



Supplement of

Constraining the particle-scale diversity of black carbon light absorption using a unified framework

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Data from field and laboratory experiments

Cappa, et al. 2012.

- 5 The mixing state of internally mixed BC aggregates measured by Cappa *et al.* 2012 (1) was found by first fitting a power-law function to mean R_{BC} as function of photochemical age ($-\log([\text{NO}_x]/[\text{NO}_y])$), which is shown in figure 1(a). The fitted equation is given by:

$$R_{BC} = (12.215 \pm 0.396) \left(-\log \left(\frac{[\text{NO}_x]}{[\text{NO}_y]} \right) \right)^{0.554 \pm 0.067} \quad (S1)$$

- 10 Mass absorption cross-section of BC (MAC_{BC}) at wavelength (λ) of 532 nm is then calculated from figure S-17 of Cappa *et al.* 2012, which shows MAC_{BC} enhancement (E_{abs}) as a function of photochemical age. Photochemical age was converted to R_{BC} using equation S1, and E_{abs} was converted to MAC_{BC} using the reported value for MAC_{BC} of pure BC ($7.75 \text{ m}^2/\text{g}$). The morphology of particles from this study was inferred using lognormal fits of the size distributions given in figure S-13 of Cappa *et al.* 2012. The single particle BC mass was then calculated assuming BC density of $1.8 \text{ g}/\text{cm}^3$ (2).

- 15 *Saliba, et al. 2016.*

Measured MAC_{BC} as a function of BC mixing state was taken from Figure 4 of Saliba *et al.* 2016 (3). The mixing state was then converted from organic to black carbon mass ratio (OA:BC) to R_{BC} using:

20 $R_{BC} = \text{OA}:\text{BC}.$ (S2)

The morphology of particles from this study was inferred using lognormal fits of the size distributions given in figure S9 of Saliba *et al.* 2019. The single particle BC mass was then calculated assuming BC density of $1.8 \text{ g}/\text{cm}^3$ (2).

- 25 *Xie, et al. 2019.*

Measured E_{abs} as a function of R_{BC} was taken from Figure 1a of Xie *et al.* 2019 (4). enhancement was converted to MAC_{BC} using a reference MAC_{BC} value of $6.55 \text{ m}^2/\text{g}$ at $\lambda = 630 \text{ nm}$, given that the authors state that the thermodenuder-derived E_{abs} was well correlated with E_{abs} calculated using reference MAC_{BC} (4).

- 30 *Cui, et al. 2016.*

Measured E_{abs} as a function of BC mixing state was taken from Figure 5c of Cui *et al.* 2016 (5). The mixing state was converted from organic to elemental carbon ratio (OC/EC) to R_{BC} using:

35 $R_{BC} = \text{OC}/\text{EC}.$ (S3)

Absorption enhancement was converted to MAC_{BC} using MAC_{BC} of pure BC = $4.02 \text{ m}^2/\text{g}$ at $\lambda = 678 \text{ nm}$, given in figure 2 of Cui *et al.* 2016 (5).

Denjean, et al. 2020.

- 40 Measured E_{abs} as a function of BC mixing state was taken from Figure 2 of Denjean *et al.* 2020 (6). Absorption enhancement was converted to MAC_{BC} using MAC_{BC} of pure BC = $7.7 \text{ m}^2/\text{g}$ at $\lambda = 550 \text{ nm}$. The morphology of particles from this study was inferred using lognormal fits of the size distributions given in figure 1 of Denjean *et al.* 2020. The average mass was then calculated assuming BC density of $1.8 \text{ g}/\text{cm}^3$ (2).

Zanatta, et al. 2018.

- 45 Average MAC_{BC} and R_{BC} were found using reported values for average coating thickness, coating density, and MAC_{BC} in Zanatta *et al.* 2018 (7). The morphology of particles from this study was inferred using reported size distributions given in Table 2 of Zanatta *et al.* 2018. The single particle BC mass was then calculated assuming BC density of $1.8 \text{ g}/\text{cm}^3$ (2).

Liu, et al. 2015.

- 50 Measured MAC_{BC} as a function of BC mixing state was taken from Figure S2 of Liu *et al.* 2015 (8). We utilize MAC_{BC} derived using standardized major axis at $\lambda = 781 \text{ nm}$ in order to avoid potential influence of absorbing coatings on MAC_{BC} . The morphology of particles from this study was inferred using the limits of BC diameter given in Figure 1d of Liu *et al.* 2015. The single particle BC mass was then calculated assuming BC density of $1.8 \text{ g}/\text{cm}^3$ (2).

- 55 *Cappa, et al. 2019.*

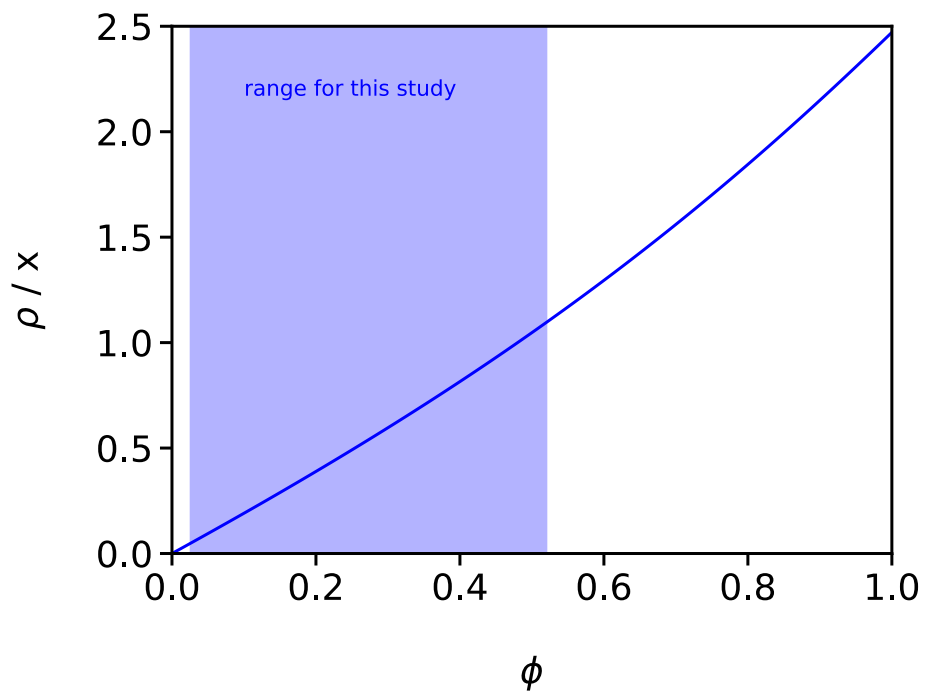
Measured MAC_{BC} as a function of BC mixing state was taken from Figure S4 and S6 of Cappa *et al.* 2019 (9). We analyze measurements of MAC_{BC} at $\lambda = 532 \text{ nm}$ only.

Shiraiwa, et al. 2010.

- 60 Measured E_{abs} as a function of BC mixing state was taken from Figure 2 of Shiraiwa *et al.* 2010 (10). The mixing state was converted from the ratio of total particle diameter to black carbon diameter using BC density of 1.8 g/cm^3 and coating density of 1.2 g/cm^3 (2). The morphology of particles from this study was inferred using reported BC core diameter.

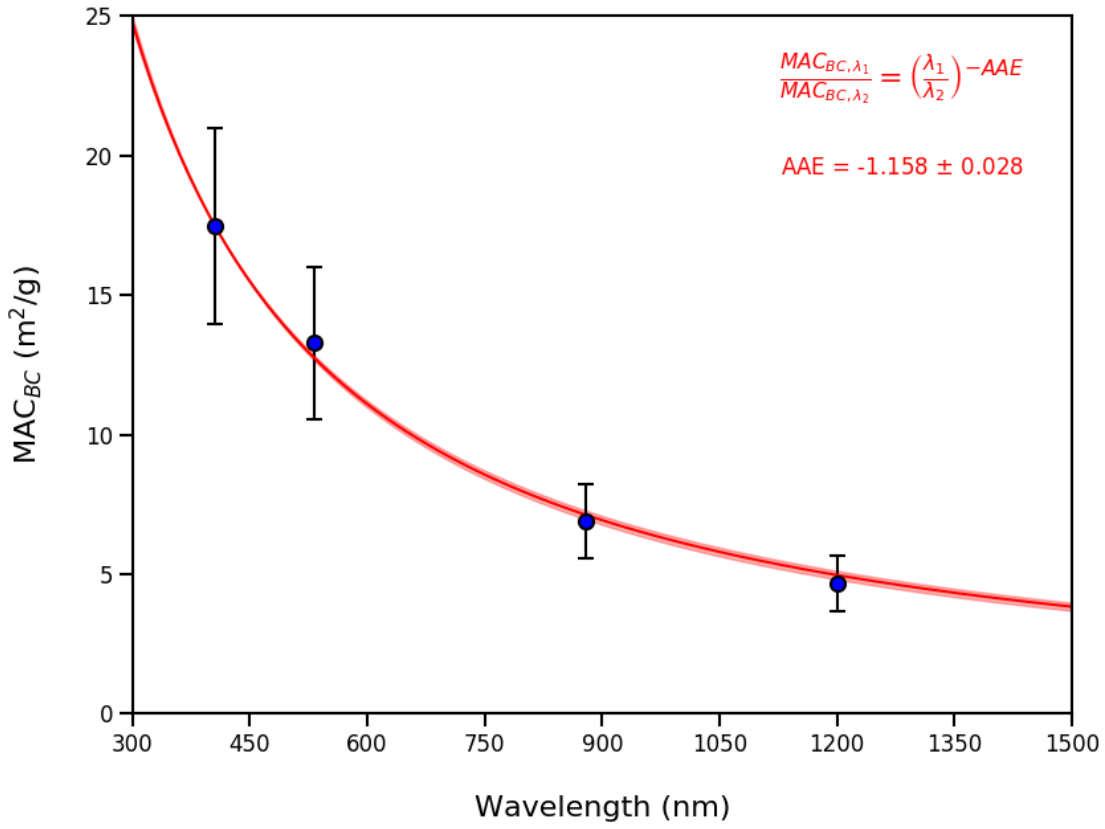
Zhang, et al. 2018.

- 65 Measured E_{abs} as a function of BC mixing state was taken from Figure S3 of Zhang *et al.* 2018 (11). The mixing state was converted from organic to elemental carbon mass ratio to R_{BC} using equation S3. Absorption enhancement was converted to MAC_{BC} using MAC_{BC} of pure BC = $4.7 \text{ m}^2/\text{g}$ at $\lambda = 880 \text{ nm}$. The morphology of particles from this study was inferred using the reported range of BC core diameters (100-150 nm).



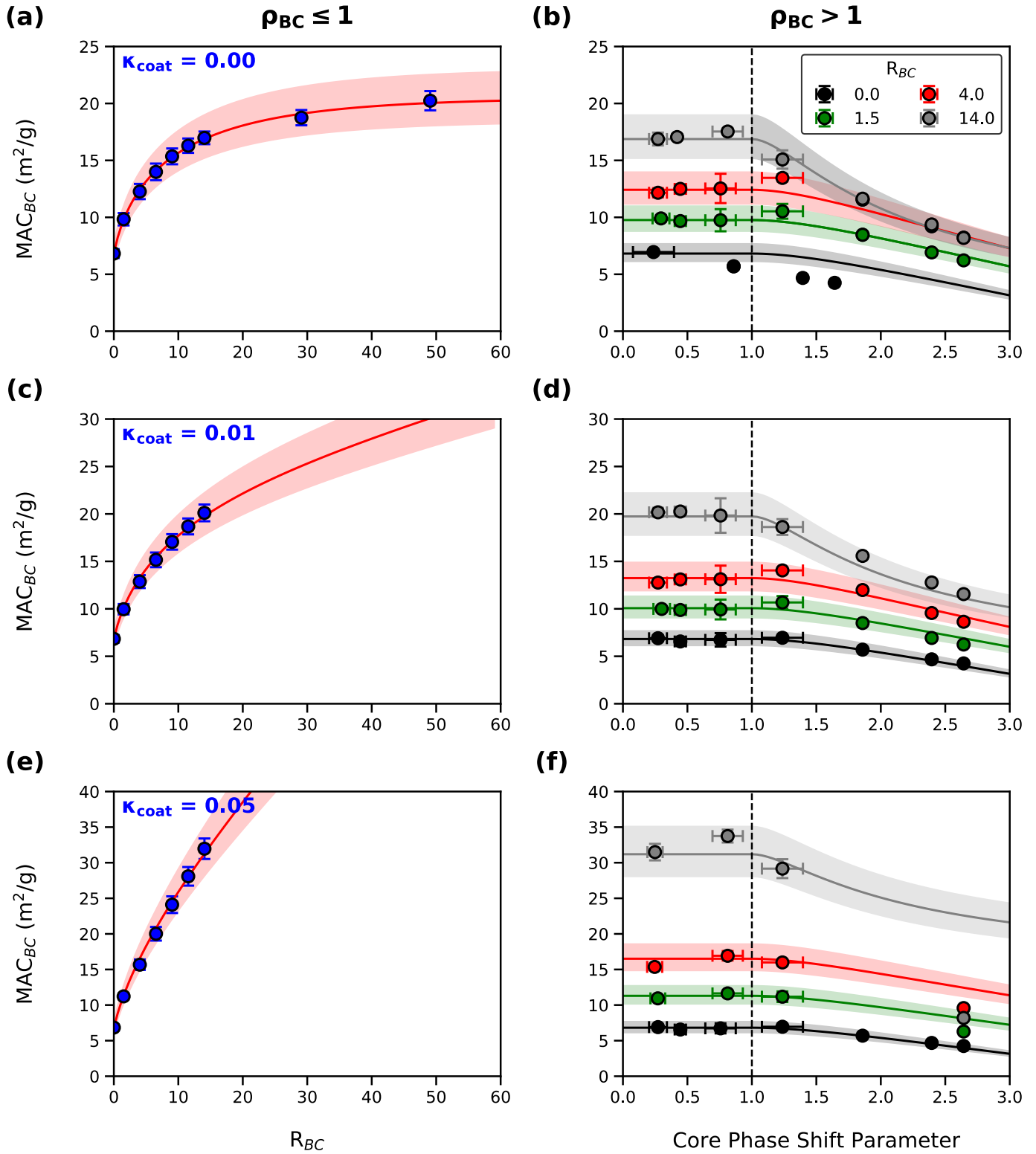
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Figure S1: Size parameter normalized phase shift parameter of black carbon as a function of monomer packing fraction. The shaded area represents the range of monomer packing fraction for aggregates in this study.



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Figure S2: Data used to calculate AAE for fractal BC aggregates with $\rho_{BC} \leq 1$, error bars show one standard deviation. Solid line shows fitted equation given in figure, error of AAE is reflective of 95% confidence interval.



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Figure S3: MAC_{BC} as a function of R_{BC} and ρ_{BC} with shaded areas representing the range of MAC_{BC} assuming BC density of 1.6 g/cm³ – 1.8 g/cm³.