

An Accurate and Compact Hyperbolic Tangent and Sigmoid Computation Based Stochastic Logic

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Outline

- ❑ **Motivation & Background**
- ❑ **Existing Methods**
- ❑ **Stochastic Logic Implementation Based Bernstein Polynomial**
- ❑ **Proposed Architecture**
- ❑ **Experimental Results & Comparisons**
- ❑ **Conclusions**



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Motivation

Hyperbolic tangent and Sigmoid function are widely used, especially signal processing based application

- **High accuracy**
- **Reasonable hardware cost**
- **Fit to the stochastic end-to-end system**



Background

Stochastic computing

Generate a random sequence to represent a number based on fraction of the number 1's in bitstream

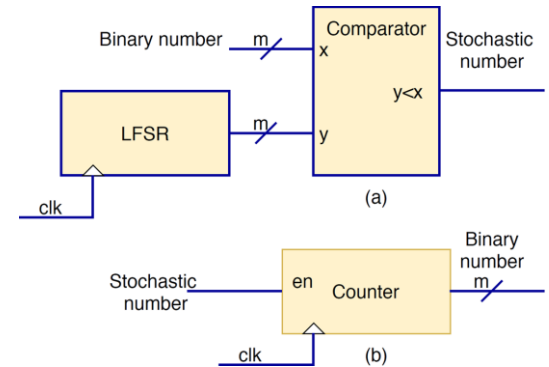
- **Unipolar format**

$$x = p(X = 1) = p(X)$$

- **Bipolar format**

$$x = p(X = 1) - 1 = 2p(X) - 1$$

Format conversion can be done the two format



(a) Stochastic number generator

(b) Converting stochastic number to binary number



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Existing Methods

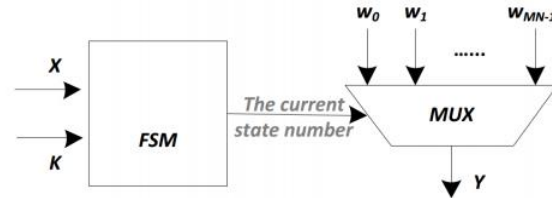
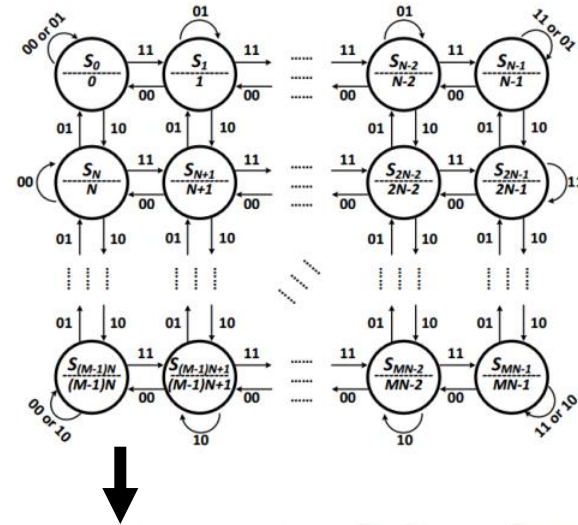
FSM based method

Pros

- Synthesize sophisticated functions

Cons

- High hardware cost
- **Low accuracy**



Existing Methods

Series expansion and JK-FFs method

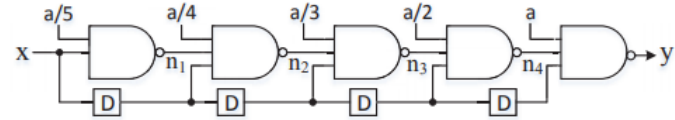
$$\tanh(ax) = \frac{e^{ax} - e^{-ax}}{e^{ax} + e^{-ax}} = \frac{1 - e^{-2ax}}{1 + e^{-2ax}}$$

Pros

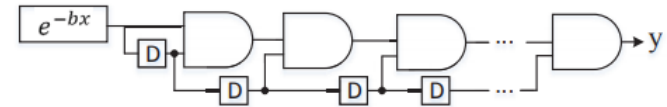
- End-to-end stochastic
- Reasonable hardware cost

Cons

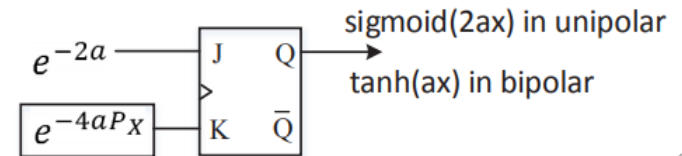
- **Low accuracy**



Stochastic implementation of e^{-ax} using Maclaurin polynomial



Stochastic implementation of e^{-ax} ($a > 1$) using e^{-bx} cascaded



Stochastic implementation of $\tanh(ax)$ and $\text{sigmoid}(2ax)$ ($a > 1$) with bipolar input using format conversion



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SC based Bernstein Polynomials

- Polynomial functions $f(x)$ are done by using multiplications and additions
- It fails to compute the polynomial functions which computation range is outside $[0, 1]$, e.g $1.2x - 1.2x^2$
- For any polynomial functions, transforming a power-form polynomial to a Bernstein polynomial:

$$B(x) = \sum_{i=0}^n b_i B_{i,n}(x)$$

Where $B_{i,n}(x) = \binom{n}{i} x^i (1-x)^{n-i}$.



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Proposed Architecture

Implementing hyperbolic tangent and sigmoid function in the bipolar format

- $\tanh(ax) = \frac{1 - e^{-2ax}}{1 + e^{-2ax}} \quad a > 0$

- $\text{sigmoid}(2ax) = \frac{1}{1 + e^{-2ax}}$

$$\Rightarrow \tanh(ax) = 2 \frac{1}{1 + e^{-2ax}} - 1$$
$$= 2\text{sigmoid}(2ax) - 1 \quad [1]$$



Proposed Architecture

Bipolar format: $x = 2P_x - 1$

- $x \in [-1, 1]$
- $P_x \in [0, 1]$

\Rightarrow Format conversion between bipolar and unipolar format

$\text{sigmoid}(2ax) \in [0, 1] \Rightarrow$ output is unipolar format

Applying format conversion to equation (1) to same

bitstream of $\text{sigmoid}(2ax) \Rightarrow \tanh(ax)$



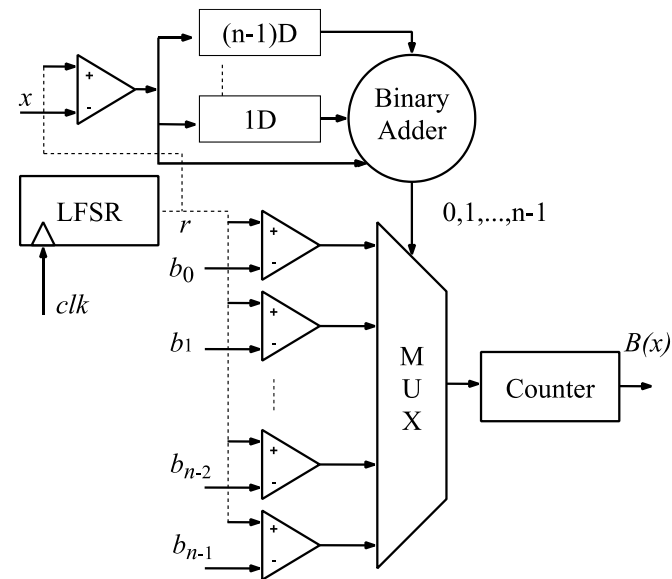
Proposed Architecture

Implementation of $\text{sigmoid}(2ax)$

- $$\text{sigmoid}(2ax) = \frac{1}{1 + e^{-2ax}}$$

$$= \frac{1}{1 + e^{-2a(2^P x - 1)}} = \frac{1}{1 + e^{-4aP_x} e^{-2a}}$$

$$= \frac{e^{-2a}}{e^{-2a} + e^{-4aP_x}}$$
- The approximation can now be made by using **Bernstein computations**.



Stochastic implementation of Sigmoid($2ax$) based Bernstein computation



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Simulations & Experiments Set-up

Design

- *Sigmoid*($2x$), *Sigmoid*($4x$), *tanh*(x), *tanh*($2x$)
- 5th order Bernstein polynomial

Simulation

- Matlab
- 10 bit LFSR
- Mean Absolute Error (MAE) results of approximated and target functions
- Monte Carlo experiments

Implementation

- Synopsys DC using TSMC 180 nm



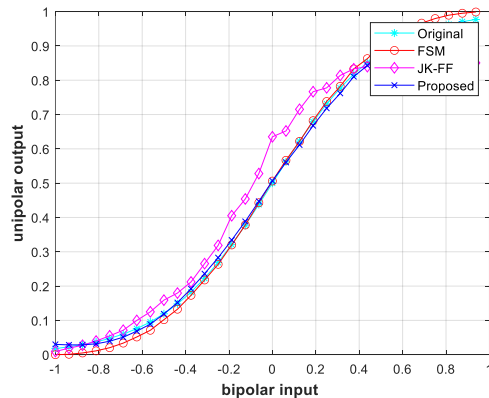
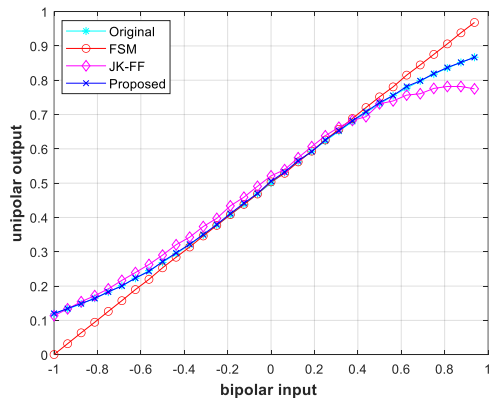
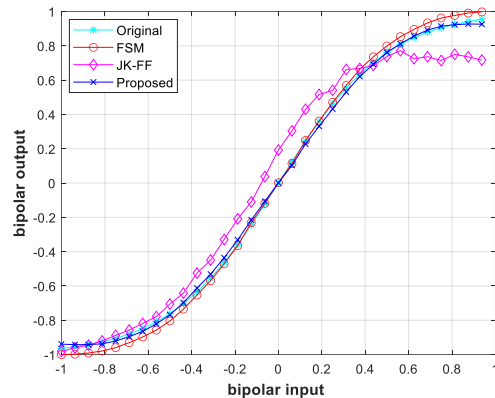
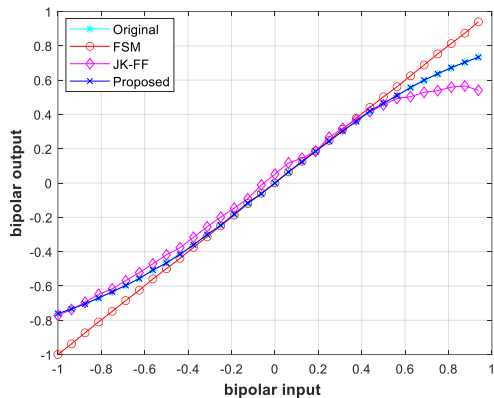
Results & Comparison

Matlab simulation results

Function	Tanh(x) and sigmoid(2x)			
Method	Proposed		FSM [4]	JK-FF [6]
	n=3	n=5	2 states	-
MAE	0.003	0.001	0.06	0.02
Function	Tanh(2x) and sigmoid(4x)			
Method	Proposed		FSM [4]	JK-FF [6]
	n=3	n=5	2 states	-
MAE	0.007	0.003	0.03	0.05



Results & Comparison



Simulation results compared different approaches with target functions: $\tanh(x)$, $\tanh(2x)$, $\text{sigmoid}(2x)$, $\text{sigmoid}(4x)$ respectively



Results & Comparison

Synopsys DC simulation results

Function	Tanh(x) and sigmoid(2x)			
	Proposed		FSM [4]	JK-FF [6]
	n=3	n=5	2 states	-
Area ($(\mu m)^2$)	1554	1777	1345	10121
Latency (ns)	2.25	2.33	2.38	3.42
Power (mW)	0.07	0.08	0.06	0.4



Results & Comparison

Synopsys DC simulation results

Function	Tanh(2x) and sigmoid(4x)			
Method	Proposed		FSM [4]	JK-FF [6]
	n=3	n=5	2 states	-
Area ($(\mu m)^2$)	1777	2106	1551	10476
Latency (ns)	2.33	3.3	3.07	3.07
Power (mW)	0.11	0.11	0.08	0.08



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Conclusions

sigmoid($2ax$) and *tanh*(ax) based **Bernstein**

polynomial in bipolar format:

- **Comparable hardware complexity**
- **Improvement of accuracy**



Reference

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THANK YOU FOR YOUR ATTENTION

