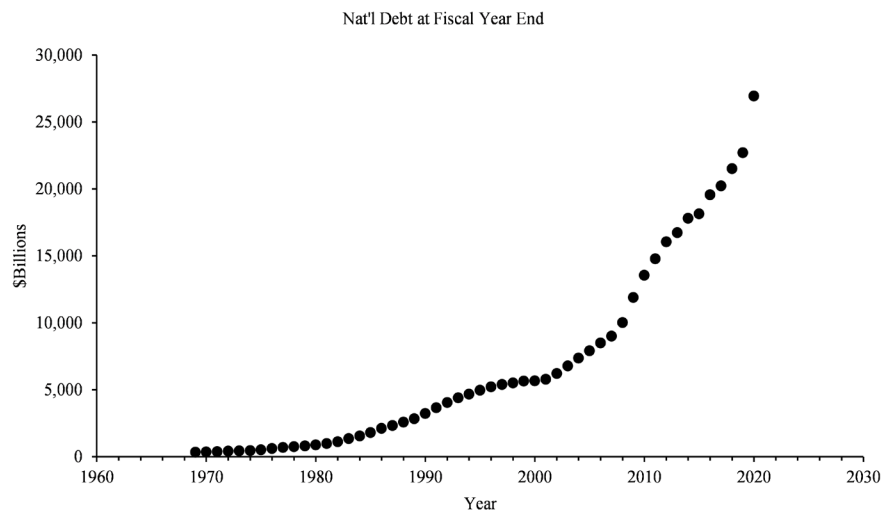


Figure 3. National debt measured in \$ billions as reported on the last day of each respective fiscal year from 1969 through 2020.

²“M2 consists of M1 plus 1) savings deposits (including money market deposit accounts); 2) small-denomination time deposits (time deposits in amounts of less than \$100,000) less individual retirement account (IRA) and Keogh balances at depository institutions; and 3) balances in retail money market mutual funds less IRA and Keogh balances at money market mutual funds. Seasonally adjusted M2 is constructed by summing savings deposits, small-denomination time deposits, and retail money funds, each seasonally adjusted separately, and adding this result to seasonally adjusted M1. M1 consists of 1) currency outside the U.S. Treasury, Federal Reserve Banks, and the vaults of depository institutions; 2) demand deposits at commercial banks (excluding those amounts held by depository institutions, the U.S. government, and foreign banks and official institutions) less cash items in the process of collection and Federal Reserve float; and 3) other checkable deposits (OCDs), consisting of negotiable order of withdrawal, or now, and automatic transfer service, or ATS, accounts at depository institutions, credit union share draft accounts, and demand deposits at thrift institutions. Seasonally adjusted M1 is constructed by summing currency, demand deposits, and OCDs, each seasonally adjusted separately.” [11].

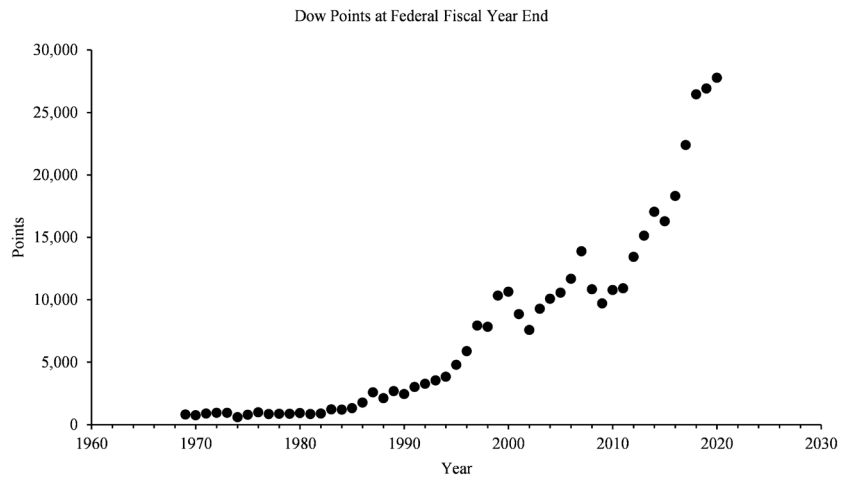


Figure 4. Dow Jones industrial index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020.

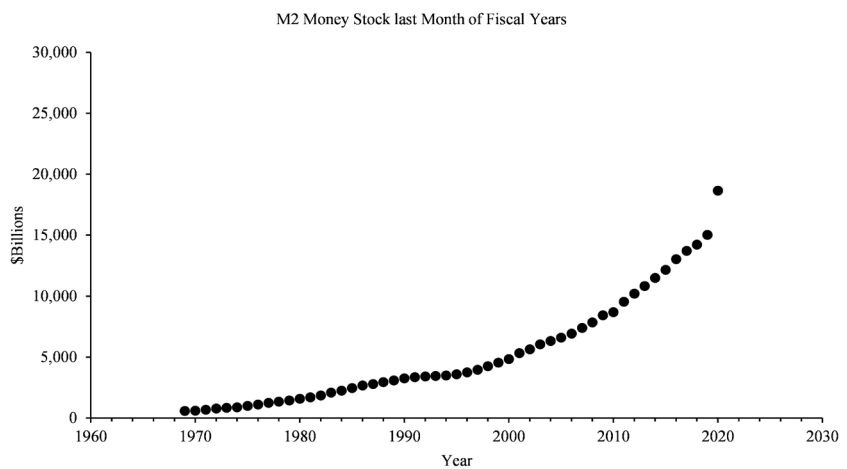


Figure 5. M2 money stock levels measured in \$ billions as reported on the last day of each respective fiscal year from 1969 through 2020.

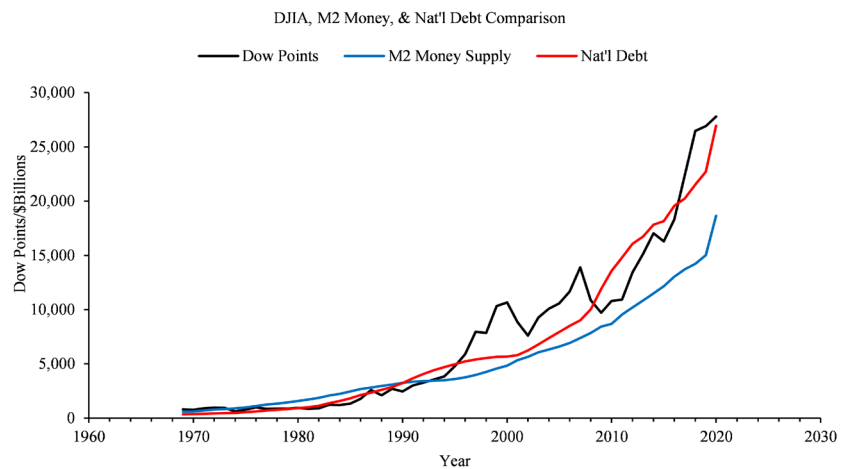


Figure 6. Comparison of Dow Jones index measured in Points, M2 Money Supply measured in \$ billions, and National Debt measured in \$ billions as reported on the last day of each respective fiscal year from 1969 through 2020.

Table 2. Dow Jones Industrial Average with computed change in value and percent change in value from 1969 through 2020 with modeled Dow Midline, and modeled Upper and Lower Bounds from 1969 through 2030.

t	Year	Dow Jones (FY end)	Δ Dow Jones	% Δ Dow Jones	Dow Model Midline	Dow Upper Bound	Dow Lower Bound
0	1969	813.1	-52.4	-6.4	1126.6	1655.0	723.3
1	1970	760.7	126.5	16.6	1198.0	1759.9	769.1
2	1971	887.2	66.1	7.5	1273.9	1871.4	817.9
3	1972	953.3	-6.2	-0.7	1354.6	1989.9	869.7
4	1973	947.1	-339.2	-35.8	1440.4	2116.0	924.8
5	1974	607.9	186	30.6	1531.7	2250.1	983.3
6	1975	793.9	196.3	24.7	1628.7	2392.6	1045.6
7	1976	990.2	-143.1	-14.5	1731.9	2544.2	1111.9
8	1977	847.1	18.7	2.2	1841.6	2705.4	1182.3
9	1978	865.8	12.8	1.5	1958.3	2876.8	1257.2
10	1979	878.6	53.8	6.1	2082.4	3059.0	1336.9
11	1980	932.4	-82.4	-8.8	2214.3	3252.8	1421.6
12	1981	850	46.3	5.4	2354.6	3458.9	1511.6
13	1982	896.3	336.8	37.6	2503.7	3678.0	1607.4
14	1983	1233.1	-26.4	-2.1	2662.4	3911.0	1709.2
15	1984	1206.7	121.9	10.1	2831.0	4158.8	1817.5
16	1985	1328.6	439	33.0	3010.4	4422.3	1932.7
17	1986	1767.6	828.7	46.9	3201.1	4702.4	2055.1
18	1987	2596.3	-483.4	-18.6	3403.9	5000.3	2185.3
19	1988	2112.9	579.9	27.4	3619.6	5317.1	2323.8
20	1989	2692.8	-240.3	-8.9	3848.9	5654.0	2471.0
21	1990	2452.5	564.3	23.0	4092.7	6012.2	2627.5
22	1991	3016.8	254.9	8.4	4352.0	6393.1	2794.0
23	1992	3271.7	283.4	8.7	4627.7	6798.1	2971.0
24	1993	3555.1	288.1	8.1	4920.9	7228.8	3159.2
25	1994	3843.2	945.9	24.6	5232.6	7686.7	3359.3
26	1995	4789.1	1093.1	22.8	5564.1	8173.7	3572.2
27	1996	5882.2	2063.1	35.1	5916.6	8691.5	3798.5
28	1997	7945.3	-102.7	-1.3	6291.5	9242.2	4039.1
29	1998	7842.6	2494.4	31.8	6690.0	9827.7	4295.0
30	1999	10,337	313.9	3.0	7113.9	10,450.3	4567.1
31	2000	10,650.9	-1803.34	-16.9	7564.6	11,112.3	4856.4
32	2001	8847.56	-1255.63	-14.2	8043.8	11,816.3	5164.1
33	2002	7591.93	1683.13	22.2	8553.4	12,564.9	5491.3

Continued

34	2003	9275.06	805.24	8.7	9095.3	13,361.0	5839.2
35	2004	10,080.3	488.4	4.8	9671.5	14,207.4	6209.1
36	2005	10,568.7	1110.4	10.5	10,284.2	15,107.5	6602.5
37	2006	11,679.1	2216.5	19.0	10,935.7	16,064.6	7020.7
38	2007	13,895.6	-3044.9	-21.9	11,628.5	17,082.3	7465.5
39	2008	10,850.7	-1138.42	-10.5	12,365.2	18,164.6	7938.5
40	2009	9712.28	1075.77	11.1	13,148.6	19,315.3	8441.4
41	2010	10,788.05	125.33	1.2	13,981.6	20,539.0	8976.2
42	2011	10,913.38	2523.75	23.1	14,867.4	21,840.2	9544.9
43	2012	13,437.13	1692.54	12.6	15,809.3	23,223.9	10,149.6
44	2013	15,129.67	1913.23	12.6	16,810.9	24,695.2	10,792.6
45	2014	17,042.9	-758.2	-4.4	17,875.9	26,259.7	11,476.3
46	2015	16,284.7	2023.45	12.4	19,008.4	27,923.3	12,203.4
47	2016	18,308.15	4096.94	22.4	20,212.6	29,692.3	12,976.5
48	2017	22,405.09	4053.22	18.1	21,493.1	31,573.4	13,798.6
49	2018	26,458.31	458.52	1.7	22,854.8	33,573.7	14,672.8
50	2019	26,916.83	864.87	3.2	24,302.7	35,700.7	15,602.3
51	2020	27,781.7			25,842.3	37,962.4	16,590.8
52	2021				27,479.5	40,367.4	17,641.9
53	2022				29,220.4	42,924.8	18,759.5
54	2023				31,071.6	45,644.2	19,948.0
55	2024				33,040.1	48,535.9	21,211.7
56	2025				35,133.3	51,610.8	22,555.6
57	2026				37,359.1	54,880.5	23,984.5
58	2027				39,725.9	58,357.3	25,504.0
59	2028				42,242.6	62,054.4	27,119.8
60	2029				44,918.8	65,985.8	28,837.9
61	2030				47,764.6	70,166.1	30,664.9

between the various data sets. In pertinent part, we found the following correlation coefficients (r)³ for the data:

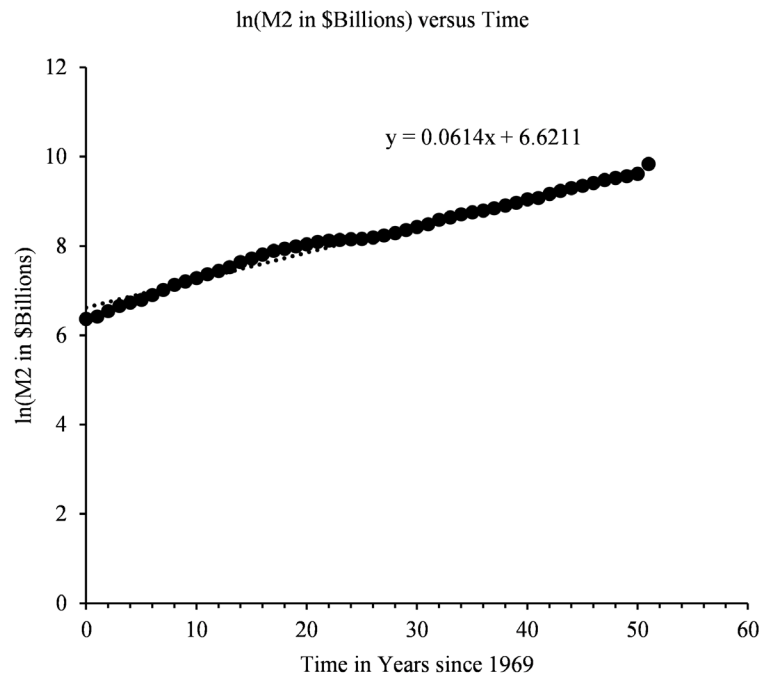
ln(M2) versus Time(t): $r \approx 0.9926$;

Dow versus M2: $r \approx 0.9832$; and

National Debt versus Dow: $r \approx 0.9814$,

(see **Figures 7-9**).

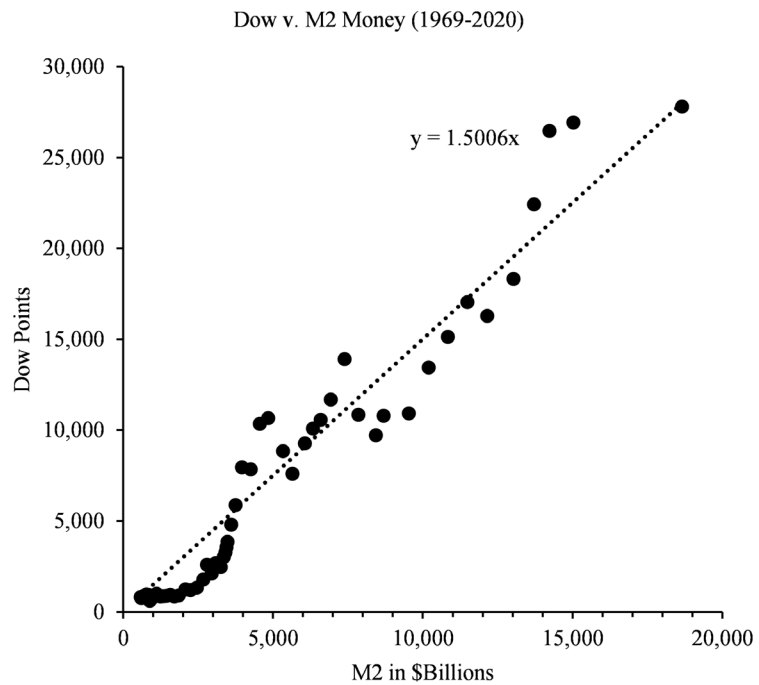
³“The linear correlation coefficient... measures the strength of a linear relationship between two quantitative variables. The symbol for the... coefficient is r ... The *range of the linear correlation coefficient* is from -1 to $+1$. If there is a *strong positive linear relationship* between the variables, the value of r will be close to $+1$. If there is a *strong negative linear relationship* between the variables, the value of r will be close to -1 ” [14].



<i>Regression Statistics</i>	
Multiple R	0.99262513
R Square	0.985304648
Adjusted R Square	0.985010741
Standard Error	0.114819467
Observations	52
ANOVA	
<i>df</i>	
Regression	1
Residual	50
Total	51
<i>Coefficients</i>	
Intercept	6.621111597
X Variable 1	0.061427342

Figure 7. Linear regression analysis of the transformed M2 Money Supply measured in \$ billions (1969-2020). The natural logarithm of M2 is plotted on the (y) axis; time measured in years since 1969 is plotted on the (x) axis.

We further explored the relationships between these data via linear regression models using the sum of least squares method [13]. We found the coefficients of determination⁴, denoted R^2 , to be ≈ 0.9853 , 0.9667 , and 0.96321 , respectively (see ⁴“[T]he coefficient of determination R^2 , ... is a measure of fit for the regression line... the closer the value of R^2 is to 1, the better the fit of the regression line. (Note that $R^2 \leq 1$ always holds).” [13])

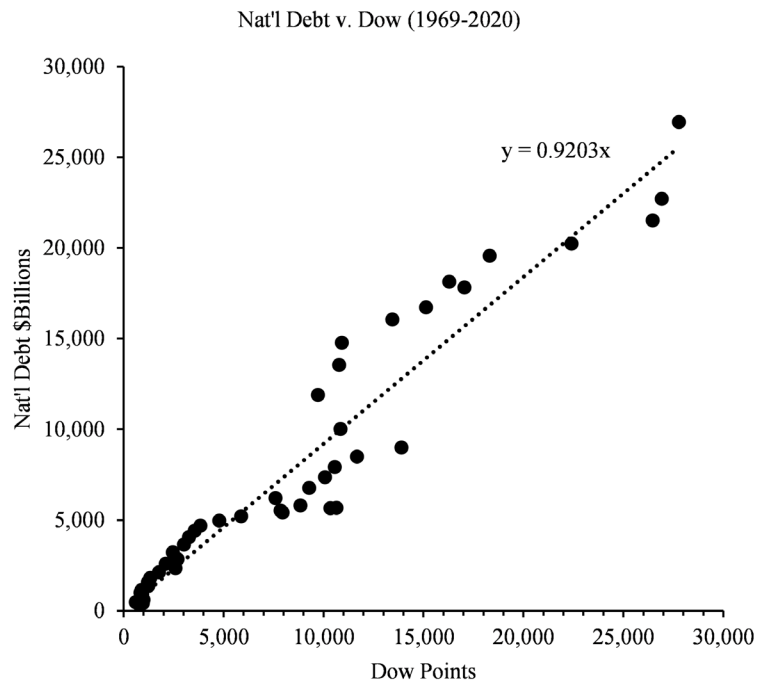


<i>Regression Statistics</i>	
Multiple R	0.983224817
R Square	0.96673104
Adjusted R Square	0.947123197
Standard Error	1928.868101
Observations	52
<i>ANOVA</i>	
<i>df</i>	
Regression	1
Residual	51
Total	52
<i>Coefficients</i>	
Intercept	0
X Variable 1	1.500623358

Figure 8. Linear regression analysis of Dow Jones Index measured in points versus the M2 Money Supply measured in \$ billions (1969-2020). The Dow Jones Index is plotted on the (*y*) axis; the M2 Money Supply is plotted on the (*x*) axis.

Figures 7-9). These observations indicate that these data sets bear a strong positive correlation to each other and provide some insight to help us model the relationship between these variables (see **Figures 7-9**).

Given these correlations and the knowledge that “monetary policy... has emerged as one of the strongest levers that the Federal Reserve pulls in its



<i>Regression Statistics</i>	
Multiple R	0.981434745
R Square	0.963214158
Adjusted R Square	0.943606315
Standard Error	1901.940348
Observations	52
<i>ANOVA</i>	
<i>df</i>	
Regression	1
Residual	51
Total	52
<i>Coefficients</i>	
Intercept	0
X Variable 1	0.920311933

Figure 9. Linear regression analysis of the National Debt measured in \$ Billions versus the Dow Jones Index measured in Points (1969-2020). The National Debt is plotted on the y -axis; the Dow Jones Index is plotted on the x -axis.

management of the economy,” [5] it is reasonable to model M2 Money stock levels as a function of time. The Dow Jones Index can be modeled as a function of the M2 Money Supply given the strong positive correlation between the variables. This is a logical thing to do because other researchers have noted that increases in the money supply explain “the substantial increase in some share prices and the drastic price increase in several commodities” [5]. “The White

House and Congress use gross domestic product (GDP)⁵ numbers to plan spending and tax policy," [15] and the Dow Jones Index curve are like those of other major stock market indices [8] [16] [17], (see **Figures 10-12**).

Considering these facts and the strong positive correlation between the National Debt and the Dow Jones Index, it makes sense to model the National Debt as a function of the Dow Jones Index.

2. Mathematical Model

When we mention the process of mathematical modeling, there are a series of steps that we must follow for our model to be successful. First, we have established an objective or goal that we want to work towards, and then research our

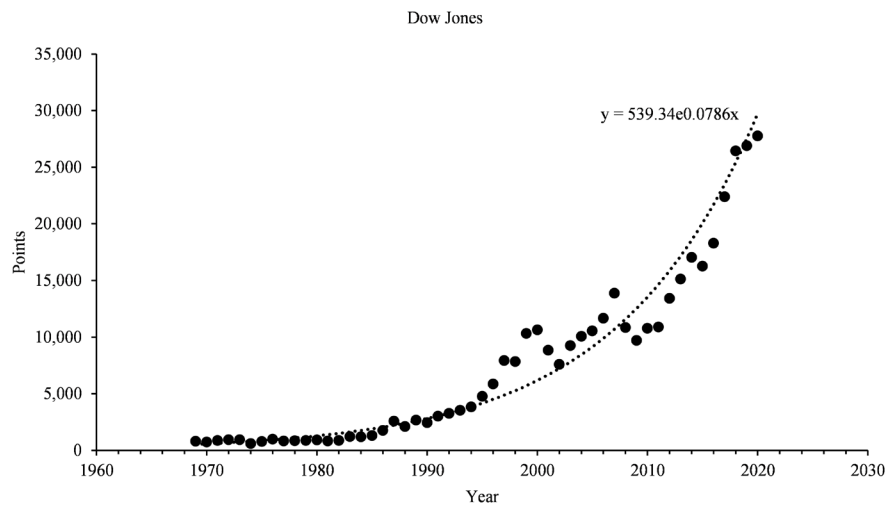


Figure 10. Dow Jones index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020.

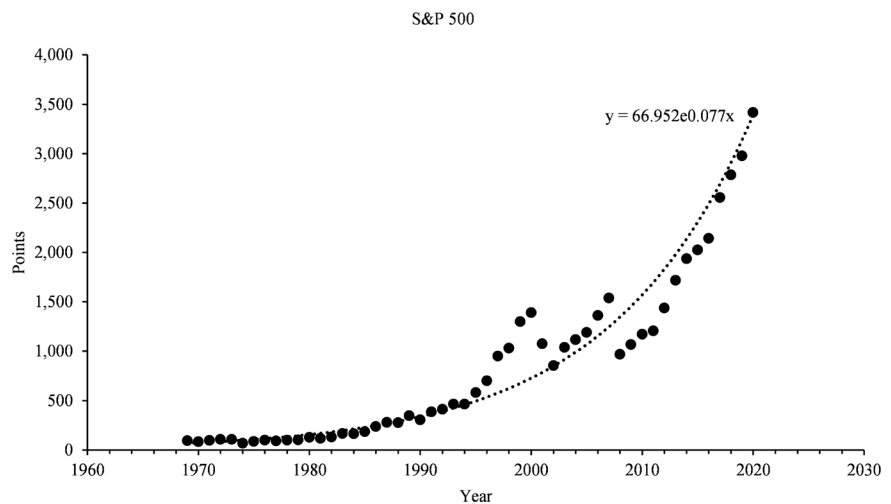


Figure 11. S & P 500 stock market index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020.

⁵“‘Current-dollar’ or ‘nominal’ GDP estimates are based on market prices during the period being measured.” [15].

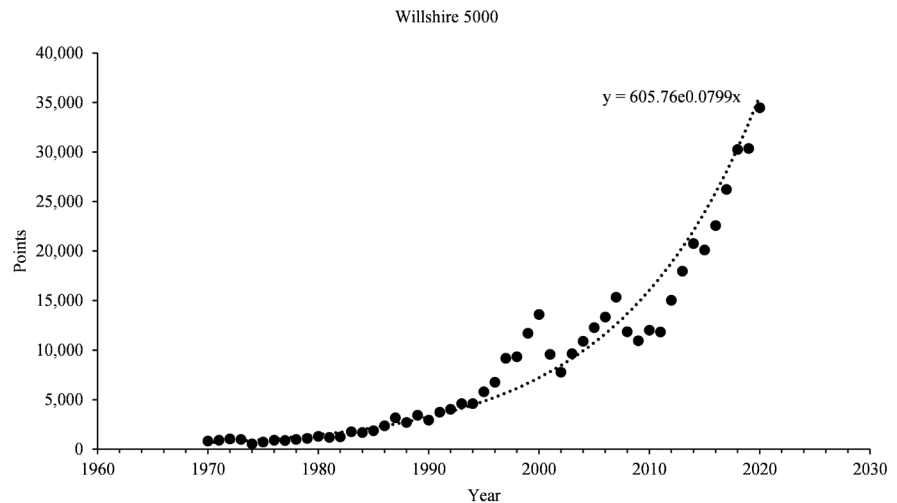


Figure 12. Wilshire 5000 stock market index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020.

topic of choice to gather data to aid us going forward. Once we have stated a clear objective and gathered data, we want to make some reasonable assumptions. This step in the modeling process is the foundation that will determine the conditions under which our model will be valid. This makes the process more manageable and aids us in analyzing our data for better understanding. From here we want to provide a list of variables that will aid us throughout our modeling analysis. Next, we want to select a model equation that is derived from our initial data collection and assumptions we have established. Then once we have our base equation, we use our knowledge of modeling techniques to transform and solve the equation to best satisfy our data collection. Finally, once we have solved our model we can compare and analyze with the actual data to see if it is valid and reasonable. When getting started, an important step in the modeling process is to simplify the problem by making reasonable assumptions [13]. After reviewing the literature, we became aware that an enormous number of variables can influence the data presently under study. Therefore, several assumptions had to be made to construct a manageable model. After observing graphs of the actual data and assessing what we learned from the literature, we decided upon the following assumptions:

1) The M2 Money Supply is controlled by the Federal Reserve Bank. This is assumed because it is known that “[t]he Federal Reserve attempts to influence the economy through interest rates and the supply or availability of money...” [5].

2) Present trends in monetary and fiscal policy will continue for the foreseeable future. We assume this based on the way the stock market indices, national debt, and money supply have behaved over the 50-plus years since President Nixon freed the dollar from the “gold standard.”

3) The Dow Jones Index accurately represents the pattern of growth and decline of the other major US stock indices. This assumption is based on our ob-

servation that the growth curves of other stock market indices, namely the S & P 500 and the Wilshire 5000, are practically identical to those of the Dow Jones Index.

4) The Dow Jones Index is proportional to the M2 Money Supply. This assumption is based on our observation that the average value of the Dow Jones Index bears a strong positive correlation to the M2 Money Supply.

5) The Dow Jones Index tends to cycle roughly every eight years, beginning at a low point in 1970. We make this assumption based on our observation of the plot of the actual data which shows there have been eight big cycles (from minimum to maximum back to a minimum) spread over 52 data points.

6) Fluctuations in the Dow Jones Index are proportional to its volume, *i.e.*, when the index becomes larger, its fluctuations become larger. We make this assumption based on our observation that the fluctuations of the Dow Jones index have grown larger over time as has the size of the index.

7) National Debt is determined by Congress. This assumption is based on Congress's "Power of the Purse."⁶

8) Congress considers GDP as a major factor in the dollar amount of debt instruments the Government can afford to issue in making appropriations; therefore, National Debt is proportional to the Dow Jones Index. This assumption is based on the known fact that "[t]he White House and Congress use Gross Domestic Product (GDP) numbers to plan spending and tax policy." [15].

Throughout this paper we have used the following variables:

N = National Debt in Billions of Dollars,

M = M2 Money Supply in Billions of Dollars,

D = Dow Jones Index measured in points,

t = Time measured in years since 1969.

Fitting the Data to a Mathematical Model

The chosen form of our model equations based on our initial data analysis and assumptions is as follows:

$$M = f(t) = Ce^{rt} \quad (1)$$

$$D = g(f(t)) \quad (2)$$

$$N = h(g(f(t))) \quad (3)$$

The thought process is to model the M2 Money Supply (M) as a function of time-based on historical data. The Dow Jones Index (D) is modeled as a function

⁶"The debt limit is currently suspended, and scheduled for reinstatement on August 1, 2021, at a level precisely accommodating federal borrowing at that point. ...The Constitution grants Congress the 'power of the purse,' which allows Congress to restrict the amount of federal debt. Under current law Congress exercises this power through the federal debt limit, which is codified at 31 U.S.C. §3101. ... When debt levels approach the statutory debt limit, Congress can choose to: 1) leave the debt limit in place; 2) increase the debt limit to allow for further federal borrowing; 3) maintain the current debt limit and require the implementation of 'extraordinary measures' that will postpone (but not prevent) a binding debt limit; or 4) temporarily suspend or abolish the debt limit." [18]

of the line of best fit relative to the M2 Money Supply at time (t). Finally, the National Debt is modeled as a function of the line of best fit relative to the Dow Jones Index. The only independent variable in this structure is time (t). There is some interdependence among the dependent variables, but, generally, the M2 Money Supply depends on time; the Dow Jones Index depends on the M2 Money Supply at time (t); and the National Debt depends on the Dow Jones Index at time (t).

Having observed that the growth of the M2 Money Supply approximates an exponential curve, we transformed the data to test the fit for a model of the following form

$$y = Ce^{rt}. \quad (4)$$

Transforming the data gives an equation of the following form

$$\ln(y) = \ln(C) + rt. \quad (5)$$

Regression analysis using the sum of least squares method on the transformed data, $\ln(M)$ versus time (t) gives an equation of the form

$$\ln(M) = \ln(C) + rt, \quad (6)$$

where $\ln(C) = 6.621112$ and $r = 0.061427$ (see **Figure 7**).

Taking the exponential on both sides in the Equation (6) and replacing the known numerical values for unknown quantities resulted in the following model equation

$$M = 750.7792e^{0.061427t}. \quad (7)$$

We have verified the model by comparing the model with the actual data and found it to be a reasonably good fit (see **Figure 13**).

The Dow Jones Index is difficult to model exactly because it tends to fluctuate chaotically; however, it is not difficult to model the index as a smooth curve to give us a general idea of the growth of the index over time. Since the Dow Jones

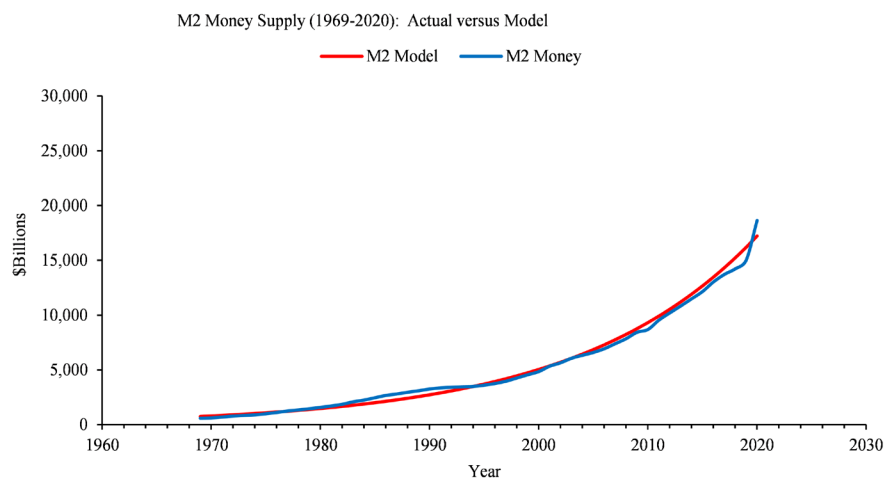


Figure 13. M2 money supply measured in \$ billions as reported on the last day of each respective fiscal year from 1969 through 2020 compared with the mathematical model.

Index is positively correlated with the M2 Money Supply, we can model the index with an equation of the form

$$D = k_1 \cdot M(t), \tag{8}$$

where k_1 is a constant of proportionality. We used the sum of least squares method to solve for $k_1 = 1.500623$ (see **Figure 8**). It follows the equation

$$D = 1.500623(M(t)), \tag{9}$$

which simplifies to

$$D = 1126.637e^{0.061427t}. \tag{10}$$

This equation gives a graph of a smooth curve that approximates the value of the Dow Jones Index (D) at time (t) (see **Figure 14**).

Based on our assumption, the Dow Jones Index cycles approximately every eight years. We decided to approximate the fluctuations in the Dow Jones Index by modeling the change in the Dow Jones Index as a Trigonometric function. We chose to model the fluctuations with a negative ($-$) cosine function shifted to the right by one year to give a minimum value in 1970, which corresponds to the halfway point of President Nixon’s first term in office. Consequently, this function also gives a minimum value in 2009, which corresponds with bottoming out of the 2008 financial crisis. The form of this function is as follows

$$D = A \cdot (-) \cos\left(\frac{2\pi}{P}(t-1)\right) + k_1(M(t)), \tag{11}$$

where

A = Amplitude,

P = Period,

k_1 = Constant of proportionality,

$M(t)$ = M2 Money supply at time (t).

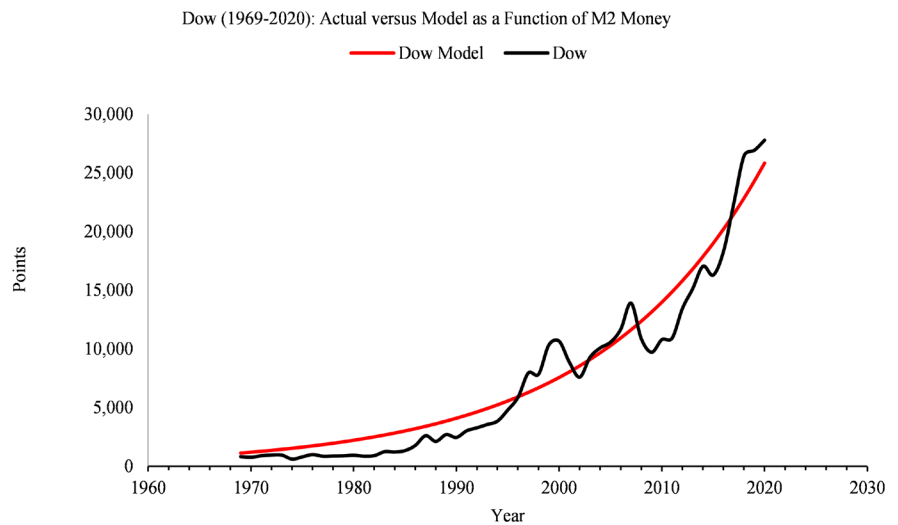


Figure 14. Dow Jones index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020 compared with the mathematical model.

We computed the amplitude as the average percent change in the Dow between 1969 and 2020 using the formula

$$\text{Amplitude} = (\text{Average annual percent change in the Dow}) \cdot k_1 M(t).$$

To compute the period for our trigonometric function, we considered our assumption that the Dow has tended to cycle every eight years since 1970. We have eight full cycles spread over 52 data points for Dow Index values. Therefore, the

$$\text{period} = \frac{\text{number of data points}}{\text{number of cycles}} = \frac{52}{8} = \frac{13}{4}.$$

After performing the necessary calculations and a little experimentation, we found the equation of the form

$$D(t) \approx (0.1498)(1.500623)(M(t)) \left(-\cos\left(\frac{4\pi}{13}(t-1)\right) \right) + (1.500623)(M(t)), \tag{12}$$

provided a fair approximation. Substituting the value $M(t)$ in Equation (12) and simplifying gives the equation of the form

$$D \approx -168.78875e^{0.061427t} \cos\left(\frac{4\pi}{13}t\right) + 1126.637e^{0.06427t}. \tag{13}$$

We verified this result to be reasonable by comparing the model with the actual data in **Figure 15**.

For the National Debt, we assumed the National Debt is proportional to the Dow Jones Index. Since we know there is a strong correlation between the National Debt and the Dow Jones Index, we can model the National Debt with an equation of the form

$$N(t) = k_2 \cdot D(t), \tag{14}$$

where k_2 is a constant of proportionality. Again, we used linear regression to solve for k_2 and then we found the line of best fit to be where $k_2 = 0.9203$ (see **Figure 9**). This gives the equation

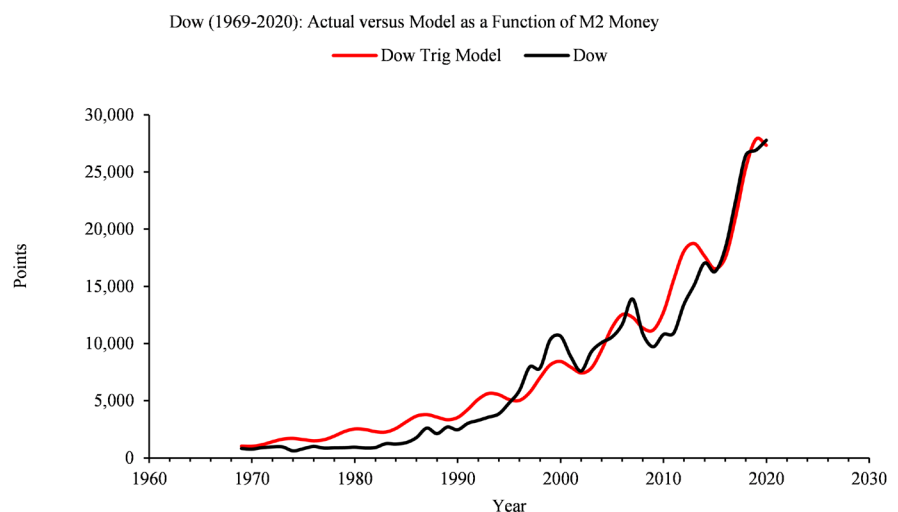


Figure 15. Dow Jones index measured in points as reported on the last day of each respective fiscal year from 1969 through 2020 compared with the mathematical model.

$$N(t) = 0.9203(D(t)). \tag{15}$$

Since we had two equations for $D(t)$, we had to choose which one provided the better approximation of the actual National Debt numbers. We tested the model with both equations and found that Equation (7), which models the Dow Jones Index as a smooth curve, provided a better fit. Therefore, we substituted Equation (10) for $D(t)$ in the formula for $N(t)$. This produces the following equation

$$N(t) = 0.9203(1126.637e^{0.061427t}). \tag{16}$$

Equation (13) simplifies to

$$N(t) = 1036.843e^{0.061427t}. \tag{17}$$

Consequently, we modeled the National Debt (N) by Equation (17) and verified the results by comparing the model with the actual data (see **Figure 16**).

3. Results

In summary, our work has produced the four model Equations (7), (10), (13), and (17).

Putting those equations together on the same graph gives a trend picture of the United States economy modeled as a function of the M2 Money Supply (see **Figure 17**).

Comparing the model to the actual data revealed that the model captures the general year-to-year trends in the United States economy during the years 1969-2020 (see **Figure 4** and **Figure 15**). However, being that this model is data-driven, it should be considered both fragile and sensitive [13]. Nevertheless, we can project the model out for several years to see what might happen if our assumptions hold (see **Figure 18** and **Table 3**).

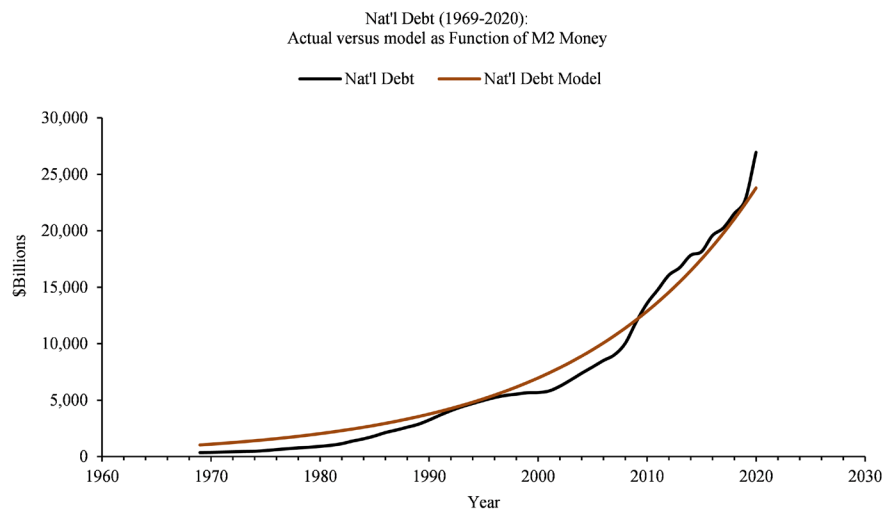


Figure 16. National debt measured in \$ billions as reported on the last day of each respective fiscal year from 1969 through 2020 compared with the mathematical model.

Table 3. Computed values for the economy modeled as a function of the M2 Money Supply from 1969 through 2020 with projections through 2030.

t	Year	$M = f(t)$	$D = g(f(t))$	$D = \text{Cosine Function}$	$N(t) = h(g(f(t)))$
0	1969	750.78	1126.64	1035.44	1036.84
1	1970	798.34	1198.01	1018.63	1102.53
2	1971	848.92	1273.91	1160.32	1172.38
3	1972	902.70	1354.62	1420.21	1246.65
4	1973	959.89	1440.43	1648.13	1325.63
5	1974	1020.70	1531.69	1708.43	1409.61
6	1975	1085.37	1628.73	1607.41	1498.92
7	1976	1154.13	1731.91	1506.31	1593.88
8	1977	1227.25	1841.63	1593.19	1694.85
9	1978	1305.00	1958.31	1913.25	1802.23
10	1979	1387.67	2082.37	2308.86	1916.40
11	1980	1475.58	2214.30	2538.86	2037.81
12	1981	1569.07	2354.58	2490.60	2166.92
13	1982	1668.47	2503.75	2301.08	2304.20
14	1983	1774.17	2662.37	2263.72	2450.17
15	1984	1886.57	2831.03	2578.59	2605.40
16	1985	2006.09	3010.39	3156.16	2770.46
17	1986	2133.18	3201.11	3662.66	2945.97
18	1987	2268.33	3403.90	3796.68	3132.61
19	1988	2412.03	3619.55	3572.18	3331.07
20	1989	2564.84	3848.86	3347.51	3542.10
21	1990	2727.33	4092.70	3540.58	3766.51
22	1991	2900.11	4351.98	4251.85	4005.12
23	1992	3083.85	4627.69	5131.02	4258.86
24	1993	3279.22	4920.87	5642.16	4528.67
25	1994	3486.96	5232.62	5534.90	4815.58
26	1995	3707.87	5564.12	5113.73	5120.66
27	1996	3942.78	5916.62	5030.71	5445.06
28	1997	4192.56	6291.46	5730.45	5790.02
29	1998	4458.17	6690.04	7014.00	6156.84
30	1999	4740.61	7113.87	8139.60	6546.89
31	2000	5040.94	7564.56	8437.43	6961.66
32	2001	5360.30	8043.80	7938.52	7402.70
33	2002	5699.89	8553.39	7439.23	7871.68
34	2003	6061.00	9095.28	7868.29	8370.37
35	2004	6444.98	9671.49	9448.96	8900.66

Continued

36	2005	6853.29	10,284.20	11,402.75	9464.54
37	2006	7287.46	10,935.74	12,538.67	10,064.15
38	2007	7749.14	11,628.55	12,300.30	10,701.74
39	2008	8240.07	12,365.25	11,364.33	11,379.73
40	2009	8762.11	13,148.62	11,179.84	12,100.67
41	2010	9317.21	13,981.63	12,734.88	12,867.28
42	2011	9907.48	14,867.40	15,587.35	13,682.46
43	2012	10,535.15	15,809.30	18,088.78	14,549.28
44	2013	11,202.58	16,810.86	18,750.67	15,471.02
45	2014	11,912.30	17,875.88	17,641.91	16,451.15
46	2015	12,666.98	19,008.36	16,532.33	17,493.38
47	2016	13,469.47	20,212.60	17,485.84	18,601.64
48	2017	14,322.79	21,493.12	20,998.60	19,780.10
49	2018	15,230.19	22,854.78	25,340.54	21,033.23
50	2019	16,195.06	24,302.69	27,864.93	22,365.74
51	2020	17,221.06	25,842.34	27,335.19	23,782.68
52	2021	18,312.07	27,479.52	25,255.16	25,289.38
53	2022	19,472.19	29,220.43	24,845.16	26,891.53
54	2023	20,705.81	31,071.63	28,300.97	28,595.19
55	2024	22,017.58	33,040.10	34,640.05	30,406.78
56	2025	23,412.46	35,133.29	40,199.03	32,333.13
57	2026	24,895.71	37,359.08	41,669.95	34,381.53
58	2027	26,472.92	39,725.89	39,205.94	36,559.70
59	2028	28,150.06	42,242.64	36,740.11	38,875.86
60	2029	29,933.44	44,918.83	38,859.10	41,338.76
61	2030	31,829.81	47,764.57	46,665.59	43,957.69

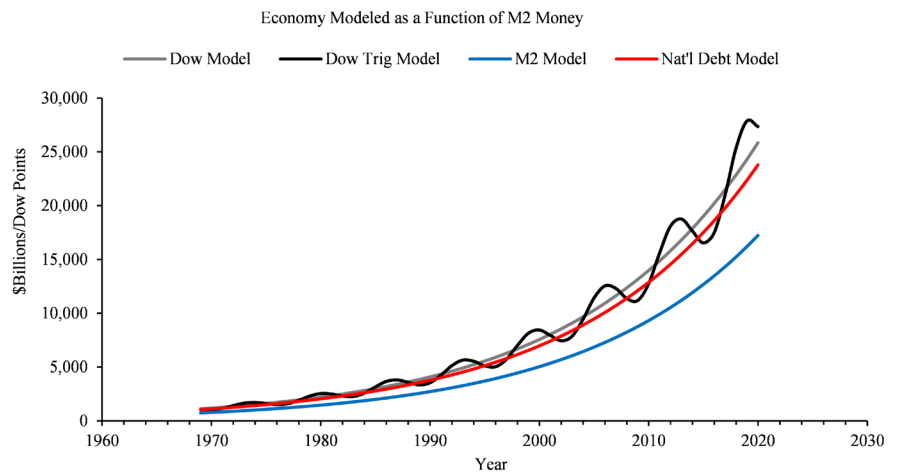


Figure 17. Comparison of mathematical models of Dow Jones index measured in points, M2 money supply measured in \$ billions, and National Debt measured in \$ billions from 1969 through 2020.

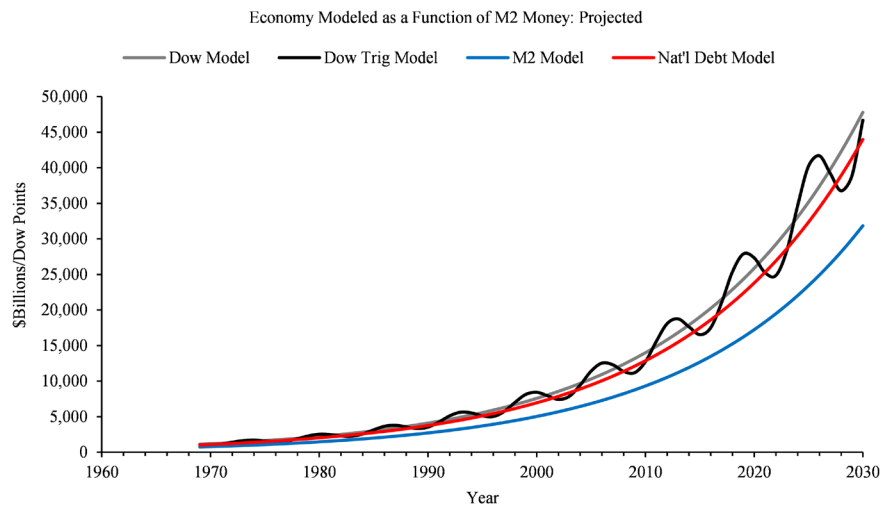


Figure 18. Comparison of mathematical models of Dow Jones index measured in points, M2 money supply measured in \$ billions, and National Debt measured in \$ billions projected through 2030.

Our model of the macroeconomic data we studied may raise more questions than it provides answers. However, these questions are both relevant and difficult to answer. If we were confident in the model's ability to predict the future, we might feel good about long-term investment in stock market index funds. Our model holds, it looks encouraging for those who hold a substantial portfolio of well-diversified assets in the companies whose stock values are tied to the Dow Jones Industrial Index, or any other major index for that matter. On the other hand, our results are troubling for persons who lack the disposable income to invest. What does the future look like for people in that situation? Will they continue to become less wealthy relative to the money supply? Is there a limit to how long this can go on before it causes an economic or political crisis or both? Is wealth trickling up rather than down? If so, has increasing the money supply operated as a mechanism by which relative wealth is transferred away from the middle and lower socioeconomic class in favor of the wealthiest participants in the U.S. economy? Analysis of other data sets may be required to answer these questions; however, our research does, we believe, provide a reasonable basis for posing these questions.

As mentioned above, the construction of our model makes it a fairly accurate illustration of some of the past general macroeconomic trends in the United States Economy. However, due to the methods we used to construct the model, its reliability in making future predictions should be viewed with suspicion. We could ask what might happen if the US Dollar ceased to be the world's reserve currency, but this model will not tell us. We could ask exactly how much US currency the world market will tolerate before people begin to become unwilling to trade for US currency or invest in the US bond market. However, this model is not built to analyze that contingency. All we can say for certain is that our model's future predictions prove accurate, a certain segment, perhaps the major-

ity, of the US population is likely to find themselves in economic distress unless increasing household profit margins prove to be a natural consequence of increased money supply and market growth. Unfortunately, as is discussed in more detail below, this has not been the general trend and we find no compelling reason to believe this is likely to change.

Overall, we are pleased with the accuracy of the model we constructed with respect to the data we considered. Arguments could be made for taking more measurements over a shorter or longer period of time, and that could be done by applying the same modeling techniques to those other measurements. Finally, as is perhaps often the case, our results give us some idea of where we have been and help us to better frame the questions we might wish to consider and the assumptions we might want to make in future research relevant to the US Economy.

4. Discussion

The models represented by Equations (7), (10), (13), and (17) could be used to aid readers in understanding the general fiscal, economic, and even political trends in the United States since 1969. Although future predictions based on these models should be viewed with caution, these figures are instructive for the analysis and general understanding of how the United States economy arrived at its present situation and where it might go given a set of specific assumptions.

The modeled projections cause us to question the sustainability of the patterns of growth in the M2 Money Supply, National Debt, and stock market indices as having more accomplished researchers who have done earlier [19]. The Federal Reserve typically increases the M2 Money Supply anytime falling market indices become a concern, a process known in the industry as "Quantitative Easing" [5]. However, the Federal Reserve Bank has been reluctant to decrease the M2 Money Supply once commodity prices fall. As others have pointed out, the increased M2 Money Supply is correlated with extremely low-interest rates [5]. Barry Ritholtz, author and co-founder, chairman, and chief investment officer of Ritholtz Wealth Management LLC, have argued that the low-interest rates have driven the actual cost of living far above those reflected by the CPI⁷, a standard benchmark for reporting inflation [21]. A survey of relevant data supports this assertion [9] [10] [22]-[28] (see **Figures 19-22**).

To illustrate this point, consider two accounts opened in 1969, each with an initial one-dollar deposit. No other deposits or withdrawals are made. The first account grows at the rate of inflation in the M2 Money Supply; it is represented by the black line in **Figure 19**. The second account grows at the rate of inflation estimated by the CPI; it is represented by the red line in **Figure 19**. The first

⁷"The Consumer Price Index (CPI) is a measure of the average change over time in the prices paid by urban consumers for a representative basket of consumer goods and services. ... CPI indexes are used to adjust income eligibility levels for government assistance, federal tax brackets, federally mandated cost-of-living increases, private sector wage and salary increases, poverty measures, and consumer and commercial rent escalations. Consequently, the CPI directly affects hundreds of millions of Americans." [20]

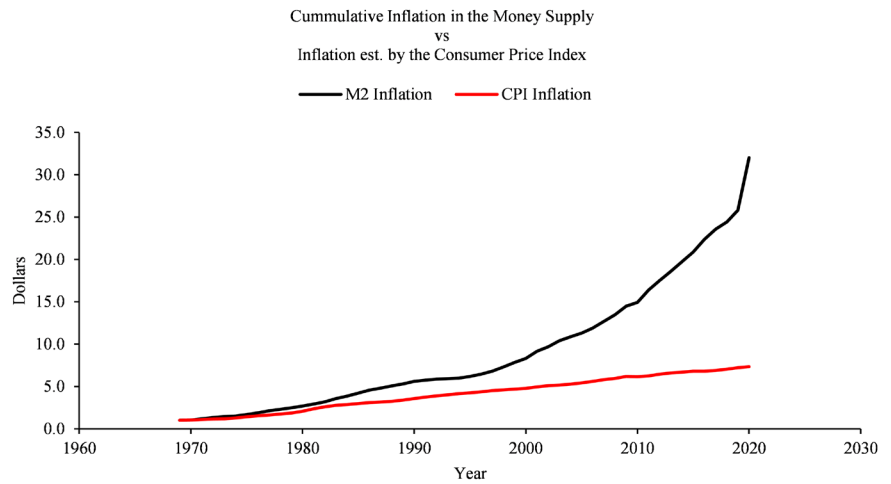


Figure 19. Cumulative consumer price index inflation versus actual cumulative inflation in the M2 money supply 1969-2020.

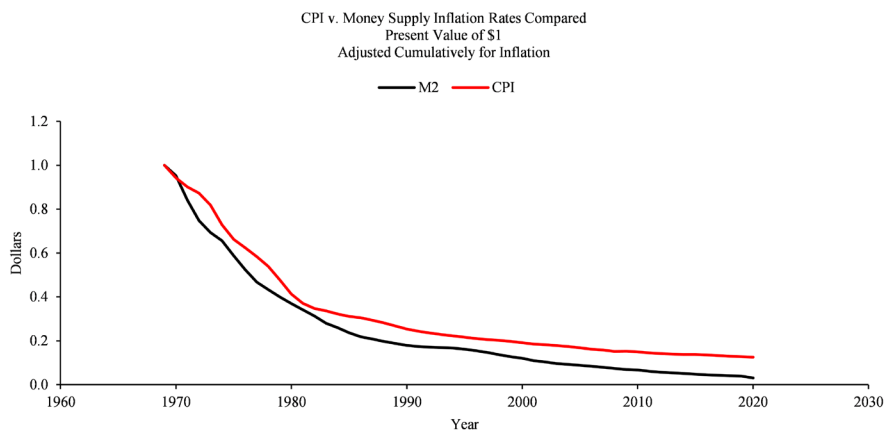


Figure 20. Present value of \$1 adjusted cumulatively for consumer price index inflation and actual inflation in the M2 Money supply, respectively, 1969-2020.

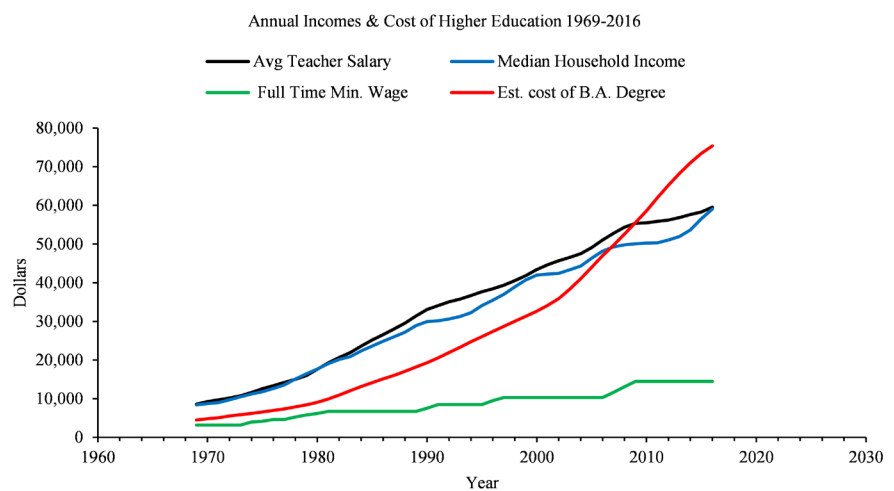


Figure 21. Changes in US average teacher salary, median household income, minimum wage times 2000 hours per year, and the estimated cost of a 4-year college degree compared.

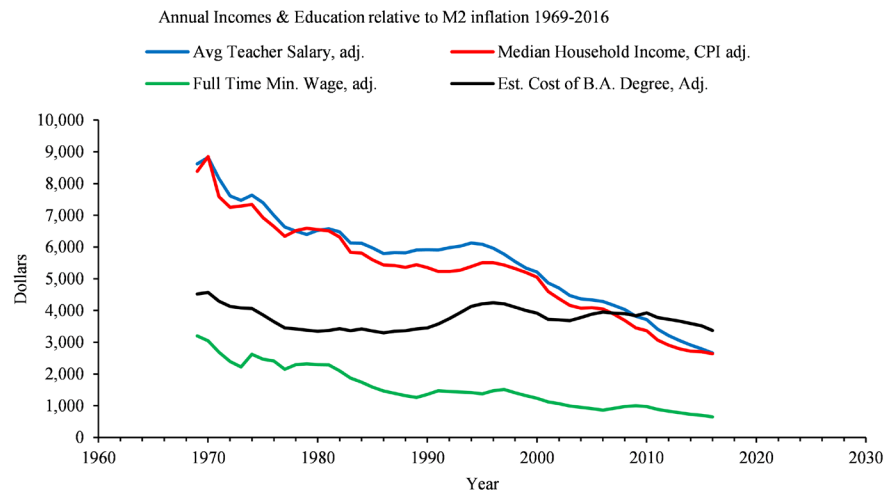


Figure 22. Changes in US Average teacher salary, median household income, minimum wage times 2000 hours per year, and the estimated cost of a 4-year college degree relative to inflation in the M2 money supply.

investment in this example is analogous to a well-diversified stock portfolio. The second account is analogous to an investment in median household income since the rate of change in median household income is roughly equivalent to the rate of change in the CPI. As **Figure 19** illustrates, the median household income is clearly losing this competition. In fact, we calculated that had the median household income increased at the same rate as the M2 Money Supply from 1969 until 2020. The median household income in 2020 would have been approximately \$216,500, and after the unprecedented increase in the Money in 2020, the median household in 2020 would have exploded to approximately \$268,750.

This further raises questions about whether the average American has enough income margin to absorb the continued rise in the cost of living, particularly if there is a sudden and unexpected increase in the price of an important commodity, such as crude oil or any other major expense like a substantial tax increase. Can the M2 Money Supply increase to infinity without consequence? We conjecture this is not likely the case. We suspect there is a limit to the amount of M2 Money the world can endure somewhere towards this side of infinity; we just do not know where that limit is. However, it appears that if such a limit exists, the Federal Reserve Bank is destined to find it.

4.1. Conclusions

The process of gathering, organizing, and analyzing the data turned out to be useful and repeatable. Although the purpose of this paper was to investigate mathematically and explore an area of curiosity within the realm of the social science of macroeconomics, our models beg important questions regarding the plans we should lay for the future. In retrospect, we considered Aaron Kasteler's assertion that "increasing the quantity of money in circulation has not been beneficial to the American public" [5]. Our research does not necessarily show that the M2

Money Supply has been of no benefit to the American people. On the contrary, it appears that anyone who has held a well-diversified investment portfolio in large-company stocks for any significant length of time has most likely benefitted a great deal from the monetary and fiscal policies of the past 50 years. On the other hand, the evidence we have reviewed and analyzed causes us to have two questions: 1) How long the US currency will remain the world's reserve currency? 2) What happens if, and when, the US dollar loses its reserve currency status? Whether the monetary and fiscal policies of the past half-century, while beneficial to some in the short term, may prove detrimental to the American people in the long run is an open question for future research.

While our models rely on a very specific set of assumptions, there are an enormous number of other variables and assumptions which might be considered in future studies of the topics discussed herein. As novices ourselves, it is simply our hope that our study will serve as a source of motivation for future investigators who undertake the study of applied mathematics. For example, we have not considered the net effect of the disparity between wage and savings growth rates and the growth rates of the money supply and the market indices; however, our review of the literature suggests that such a discrepancy does, in fact exist. We hope the modeling techniques we have employed herein will prove useful for some future investigations of that issue.

4.2. Extension and Applications

As a corollary to our research, we have, in the process of deriving Equations (7), (10), and (13), discovered the equations necessary to model the economy solely in terms of money with the M2 Money supply as the independent variable. e.g.,

$$D = 1.500623(M), \quad (18)$$

$$N = 0.9203(1.500623(M)). \quad (19)$$

Given the historical maximal and minimal fluctuations in the Dow Index, one could also apply that knowledge to our model formula to estimate the probable upper and lower bounds of the Dow Index at some future time based on the amount of M2 Money presently in circulation (see **Table 2**). e.g., we had the following as of the end of the fiscal year 2020:

$$D_{\text{midline}} = 1126.637e^{0.061427t}, \quad (20)$$

$$D_{\text{upper bound}} = 1126.637e^{0.061427t} + 0.469(1126.637e^{0.061427t}), \quad (21)$$

$$D_{\text{lower bound}} = 1126.637e^{0.061427t} - 0.358(1126.637e^{0.061427t}). \quad (22)$$

Although these rather simple equations are far from a crystal ball, they do give us a general idea of the potential impact an increase or decrease in the M2 Money Supply may have on index fund investments, national debt, tax policy, or the federal government's ability to fund programs such as national defense, higher

education, social security, and public healthcare programs. In evaluating the potential changes in stock market indices, the wary investor should keep in mind that, between 1969 and 2020, the Dow Jones Index has been known to drop as much as 35.8%, and rise as much as 46.9%, from the end of one fiscal year to the end of the next (see **Table 2**). However, knowledge of the likely midline and upper and lower bounds of the market index could prove helpful in weighing long-term investment risks and opportunities (see **Figure 23**).

Important questions remain regarding the stability and sustainability of current trends in fiscal and monetary policy. However, these models may provide a springboard for analyzing and understanding the practical impact past policy decisions have had on the present and the impact present policy decisions may have on future generations.

4.3. Possible Related Research Topics

The modeling techniques used herein are adaptable to any data set that bears a strong positive or negative correlation to the M2 money supply, national debt, or any given stock market index. These techniques are also adaptable to modeling the broader overall changes in the economy versus the rates of change in, for example, median incomes, tuition prices, real estate valuations, etc., all of which could help individuals ascertain their future financial needs and weigh their investment options. It may be interesting to model the comparison between inflation in the M2 money supply and various other inflation indices such as the CPI. It is also possible to adjust the value of a dollar to account for changes in the M2 money supply which may cause us to ask exactly what we have accomplished economically over the past half-century (see **Figure 6** and **Figure 24**).

Exploring these related topics might allow individuals to weigh their past, present, and future financial positions relative to the amount of money in circulation. Although more sophisticated modeling techniques exist in the world of

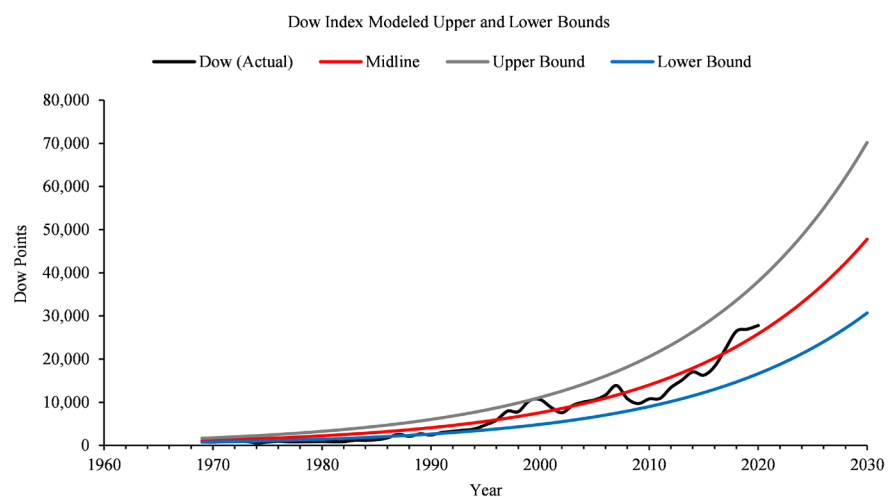


Figure 23. Comparison of actual Dow Jones index data (1969-2020) with mathematical models of Dow Jones index midline, and upper and lower bounds projected through 2030.

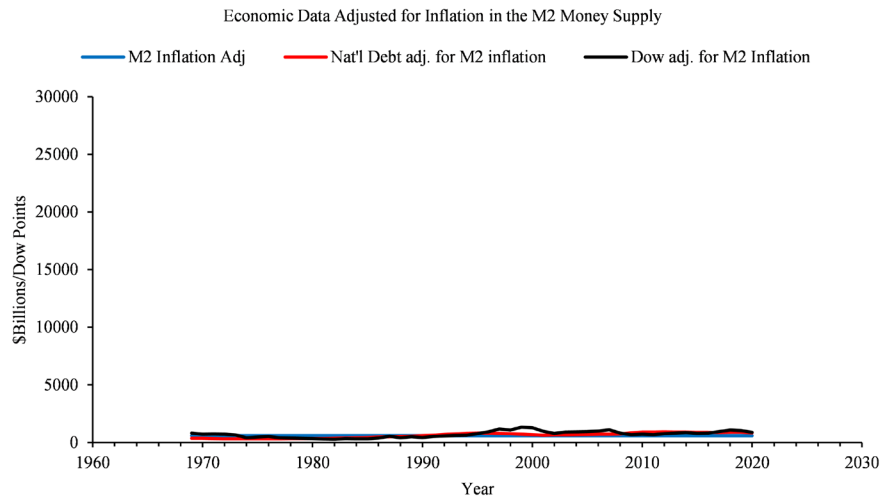


Figure 24. M2 money supply, national debt, and Dow Jones data adjusted for inflation in the M2 money supply since 1969 on the same scale as in **Figure 6**.

economics, the models discussed herein remain useful for the general understanding necessary for adopting a reasonable position regarding fiscal and monetary policy. While these models may prove useful in planning for the future, their simplicity may at the very least make them useful for arousing curiosity in the researchers' minds to the next generation.

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Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

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