

Supplement of

Improved representation of phosphorus exchange on soil mineral surfaces reduces estimates of phosphorus limitation in temperate forest ecosystems

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S1 Additional figures and tables

Table S1: The normalized root mean square ratio (K_{nrmsr}) between simulated and observed soil properties along soil profiles of four models at five study sites (Fig. 2).

Soil	Site	4pool	siLang	dbLang	Control
properties					
SOC	BBR	0.32	0.32	0.32	0.32
	MTF	0.59	0.58	0.59	0.59
	VES	0.56	0.54	0.56	0.56
	COM	0.47	0.49	0.47	0.47
	${\rm LUE}$	0.59	0.58	0.63	0.61
SOM CN ratio	BBR	0.9	0.90	0.90	0.90
	MTF	0.95	0.95	0.95	0.95
	VES	0.93	0.93	0.93	0.93
	COM	0.85	0.84	0.85	0.85
	${\rm LUE}$	0.84	0.84	0.85	0.86
SOM CP ratio	BBR	0.54	0.54	0.54	0.54
	MTF	0.58	0.58	0.58	0.58
	VES	0.74	0.74	0.74	0.74
	COM	0.76	0.73	0.76	0.76
	LUE	0.61	0.61	0.63	0.67
Bulk density	BBR	0.69	0.69	0.69	0.69
	MTF	0.76	0.76	0.76	0.76
	VES	0.79	0.79	0.79	0.79
	COM	0.66	0.61	0.66	0.66
	${\rm LUE}$	0.81	0.81	0.82	0.84
SOP	BBR	0.33	0.33	0.33	0.33
	MTF	0.39	0.40	0.39	0.40
	VES	0.46	0.46	0.46	0.46
	COM	0.49	0.52	0.49	0.49
	LUE	0.49	0.50	0.45	0.42
SIP	BBR	0.77	0.78	0.77	0.79
	MTF	0.85	0.78	0.85	0.81
	VES	0.78	0.72	0.81	0.78
	COM	0.76	0.68	0.80	0.82
	LUE	0.81	0.81	0.81	0.77

Table S2 Parameters for sensitivity analysis

k_{des}	$PO4$ desorption rate from $Psorb$		P/kg μ mol	Yang et al.
	to Plab	733	soil/s	2014
$K_{m,PO_{A}}^{pH}$	Correction coefficient of pH on	0.4		this study
	Langmuir Km			
$Q_{max.PO_4}^{Al/Fe}$	Phosphate sorption capacity of	9.134	mmol P/kg	this study
	Al/Fe oxides		clay	
Q^{fs}_{max,PO_4}	Phosphate sorption capacity of	9.134	mmol P/kg	this study
	fine soil		fine soil	
Q_{max,PO_4}^{sand}	Phosphate sorption capacity of	4.567	mmol P/kg	this study
	sand		sand	
Q^{OM}_{max,PO_4}	Phosphate sorption capacity of	4.567	mmol P/kg	this study
	organic matter		OM	

Table S3. The weighted mean values of partial correlation coefficient against all the output variables (Fig. 5) for the 16 selected parameters (Table S2) in the LHS sensitivity runs. Overall importance of parameters is measured by first calculating the RPCC for each output variable and then calculating the mean of the absolute RPCC values across selected outputs in Fig.5, weighted by the uncertainty contribution of these model outputs

Figure S1: Reported Smax, Km, and Ptot in batch experiment data. The plot is produced based on 258 data inputs from [1-27]. The processing details are given in Section "A1 Processing of the reviewed data".

Figure S2: Simulated GPP, LAI, aboveground C, fine root C, plant uptakes of N and P. The simulated values are the yearly average of the period 2006–2015. The lime line represents the Langmuir model with only four inorganic P pools (4pool), the blue line represents the singlesurface Langmuir model (siLang), the red line represents the double-surface Langmuir model (dbLang), and the light sky-blue line represents the Control model.

Figure S3: 4pool model responses to C and P fertilisation. The simulated values are the yearly average of the period 2006–2015. The lime line represents the 4pool model, the blue line represents the CO2 fertilization, the red line represents the P fertilization, and the light sky-blue line represents the C&P fertilization.

Figure S4: dbLang model responses to C and P fertilization. The simulated values are the yearly average of the period 2006–2015. The lime line represents the 4pool model, the blue line represents the CO2 fertilization, the red line represents the P fertilization, and the light sky-blue line represents the C&P fertilization.

Figure S5: siLang model responses to C and P fertilization. The simulated values are the yearly average of the period 2006–2015. The lime line represents the 4pool model, the blue line represents the CO2 fertilization, the red line represents the P fertilization, and the light sky-blue line represents the C&P fertilization.

Figure S6: Normalized output variations in the LHS sensitivity analysis of siLang and dbLang models at COM and MTF sites. The selected output variables include GPP (kg C/m^2 /yr), foliar N content (mg N/g d.w.), foliar P content (mg P/g d.w.), plant C (kg C/m^2), SOC stock (kg C/m^2), SOP and SIP stocks (g P/m²) and Lab-to-Exchangeable P ratio. All the calculations are performed based on data from the last 10 years of 1000 LHS simulations, and soil variables are based on the topmost 1m of soil. The numbers below bars are the mean values of the 1000 LHS runs, and bars are the distribution of all 1000 LHS runs normalized to the mean value.

Variation in output variables (each normalized by the mean) for siLang and dbLang at sites COM and MTF

The simulated annual GPP was lower in siLang $(1.37 \pm 0.12 \text{ and } 1.72 \pm 0.12 \text{ kg C/m}^2/\text{yr}$ for COM and MTF) than in dbLang $(1.65 \pm 0.04 \text{ and } 1.82 \pm 0.01 \text{ kg C/m}^2/\text{yr}$ for COM and MTF), and siLang responded more strongly to changes of P cycling processes parameterization than dbLang (Figs. 5 and S6), reflecting a stronger Pcontrol on plant productivity in the silang model. This stronger P limitation also led to lower plant and soil C in silang (plant C: 7.67 \pm 1.58 and 12.51 \pm 1.55 kg C/m² for COM and MTF; soil C: 13.31 \pm 0.94 and 15.50 \pm 0.96 kg C/m² for COM and MTF) than in **dbLang** (plant C: 12.40 \pm 1.06 and 14.14 \pm 0.07 kg C/m² for COM and MTF; soil C: 15.78 \pm 0.76 and 16.04 \pm 0.95 kg C/m² for COM and MTF).

Figure S7: Responses of Labile-to-Active P fraction to changes in parameterization in siLang and dbLang models at COM and MTF sites

(c) COM_siLang Distribution of Labile-2-Active P under varying k_desorpt_po4

under varying tau_slow 0.0 0.2 soil depth, m
0.4 0.6 $_{0.8}$ 0.8 19 $\frac{0.4}{\text{mol/mol}}$ 0.0 0.8 0.2 0.6

(b) MTF_dbLang Distribution of Labile-2-Active P

(d) COM_dbLang Distribution of Labile-2-Active P under varying tau_slow

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5 S2 Processing of the reviewed data

As most P species present in soil solution are negatively charged, the major P sorbents are those constituents that bear positive charges. These include hydroxyl (Fe and Al oxides), carboxyl (organic matter) or silanol (clays) groups [28]. Of the studies that we reviewed, the P sorption capacity of soils has been variously related to soil pH [18, 23, 29], mineralogy or clay content [30-32], organic complexes of Fe and Al [33], soil organic matter such as DOC, organic acids, DOP etc. [29, 34-37], calcium 10 carbonate [8, 26], soil pedogenesis [32, 35], extractable Fe and Al oxides, hydroxides, and oxyhydroxides, and other soil

properties. The correlation between soil properties and Langmuir parameters are demonstrated in the figure below,

Figure S8: Correlation between reported soil properties and Langmuir parameters from reviewed literature. More details given below.

- 15 To derive Figs. S1 and S8, the raw data from reference [1-27] were processed in the following steps:
	- 1. Conversion of Langmuir coefficient from K_L to K_m . The Langmuir isotherm in the batch sorption experiments were reporting the Langmuir coefficient either as K_L in the unit of L/mg P, or as K_m in the unit of mg P/L. We unified the Langmuir coefficient to K_m by inverting $1/K_L$. To further generate the data for Table 1 and Fig. 2, we assumed that the soil water content for all experiments data are 330 L/m³ soil and converted the unit from mg P/L to g P/m².
- 20 2. Selection of reported soil properties. The reviewed papers don't follow the same protocols in reporting the soil properties, apart from the two Langmuir isotherm parameters $(S_{max}$ and K_m), many studies also reported organic matter contents (OM, in percent), soil texture (clay, silt and sand), pH (measured in water or CaCl2/KCl), total soil P (Ptot,

mg P/ kg soil), available P (Pavi, mg P/kg soil). We selected the abovementioned variables (pH as water measured values) to understand their relationships with Langmuir parameters.

25 Conversion of OM and soil texture to weights. In order to derive a weight-based relationship between Langmuir parameters, the reported OM contents and soil texture were converted to OM and clay, silt, sand weights, assuming an OM density of 250 $kg/m³$ and mineral soil bulk density of 1000 kg/m³. The correlation between the soil properties and Langmuir parameters are plotted in Fig. S7, where WOC, Wclay, Wsilt, Wsand are the OM, clay, silt, and sand weights [kg/m³], respectively, and Wfs stands for weight of fine soil (clay plus silt).

30 S3 Double-surface Langmuir isotherm and parametrization

As both single- and double-surface Langmuir isotherm could be fitted against the same experiments data, the apparent maximum sorption capacity (S_{max}) in Eq. 1 is the sum of sorption maxima of two sorption sites ($S_{\text{max},1}$ and $S_{\text{max},2}$, Eqs. 3.1 and 3.2) and the apparent Langmuir coefficient (K_m) in Eq. 1 could be derived mathematically from the Langmuir coefficients of two sorption sites $(K_{m,1}$ and $K_{m,2}$, Eqs. 3.4 and 3.5).

35 Following the concept of double-surface Langmuir isotherm, we assume that the apparent maximum sorption capacity and Langmuir coefficient in all the batch sorption experiment are in fact a combined value of two (or more) sorption surfaces.

$$
S = S_{max} \frac{P_{sol}}{K_m + P_{sol}} = S_{max,1} \frac{P_{sol}}{K_{m,1} + P_{sol}} + S_{max,2} \frac{P_{sol}}{K_{m,2} + P_{sol}},
$$
(S1)

Where the apparent maximum sorption capacity is the sum of sorption maxima of individual sorption surface,

$$
S_{max} = S_{max,1} + S_{max,2} \tag{S2}
$$

40 The apparent Langmuir coefficient is calculated in Eq.3d which is derived using the differential form of double-surface Langmuir isotherm,

$$
\frac{dS}{dt} = \frac{S_{max}K_m}{(K_m + P_{sol})^2} \frac{dP_{sol}}{dt} = \frac{S_{max,1}K_{m,1}}{(K_{m,1} + P_{sol})^2} \frac{dP_{sol}}{dt} + \frac{S_{max,2}K_{m,2}}{(K_{m,2} + P_{sol})^2} \frac{dP_{sol}}{dt}
$$
, thus (S3)

$$
K_m = \frac{\frac{S_{max}}{hl} - 2P_{sol} \pm \sqrt{\frac{S_{max}^2}{hl^2} - 4\frac{S_{max}P_{sol}}{hlp}}}{2},
$$
 where (S3.1)

$$
hlp = \frac{S_{max,1}K_{m,1}}{(K_{m,1} + P_{lab})^2} + \frac{S_{max,2}K_{m,2}}{(K_{m,2} + P_{lab})^2}
$$
(S3.2)

- 45 To estimate the sorption maximum and Langmuir coefficient of each sorption surface, we derived pedo-functions based on the reported soil properties from the batch sorption experiment data. As shown in Fig.S2, the maximum sorption capacity is positively correlated with clay and silt content, negatively correlated with sand content and does not show correlation with OM content; the Langmuir coefficient is strongly correlated with soil pH and OM content and not correlated with soil texture. Given the high uncertainty in the original experiment data, and the lack of extractable Al and Fe content that represent
- 50 crystalline and non-crystalline Fe and Al oxides and organic complexes of Fe and Al, which are commonly considered the

main sorbents of P, we tested different combination of soil sorbents and finally used a four sorbents pedo-functions for S_{max} and K_m ,

Where $Q_{max,PO_4}^{Al/Fe}$ is the sorption capacity of crystalline and non-crystalline Fe and Al oxides normalized by the clay content; 60 f_{Al/Fe} is the correction coefficient of oxalate-extractable Al and Fe, which is calculated in Eq. 4.3, assuming that most Al- $\&$ Fe- (hydro)oxides reside in clay and the rest in silt; k_{ph} is a unitless correction factor to account for the effect of pH, and $K_{m,l}$ and $K_{m,2}$ are calculated using Eqs.4.4 and 4.5.

Table S4: Parameters for double-surface Langmuir isotherm

65 S4 Deep soil inorganic P initialization

The initial inorganic P pools of soils deeper than 1m was calculated using the following equations:

$$
P_{primary}^{frac} = min\left(\frac{2*\sqrt{z}, 3.4}{3.5}\right)
$$
\n(Fquation S5.1)
\n
$$
P_{exchange}^{frac} = \frac{0.8^{2*z}}{3.5}
$$
\n(Fquation S5.2)
\n
$$
P_{ocl}^{frac} = max\left(1 - P_{primary}^{frac} - P_{exchange}^{frac} \cdot \frac{0.1}{3.5}\right)
$$
\n(Fquation S5.2)
\n(Fquation S5.3)

70 Where z is the soil depth in m, and P_{exchangeable} includes P_{sorb} and P_{lab} with a constant ratio of 9/8 at all depths. The total soil inorganic P contents for all the study sites (g $P/m³$, >1m depth) are given in Table S5.

Table S5: The total soil inorganic P contents (g P/m³, >1m depth) for all study sites at specific depth at QUINCY initialization. The initial values of soil inorganic P contents at top 1 m soil were prescribed from the Hedley fractionation measurements.

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