

Simultaneous Routing with Washing Droplets in MEDA Biochips

Chiharu Shiro¹, Hiroki Nishikawa², Xiangbo Kong³, Hiroyuki Tomiyama^{1,*} and Shigeru Yamashita¹

¹Ritsumeikan University

²Osaka University

³Toyama Prefectural University

Abstract

Micro electrode dot array (MEDA) have attracted attention in the biochemical and medical industries. MEDA biochips enable biochemical experiments such as DNA analysis by manipulating droplets on the chip. Since the manipulation of droplets on the chip is based on the electro wetting on dielectric (EVoD) effect, a certain percentage of droplets may remain on the chip. Contamination cells on the chip due to left droplet has been considered as unavailable in previous studies. However, as the number of contaminated cells increases, droplets may not be able to move to the desired position if the contaminated cells are avoided. In order to clean the contamination, it is necessary to manually wash the chips or to move the droplets on the chips for washing. In this paper, we propose a method for simultaneous routing of washing droplets and functional droplets when a blockage occurs due to residual droplet contamination and reduce the droplet routing time by an average of 55% compared to existing method.

Keywords

MEDA, Mathematical Programming Problem, Droplet Routing, Washing Cells.

1. Introduction

Digital Microfluidic Biochips (DMFBs), a subset of Labs on a Chip (LoCs), have garnered attention in the fields of biochemistry and healthcare [1] [2] [3]. However, existing DMFBs face challenges in controlling the volume and shape of droplets during operation, as well as real-time droplet detection, posing functional and reliability issues for practical applications [4] [5].

Micro Electrode Dot Array (MEDA) biochips have been designed to deal these challenges. DMFBs control droplets using one electrode per cell, but MEDA biochips divide each cell into microelectrode cells (MCs). By utilizing MCs to control droplets, MEDA biochips enables precise manipulation of droplet size and shape, which was previously unattainable with DMFBs. Furthermore, real-time sensing is facilitated by integrating droplet detection circuits within MCs.

ATAIT 2024: The 6th International Symposium on Advanced Technologies and Applications in the Internet of Things, August 19–22, 2024, Kusatsu, Shiga, Japan


*Corresponding author.

✉ chiharu.shiro@tomiyama-lab.org (C. Shiro); nishikawa.hiroki@ist.osaka-u.ac.jp (H. Nishikawa);

kong@pu-toyama.ac.jp (X. Kong); ht@fc.ritsumei.ac.jp (H. Tomiyama); ger@cs.ritsumei.ac.jp (S. Yamashita)

© 2024 Copyright for this paper by its authors.

Use permitted under Creative Commons License Attribution 4.0 International (CC BY 4.0).

 CEUR Workshop Proceedings (CEUR-WS.org)

In DMFBs, the time required for droplet movement often constituted a small part of the overall process due to the complexity of mixing processes. However, MEDA biochips require fewer steps for mixing than DMFBs. As a result, the time required for droplet movement using MEDA biochips becomes more dominant in the overall process compared to using DMFBs.

During droplet movement on the biochip, there is a possibility of contamination when droplets partially remain in cells through which they have passed. These remain droplets have potential affecting the properties of subsequently passing droplets. There are lot of works to avoid the effect by remain droplets. One method has been proposed such as allowing only one type of droplet to pass through each cell to prevent interference from remain droplets [6], and the other method has been proposed such as washing cells to eliminate remain droplets [7] [8] [9]. However, these methods may cause to the no mixing routes of droplet under some conditions or to degradation of biochip cells due to unnecessary washing. Therefore, this paper proposes a routing method with washing droplets in MEDA biochips.

The contributions of this paper are as follows.

1. We achieve simultaneous routing method of target droplet and washing droplet on MEDA biochips.
2. We realize a routing method that solves problems caused by route contamination by using washing.
3. We solve routing problems with different droplet volume ratios.

The rest of this paper is organized as follows. Section 2 describes related work, and Section 3 formulates our droplet routing problem that routing with washing droplets simultaneously. Section 4 describes the experiments and a comparison of the results, and Section 5 describes the conclusions of this paper.

2. Related Work

Since the 2000s, extensive research has been conducted on efficient droplet routing in digital microfluidic biochips (DMFB) [5] [10]. However, due to the limitation of DMFBs to perform mixing only at a 1:1 volume ratio, the impact of droplet routing time is considered minimal for complex mixing ratios. Furthermore, the characteristic of DMFBs allowing movement only along the x and y axes affects routing efficiency [11]. Thus, DMFBs have many constraints, and most research on DMFBs has been conducted under these constraints.

In contrast, MEDA biochips achieves diverse droplet operations by dividing electrodes into microelectrode cells (MCs) [12] [13] [14] [15]. Droplets are moved using Electro Wetting on Dielectric (EWOD) achieved by operating MCs electrodes. MCs is equipped with devices to detect and control droplets, enabling real-time droplet detection within 10ms, which is impossible with conventional DMFBs [16]. By grouping MCs, it is possible to manipulate droplets of various volumes and perform non-1:1 mixing [17] [18]. Dilution and mixing operations that required several steps in DMFBs can be performed in a single step using the characteristics of MEDA biochips, significantly reducing the time required for each operation [19]. Given the higher flexibility and more numerous operations possible with MEDA biochips compared to DMFBs, methods used for DMFBs are not necessarily optimal for MEDA.

There is also extensive research on droplet routing leveraging the functions of MEDA biochips [6] [12] [13] [14] [15] [20]. Keszocze et al. proposed a method utilizing the deformation of droplets, a feature of MEDA biochips [12]. By taking advantage of the change in droplet movement speed due to droplet shape [20], there are methods that effectively use droplet deformation to minimize the time required for droplet movement [6]. In routing problems for MEDA biochips, it is often assumed that some cells are unusable due to MC or electrode failures. Many problems also consider scenarios where a part of the droplet remains as residue on a cell after a failed movement, preventing other droplets from using the cell to avoid interference with the residual droplet. It is known that if a certain number of unusable cells occur, there might be no possible paths for droplets [6].

Electrodes degrade over time with increased use, raising the likelihood of failures. Additionally, it is known that droplet movement time depends on droplet size [6] [19]. Therefore, when using larger droplets, certain electrodes endure prolonged stress to move the droplets. To extend the biochip's lifespan, it is necessary to use smaller droplets and distribute the load on the electrodes.

If a certain number of unusable cells occur or if there are too many droplets relative to the biochip's size, making it impossible to avoid interference with residual droplets, the biochip needs to be cleaned. In the former case, cleaning before routing solves the issue [21], but in the latter case, functional droplets, which are droplets intended for operations such as mixing, and cleaning droplets must be routed simultaneously. There are studies on simultaneously routing functional droplets and cleaning droplets [7] [8] [9]. These studies primarily focus on cleaning the crossing points of droplets when moving multiple functional droplets. However, since these three studies target DMFBs, they are not necessarily optimal for MEDA biochips due to differences in droplet sizes between cleaning and functional droplets. Therefore, this paper addresses the problem of routing functional droplets while cleaning unusable cells caused by residual droplets in MEDA biochips as an integer programming problem. It has been revealed that droplet movement can be hindered by contamination from residual droplets, making some paths nonviable. This study proposes a method to preemptively clean such residual droplet contamination and solve the routing problem, thereby minimizing the movement time for functional droplets.

3. Simultaneous Routing with Washing Droplets in MEDA biochips

3.1. Problem Description

In this section, we formulate the problem of simultaneous routing of washing droplet and target droplet on MEDA biochips. We assume that MEDA biochips is composed of $W \times H$ cells, and the coordinates of each cell are defined as (x, y) with the bottom-left corner of the biochip being $(1, 1)$. The washing droplet is set to the minimum volume of 1 to distribute the load on the electrodes. We assume a problem where the target droplet's route does not exist due to contamination from past moving droplets, as shown in Figure 1(a). These contamination cells form a continuous block from the left edge to the right edge of the biochip. The washing droplet

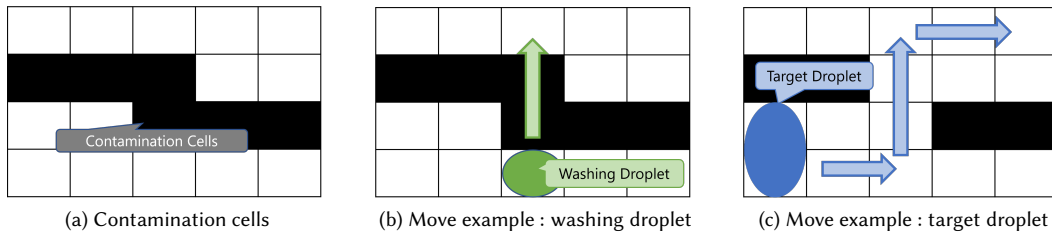


Figure 1: Contamination cells and move example

(Figure 1(b)) and target droplet (Figure 1(c)) move to each goal cells from each start cell. The target droplet move from the bottom-left to the top-right of the biochip, while the washing droplet move from the bottom edge to the top edge. The start and goal cells of the washing droplet can be set to any cell on the edges. In this condition, we realize routing problem that no mixing routes of target droplet by past moving droplet's contamination.

MEDA biochips can reshape droplet. Reshaping a droplet takes the time as same as one moving, but it provides the advantage of potentially reducing the number of cells the droplet needs to pass through, depending on the direction of movement. This paper determines the routes that minimizes the moving time of the target droplet while using the smallest washing droplet to reduce the electrode load.

3.2. Example

We consider a problem where pre-existing contaminated cells can be washed, and volume-1 washing droplet and volume-2 target droplet are routed simultaneously. The start and goal cell for the washing droplet are given. Figure 2 shows a 6×6 biochip, the contaminated cells, the start and goal cells of each droplet, and the initial shapes of the droplets.

Both the washing droplet and the target droplet move from their start cells to their goal cells. Once the washing droplet reaches its goal cell, they are discharged into a reservoir and thus are no longer present on the biochip. Since there is a possibility of interference between the washing droplet and the target droplet, a certain distance must be maintained between them during movement. Contaminated cells, indicated by black cells in Figure 2, are washed once the

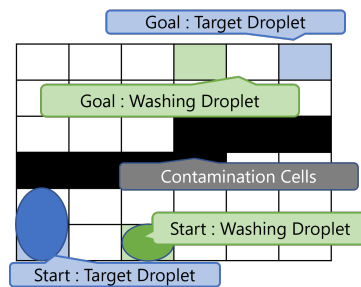


Figure 2: Initial state of MEDA Biochips

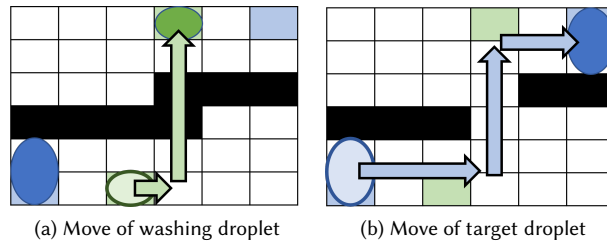


Figure 3: Step for moving droplets [21]

washing droplet pass through them and become usable from the next operation cycle.

The objective of this problem is to minimize the time it takes for both the target droplet and the washing droplet to reach their goal cells.

First, we calculate the routing time based on the existing method [21]. The existing method optimizes the route of the washing droplet and does not consider simultaneous routing with target droplet. In other words, the existing method determines the route for the target droplet only after the washing droplet have completed their washing.

As shown in Figure 3(a), the washing droplet move and require 6 steps. Then, as shown in Figure 3(b), the target droplet move, requiring 9 steps. In the existing method, the total routing steps are the sum of two droplets requiring steps both washing droplet and target droplet, resulting in a total of 15 steps.

Next, we calculate the routing time based on the proposed method in this paper. The proposed method moves the washing droplet and target droplet simultaneously. Therefore, it is necessary to avoid interference between the washing droplet and the target droplet.

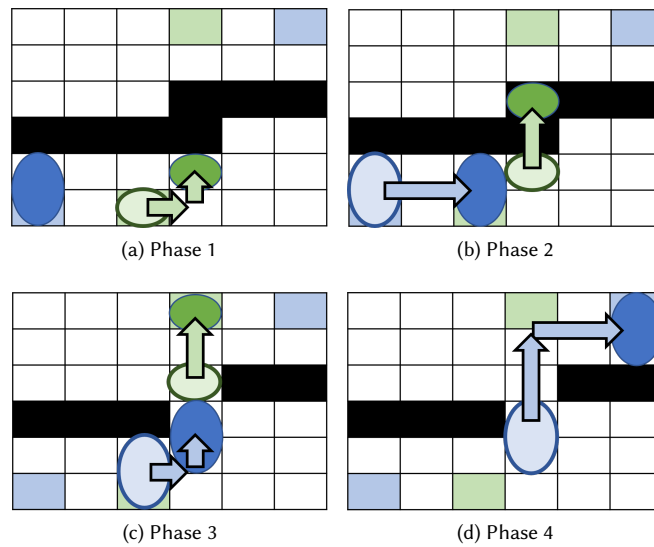


Figure 4: Routing method in proposed method

Table 1
Notations

Character	Meaning	Range
Vol	Volume of target droplet	given
$Wash.Num$	The number of washing droplets	given
Num	The number of target droplets	given
$(X.Wash.start_i, Y.Wash.start_i)$	Start cell of washing droplets i	given, $1 \leq i \leq Wash.Num$
$(X.Wash.goal_i, Y.Wash.goal_i)$	Goal cell of washing droplets i	given, $1 \leq i \leq Wash.Num$
$(X.start_i, Y.start_i)$	Start cell of target droplets i	given, $1 \leq i \leq Num$
$(X.goal_i, Y.goal_i)$	Goal cell of target droplets i	given, $1 \leq i \leq Num$
$(Contami.x, Contami.y)$	Contamination cells	given
$(x.wash_{i,s}, y.wash_{i,s})$	The reference point of washing droplet i at step s	$1 \leq x.wash_{i,s} \leq W, 1 \leq y.wash_{i,s} \leq H$
$(x_{i,s}, y_{i,s})$	The reference point of target droplet i at step s	$1 \leq x_{i,s} \leq W, 1 \leq y_{i,s} \leq H$
$(w_{i,s}, h_{i,s})$	The aspect ratio of target droplet i at step s	$1 \leq (w_{i,s}, h_{i,s}) \leq Vol$
$dir.wash_{i,s}$	The operation of washing droplet i at step s	$0 \leq dir.wash_{i,s} \leq 2$
$dir_{i,s}$	The operation of target droplet i at step s	$0 \leq dir_{i,s} \leq 4$
$time_i$	The routing time of target droplet i	$0 \leq time_i$

In Figure 4(a), the washing droplet moves for 2 steps, but the target droplet does not move to avoid interference. In Figure 4(b), the washing droplet moves upwards for 2 steps, while the target droplet moves rightwards for 2 steps. At this point, the contamination cells that the washing droplet passes through are washed, allowing the target droplet to pass through.

Subsequently, in Figure 4(c), the washing droplet moves upwards for 2 steps, and similarly, the target droplet moves for 2 steps. Once the washing droplet reaches goal cell, it is discharged into a reservoir and disappears from the biochip. Finally, in Figure 4(d), the target droplet moves to the goal position in 5 steps.

From the above, we show the example that the washing droplet requires 6 steps and the target droplet requires 11 steps. In the proposed method, the total routing steps are determined by the longer routing steps between target droplet and the washing droplet, resulting in a total of 11 steps. This shows an improvement of 4 steps compared to the existing method.

3.3. Formulation

We present the formulation of the routing problem with washing based on integer programming. Table 1 shows the character used in this formulation and their meanings.

We define the coordinates and shapes of the droplets are expressed using formulation. Let i represent the droplet number, which depends on the number of droplets, and s denote the operation step. $(x.wash_{i,s}, y.wash_{i,s})$ is defined as the reference point of washing droplet i at step s . Similarly, $(x_{i,s}, y_{i,s})$ is defined as the reference point of target droplet i at step s . The reference point is the coordinate at the bottom-left of the droplet. The shape of target droplet i at step s can be expressed as $(w_{i,s}, h_{i,s})$, where $(w_{i,s}, h_{i,s})$ represent the width and height of the droplet, respectively.

Washing droplet is always assumed to be of size 1 and exist only at the reference point to reduce the load on the electrodes. In this paper, droplets are assumed to always occupy a rectangular cells, so target droplet i occupies the cells from $(x_{i,s}, y_{i,s})$ to $(x_{i,s} + w_{i,s} - 1, y_{i,s} + h_{i,s} - 1)$.

Formula (1) shows that the target droplet reshapes while maintaining a constant volume. For example, if the volume of the droplet is 2, it can be in one of the two states: $(w_{i,s} \times h_{i,s}) = (1 \times 2)$ or (2×1) .

$$\forall i, s, \quad w_{i, s} \times h_{i, s} = Vol_i \quad (1)$$

There is no change in the formulation of the washing droplet and target droplet from Formula (2) to Formula (5). $dir.both_{i, s}$ refers to both $dir.wash_{i, s}$ and $dir_{i, s}$. $(x.both_{i, s}, y.both_{i, s})$ refer to both $(x.wash_{i, s}, y.wash_{i, s})$ and $(x_{i, s}, y_{i, s})$.

Formula (2) represents the initial positions of the washing droplet and target droplet. The coordinates at step 0 for both washing and target droplets are given.

$$\begin{aligned} \forall i, \quad & (x.both_{i, 0} = X.Both.start_i) \\ & \wedge (y.both_{i, 0} = Y.Both.start_i) \end{aligned} \quad (2)$$

Next, we formulate the operations of the droplets. We assume that droplets can move in various directions and reshape during routing. Droplets can move in horizontal (x-axis), vertical (y-axis), and diagonal directions. When $dir.both_{i, s} = 0$, the washing droplet i and the target droplet i do not move at step s . When $dir.both_{i, s} = 1$, the washing droplet i and the target droplet i move one cell horizontally at step s . When $dir.both_{i, s} = 2$, the washing droplet i and the target droplet i move one cell vertically at step s . $dir_{i, s} = 3$, the target droplet i reshapes at step s . When $dir_{i, s} = 4$, the target droplet i moves one cell diagonally at step s .

Formula (3) represents the condition where both the washing droplet i and the target droplet i do not move when $dir.both_{i, s} = 0$. This is mainly used to avoid interference between droplets.

$$\begin{aligned} \forall i, s, \quad & (dir.both_{i, s} = 0) \rightarrow \\ & (x.both_{i, s} = x.both_{i, s-1}) \wedge (y.both_{i, s} = y.both_{i, s-1}) \end{aligned} \quad (3)$$

Formula (4) represents the condition where both the washing droplet i and the target droplet i move one cell horizontally when $dir.both_{i, s} = 1$. This is mainly used to avoid interference between droplets. The reference points of the washing droplet i and the target droplet i move horizontally, but the vertical coordinates remain unchanged.

$$\begin{aligned} \forall i, s, \quad & (dir.both_{i, s} = 1) \rightarrow \\ & (x.both_{i, s-1} - 1 \leq x.both_{i, s} \leq x.both_{i, s-1} + 1) \\ & \wedge (y.both_{i, s} = y.both_{i, s-1}) \end{aligned} \quad (4)$$

Similar to Formula (4), Formula (5) shows the vertical motion of $dir.both_{i, s} = 2$:

$$\begin{aligned} \forall i, s, \quad & (dir.both_{i, s} = 2) \rightarrow \\ & (x.both_{i, s} = x.both_{i, s-1}) \\ & \wedge (y.both_{i, s-1} - 1 \leq y.both_{i, s} \leq y.both_{i, s-1} + 1) \end{aligned} \quad (5)$$

Formula (6) represents the deformation of a droplet when $dir_s = 3$. When the target droplet i is reshaped, the shape at step s is different from the one at step $s - 1$:

$$\begin{aligned} \forall i, s, \quad & (dir_{i, s} = 3) \rightarrow \\ & (w_{i, s} \neq w_{i, s-1}) \wedge (h_{i, s} \neq h_{i, s-1}) \end{aligned} \quad (6)$$

Formula (7) also shows the case of $dir_{i, s}$. Droplets have several ways of reshaping the droplet. The reference point changes depending on the way of reshaping. The expression that allows such possible shapes is given by:

$$\forall i, s, \quad (dir_{i, s} = 3) \rightarrow$$

$$\begin{aligned} & \left\{ \begin{array}{l} (x_{i,s} \leq x_{i,s-1}) \wedge (y_{i,s} \geq y_{i,s-1}) \\ \wedge (x_{i,s} + w_{i,s} \geq x_{i,s-1} + w_{i,s-1}) \\ \wedge (y_{i,s} + h_{i,s} \leq y_{i,s-1} + h_{i,s-1}) \end{array} \right\} \\ \vee & \left\{ \begin{array}{l} (x_{i,s} \geq x_{i,s-1}) \wedge (y_{i,s} \leq y_{i,s-1}) \\ \wedge (x_{i,s} + w_{i,s} \leq x_{i,s-1} + w_{i,s-1}) \\ \wedge (y_{i,s} + h_{i,s} \geq y_{i,s-1} + h_{i,s-1}) \end{array} \right\} \end{aligned} \quad (7)$$

Formula (8) represents the diagonal movement when $dir.both_s = 4$.

$$\forall i, s, \quad (dir_{i,s} = 4) \rightarrow (x_{i,s} = x_{i,s-1} \pm 1) \wedge (y_{i,s} = y_{i,s-1} \pm 1) \quad (8)$$

Formula (9) shows whether the droplet is finished routing. Formula (9) determines if at least one cell of the droplet reaches the destination cell.

$$\forall i, \quad \sum_{s=1} \left\{ \begin{array}{l} (x.both_{i,s} \geq X.goal_i) \\ \wedge (x.both_{i,s} + w_{i,s} - 1 \leq X.goal_i) \\ \wedge (y.both_{i,s} \geq Y.goal_i) \\ \wedge (y.both_{i,s} + h_{i,s} - 1 \leq Y.goal_i) \end{array} \right\} \quad (9)$$

Formula (10) represents the constraints related to unusable cells. Target droplet cannot enter contamination cells. However, target droplet can enter contamination cells after the washing droplet have passed through.

$$\begin{aligned} & \forall i, s, t, \\ & \neg \left\{ \begin{array}{l} (x.both_{i,s} \leq Contami.x) \\ \wedge (x.both_{i,s} + w_{i,s} - 1 \geq Contami.x) \\ \wedge (y.both_{i,s} \leq Contami.y) \\ \wedge (y.both_{i,s} + h_{i,s} - 1 \geq Contami.y) \end{array} \right\} \\ & \vee \left\{ \begin{array}{l} (t < s) \wedge (x_{i,s} \leq x.wash_{i,t}) \\ \wedge (x.wash_{i,t} \leq x_{i,s} + w_{i,s} - 1) \\ \wedge (y_{i,s} \leq y.wash_{i,t}) \\ \wedge (y.wash_{i,t} \leq y_{i,s} + y_{i,s} - 1) \end{array} \right\} \end{aligned} \quad (10)$$

Formula (11) defines $time_i$, which represents the number of operations for target droplet i . In this paper, the operation steps of the droplets are defined as the time required for movement, so the total number of operations corresponds to the movement time.

$$\forall i, \quad time_i = Max_s \{ (dir_{i,s} \neq 0) \times s \} \quad (11)$$

The objective function is to minimize the movement time of the target droplet.

$$Minimize : Max_i (time_i) \quad (12)$$

4. Simulations

4.1. Simulations Setup

We conduct simulations to demonstrate the effectiveness of our proposed method. We compare the proposed method with the existing method for the problem of simultaneous routing of

washing droplet and target droplet. The size of the biochip, the positions of contamination cells, the volume of the two droplets, and their respective start and goal cells are given. The objective function of this experiment is to minimize the routing time of the droplets from the start cell to the goal cell. We compare the routing time with the following two techniques:

- *Existing Method*: A method where the movement of the target droplet begins after the washing droplet have completed the washing process [21].
- *Proposed Method*: The method presented in Section 3, where washing droplet and target droplet move simultaneously.

The following conditions are given for the experiment. The size of the washing droplet is set to 1, with only one present on biochips. Similarly, the size of the target droplet is set to 2, with only one present on biochips. Simulations are conducted in two scenarios: one where there is a single sequence of contamination cells on biochips and another where there are two sequences of contamination cells. The size of MEDA biochips is assumed to be $W = 10, H = 15$. The start and goal cells of the washing droplet are randomly assigned. In the case of a single sequence of contamination cells, 20 patterns are conducted by changing the start and goal cells of the washing droplets. Similarly, 20 patterns are conducted for the case of two sequences of contamination cells.

The experiments are executed on a Ryzen Threadripper 3970X (3.7 GHz, 32 cores, 64 threads) with 256 GB of memory. We use IBM ILOG CPLEX Optimization Studio 20.1.0 to solve both the existing method and the proposed method. The computation time is limited to a maximum of 10 hours of CPU time. If the optimal solution is not obtained within the computation time, the best feasible solution found within the time limit is used for comparison.

4.2. Results

Figures 5:(a) and 5:(b) show the experimental results for cases with one and two sequences of contamination cells. The horizontal axis represents the problem number, while the vertical axis

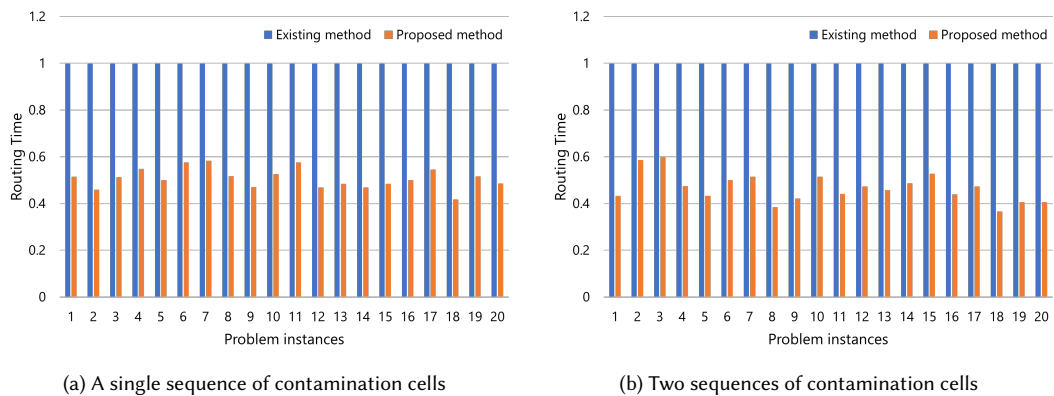


Figure 5: Simulation results

indicates the normalized routing time of the proposed method, using the routing time of the existing method as a baseline.

The proposed method successfully reduces routing time in all patterns compared to the existing method. As shown in Figure 5, the proposed method successfully reduces routing time by simultaneously moving the washing droplet and the target droplet. On average, the proposed method achieves a 55% reduction in routing time. In the results for one sequence of contamination cells shown in Figure 5:(a), an average 50% reduction in routing time is achieved. For two sequences of contamination cells shown in Figure 5:(b), an average 60% reduction in routing time is achieved. This indicates that the increase in the number of contaminated cells requiring washing cause a more widespread distribution of contamination cells. Multiple points requiring mandatory washing emerged with the increase in the number of sequences of contamination cells, extending the washing droplet routing time. However, the proposed method alleviated this problem to some extent by moving the target droplet simultaneously with the washing droplet. If there were lot unusable cells which caused by broken, proposed method would not alleviate. Therefore, setting unusable cells that the washing droplet cannot handle due to electrode failures, or setting a limit on the number of cells that can be washed per unit volume of the washing droplet, can create more realistic problems. Additionally, it is known that droplet movement speed varies depending on their shape [6]. For this problem, it is also necessary to consider speed from the perspective of interference between the target droplet and the washing droplet. Therefore, future challenges include solving these issues.

5. Conclusion

We proposed a simultaneous routing method for washing droplet and target droplet on MEDA biochips to minimize the routing time of target droplet, including the washing process. The proposed method successfully reduced the droplet routing time by an average of 55% compared to existing method. The future challenges include extending the problem to consider droplet movement speed and washing limits, and experimenting on actual biochips.

Acknowledgments

This work is partly supported by KAKENHI 20H04160 and 20H00590.

References

- [1] N. Azizipour et al., "Evolution of biochip technology: A review from lab-on-a-chip to organ-on-a-chip," *Micromachines*, vol. 11, no. 6, p. 599, 2020,
- [2] D. Barglazanb et al., "Organisation and quality monitoring for point-of-care testing (POCT) in Belgium: Proposal for an expansion of the legal framework for POCT into primary health care," *Acta Clinica Belgica*, 2021.
- [3] L. L. Gibson et al., "The RADx tech clinical studies core: A model for academic based clinical studies," *Engineering in Medicine and Biology*, vol. 2, pp. 152–157, 2021.

- [4] Z. Zhong et al., "Micro-electrode-dot-array digital microfluidic biochips: Technology, design automation, and test techniques," *IEEE Transactions on Biomedical Circuits and Systems*, vol. 13, no. 2, pp. 292–313, 2018.
- [5] T. Xu, and K. Chakrabarty, "Integrated droplet routing in the synthesis of microfluidic biochips," *Design Automation Conference*, 2007.
- [6] C. Shiro et al., "Shape-dependent velocity based droplet routing on MEDA biochips," *IEEE Access*, vol. 10, pp. 122423–122430, 2022.
- [7] Y. Zhao et al., "Cross-contamination avoidance for droplet routing in digital microfluidic biochips," *IEEE transactions on computer-aided design of integrated circuits and systems*, vol. 31, no. 6, pp. 817–830, 2012.
- [8] Z. Huang et al., "Unified contamination-aware routing method considering realistic washing capacity constraint in digital microfluidic biochips," *IEEE Access*, vol. 8, pp. 192867–102879, 2020.
- [9] H. Yao et al., "Integrated functional and washing routing optimization for cross-contamination removal in digital microfluidic biochips," *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, vol. 35, no. 8, pp. 1283–1296, 2015.
- [10] M. Cho, and D. Pan, "A high-performance droplet routing algorithm for digital microfluidic biochips," *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, vol. 27, no. 10, pp. 1714–1724, 2008.
- [11] O. Keszocze et al., "A general and exact routing methodology for digital microfluidic biochips," *International Conference on Computer-Aided Design*, 2015.
- [12] O. Keszocze et al., "Exact routing for micro-electrode-dot-array digital microfluidic biochips," *Asia and South Pacific Design Automation Conference*, 2017.
- [13] S. Chakraborty, and S. Chakraborty, "Routing performance optimization for homogeneous droplets on MEDA-based digital microfluidic biochips," *Computer Society Annual Symposium on VLSI*, 2019.
- [14] T. Liang et al., "Multitarget sample preparation using MEDA biochips," *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, vol. 39, no. 10, pp. 2682–2695, 2019.
- [15] P. Roy et al., "Harnessing the granularity of micro-electrode-dot-array architectures for optimizing droplet routing in biochips," *ACM Transactions on Design Automation of Electronic Systems*, vol. 25, no. 10, pp. 1-37, 2019.
- [16] K. Lai et al., "An intelligent digital microfluidic processor for biomedical detection," *Signal Processing Systems*, vol. 78, no. 11, pp. 85–93, 2015.

- [17] Z. Chen et al., “Droplet routing in high-level synthesis of configurable digital microfluidic biochips based on microelectrode dot array architecture,” *BioChip Journal*, vol. 5, no. 4, pp. 343–352, 2011.
- [18] G-R. Lu et al., “Flexible droplet routing in active matrix–based digital microfluidic biochips,” *ACM Transactions on Design Automation of Electronic Systems*, vol. 23, no. 3, pp. 1–25, 2018.
- [19] Z. Li et al., “Droplet size-aware high-level synthesis for micro-electrode-dot-array digital microfluidic biochips,” *IEEE Transactions on Biomedical Circuits and Systems*, vol. 11, no. 3, pp. 612–626, 2017.
- [20] P. Howladar et al., “Micro-electrode-dot array based biochips : Advantages of using different shaped CMAs,” *Computer Society Annual Symposium on VLSI*, 2019.
- [21] D. Mitra et al., “Automated path planning for washing in digital microfluidic biochips,” *Automation Science and Engineering*, pp. 115–120, 2012.