



1 **Assimilation of L-band InSAR snow depth retrievals for**
2 **improved snowpack quantification**

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46 **Abstract**

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48 The integration of snow hydrology models and remote sensing observations via
49 data assimilation is a promising method to capture the dynamics of seasonal
50 snowpacks at high spatial resolution and reduce uncertainty with respect to snow water
51 resources. In this study, we employ a modified interferometric Synthetic Aperture
52 Radar (InSAR) technique to quantify snow depth change using modeled snow density
53 and assimilate the referenced and calibrated retrievals into a multilayer snow hydrology
54 model (MSHM). Although the impact of assimilating snow depth change is local in
55 space and time, the impact on snowpack mass properties (snow depth or SWE) is
56 cumulative, and the InSAR retrievals are valuable to improve snowpack simulation and
57 capture the spatial and temporal variability of snow depth or SWE. Details in the
58 estimation algorithm of InSAR snow depth or SWE changes, referencing and
59 calibration prove to be important to minimize errors during data assimilation.

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61 **1 Introduction**

62 Remote sensing and distributed modelling of snowpack with data assimilation is
63 a promising methodology to quantify snow water resources (including condition) and
64 reduce uncertainty. Current and upcoming snow remote sensing using Synthetic
65 Aperture Radar (SAR) aim to provide global coverage at hyper-resolution, which is
66 needed to quantify snow variability with reduced uncertainty. Recent studies have
67 either mostly used backscatter approaches (Lievens et al., 2019, 2022; Singh et al.,
68 2024; Tsang et al., 2021) or interferometric SAR (InSAR) techniques (Guneriussen et
69 al., 2001) to quantify snow depth and snow water equivalent (SWE). The latter have
70 been applied extensively for SWE retrievals from dry snowpacks using ground-based
71 (e.g. Leinss et al., 2015; Ruiz et al., 2022) and satellite-based SARs (e.g. Conde et al.,
72 2019; Dagurov et al., 2020; Deeb et al., 2011; Guneriussen et al., 2001; Lei et al., 2023;
73 H. Li et al., 2016; S. Li & Sturm, 2002; Liu et al., 2017). The InSAR technique assumes
74 that the volume backscatter and absorption of microwave signal in the snowpack are
75 negligible with the backscatter at the ground-snowpack interface being dominant while
76 refraction results in phase delay. Previous studies have shown also that the InSAR
77 retrievals are more suitable at longer wavelengths (e.g., L-band), owing to
78 transparency of dry snow, preservation of coherence for longer periods of time and
79 larger threshold for phase wrapping. With the upcoming NASA-ISRO (Indian Space
80 Research Organization) SAR (NISAR) mission, multiple studies with airborne L-band
81 UAVSAR (Uninhabited Aerial Vehicle Synthetic Aperture Radar) data have already
82 demonstrated the potential of InSAR for snow remote sensing (e.g. Bonnell et al., 2024;
83 Deeb et al., 2021; Hoppinen et al., 2023; Idowu and Marshall, 2022; Marshall et al.,
84 2021; Palomaki and Sproles, 2023; Tarricone et al., 2022).

85 InSAR retrieval algorithms need spatial data of snow density and referencing to



86 estimate the spatial variability in absolute snow depth or snow water equivalent (SWE).
87 Leinss et al. (2015) have proposed a modified InSAR technique to circumnavigate the
88 need of snow density in SWE retrievals by introducing an additional parameter with
89 very small variability for a range of incidence angles and snow density, their approach
90 also assumes that the vertical profile of snow density does not change between the
91 two dates for each InSAR pair. However, the density profiles can change depending
92 on the time interval between revisits, new snowfall events, and weather conditions that
93 may impact the top layer of the snowpack. Furthermore, snow density might still be
94 needed in referencing the retrievals to obtain absolute snow depth or SWE for
95 assimilation purposes. Hyper-resolution snow hydrology models driven by realistic
96 hydrometeorological forcing can potentially provide a good estimate of snow density
97 for the InSAR algorithm, and in turn the assimilation of InSAR retrievals can potentially
98 improve the modeled snowpack states. Earlier studies have already shown the
99 potential of assimilating retrieval of snow depth or SWE from airborne or satellite SAR
100 to improve modeled snowpack and reduce uncertainty (e.g. Giroto et al., 2024; Pflug
101 et al., 2024; Shrestha and Barros, 2024). The upcoming launch of the NASA-ISRO SAR
102 (NISAR) mission that will provide L-band measurements globally provides impetus to
103 investigate the assimilation of InSAR retrievals and associated uncertainty
104 quantification with potential application to operational water prediction. Here, we
105 leverage the multiple in-situ and airborne snow measurements available from NASA's
106 SnowEx'20 (Marshall et al., 2019) campaign over Grand Mesa to 1) evaluate L-band
107 InSAR retrievals of snow depth, and 2) assimilate the retrievals into a distributed snow
108 hydrology model to evaluate the impact on the simulated macro-physical snow
109 properties and their uncertainties. We evaluate the L-band InSAR retrievals at their
110 native resolution over different snow depths and land covers against ground-based
111 measurements and airborne Lidar (Light Detection and Ranging) retrievals. The InSAR



112 retrievals with the common first flight date with available observed spatial snow depth
113 measurements were used for assimilation at different time windows and the other
114 retrievals were used to evaluate the ensemble snow hydrology model prediction of
115 snow properties and to characterize the impact of assimilating the InSAR retrievals of
116 snow depth.

117 **2 Methods**

118 **2.1 Study Area**

119 The study area is located over the western part of Grand Mesa plateau, Colorado,
120 USA (GM domain; Fig. 1). The land cover is dominated by grassland and mixed forests
121 across the plateau with elevations ranging from 3000 to 3200 m. There are several
122 scattered open water bodies (e.g., lakes and reservoirs), as well as areas with shrubs
123 and wetlands. During the SnowEx'20 campaign, Grand Mesa was used to host an
124 Intensive Observation Period (IOP) during the snow-on season, including bi-weekly
125 UAVSAR flights and airborne Lidar data collections.

126 **2.2 Data**

127 **2.2.1 UAVSAR**

128 UAVSAR is a fully polarimetric L-band synthetic aperture radar designed to obtain
129 high quality airborne repeat pass interferometry (Hensley et al., 2008; Rosen et al.,
130 2006). The radar operates at a frequency of 1.26 GHz ($\lambda = 0.2379$ m) with a bandwidth
131 of 80 MHz, and is mounted on the NASA NASA Gulfstream III, flying at a nominal
132 altitude of 13800 m. UAVSAR data are available from the ASF-DAAC for multiple
133 campaigns (https://api.daac.asf.alaska.edu/services/utills/mission_list). The
134 `uavsar_pytools` (https://github.com/SnowEx/uavsar_pytools) was used to download



135 and convert InSAR georeferenced binary grid files to geotiffs in WGS84 for Grand
136 Mesa (SnowEx'20). The interferometric data consists of the interferogram, coherence,
137 unwrapped phase in quad polarizations, including the digital elevation and incidence
138 angles along the flight path. In some cases, all polarizations were not available. There
139 were 7 InSAR pairs available based on 5 UAVSAR flights for repeated flight paths at a
140 heading of 274° (Table 1). The interval between the InSAR pairs varied between 7 to
141 40 days (e.g. track 3-5 (11d), 3-8 (18d), 3-13 (25d),3-17 (40d),5-8 (7d),8-13 (7d) and
142 13-17 (15d)).

143 **2.2.2 Snow Pit and Snow Pole Measurements**

144 The snow pit data include measurements of snow temperature, snow depth, snow
145 density, snow stratigraphy, snow grain size, liquid water content, and snow water
146 equivalent over Grand Mesa. The SNEX20_GM_SP collection (Vuyovich et al., 2021)
147 has 154 snow pit measurements between 27 January and 12 February 2020. Similarly,
148 the SNEX20_TS_SP collection(Mason et al., 2024) has time-series of snow pit
149 measurements between October 2019 and May 2020, obtained by the SnowEx
150 community during the 2020 campaign.

151 The snow pole data (SNEX20_SD_TLI) consists of snow depth measurements
152 based on time-lapse imagery by capturing a snow pole in each imagery(Breen et al.,
153 2022). The temporal coverage for these data is from 29 September 2019 through 10
154 June 2020. The cameras took either three images daily (11AM, 12 PM, 1PM) or twice
155 daily (11AM and 12PM). The cameras were placed in the Grand Mesa based on a
156 combination of tree-density map (treeless, sparse and dense) and reference snow
157 depths from Airborne Snow Observatory (ASO) Lidar retrievals on 8 Feb 2017 (shallow,
158 intermediate and deep). The error estimates for each camera vary and range from ± 2
159 to ± 16 cm.



160 **2.2.3 ASO**

161 The Airborne Snow Observatory(ASO; Painter et al., 2016) Lidar derived snow
162 depths at 3 m and 50 m resolution for Grand Mesa were available for Feb 1/2 (fused
163 together) and Feb 13 during the SnowEx'20 campaign. The snow depths over forested
164 area represent snow depths at the ground. SWE estimates were also available from
165 ASO at 50 m resolution, based on bias corrected snow density using a snow hydrology
166 model at 50 m resolution. The reported uncertainty in the data was 5.8 cm and 1.7 cm
167 at 3 m resolution for the two dates, and less than 1 cm at 50 m resolution for both
168 dates. In the ASO retrievals for SWE, the snow density was obtained by calibrating the
169 modelled density with ground-based observations.

170 **2.2.4 Atmospheric data**

171 The High-Resolution Rapid Refresh (HRRR;Dowell et al., 2022) 3 km first hour
172 forecast data for water year 2020, was downloaded using a python package
173 (<https://doi.org/10.5281/zenodo.4567540>). The HRRR ensemble consists of 36
174 members for DA and 9 members for forecast run but were not available in the servers
175 except the single forecast. This HRRR data were used both to estimate atmospheric
176 correction of InSAR phase and as offline atmospheric forcing for the snow hydrology
177 model. The HRRR grids interpolated to regular geographic grids are also outlined in
178 the GM domain (Fig. 1).

179 **2.3 InSAR snow depth retrieval**

180 The total interferometric phase difference obtained with repeat pass SAR data
181 over a snow-covered region includes contributions due to phase impacts from flat
182 Earth, local topography, atmospheric delay, snowpack, and random and systematic
183 errors. While the random error mostly comes from the temporal decorrelation,



184 assuming that phase impacts from flat Earth, local topography and systematic errors
185 are accounted for in the UAVSAR InSAR processing chain, the extraction of the phase
186 contribution only requires accurate estimation of phase contribution due to atmospheric
187 delay (see Appendix A1). With known InSAR phase difference ($\Delta\phi_s$) due to the
188 presence of snowpack, the change in snow depth (Δz_s) can be estimated following
189 Guneriusson et al. (2001) for coherent reflections:

$$190 \quad \Delta z_s = - \left(\frac{\lambda}{4\pi} \right) \frac{\Delta\phi_s}{(\cos\theta_i - \sqrt{\varepsilon - \sin^2\theta_i})} \quad (1)$$

191 where λ is the SAR wavelength, θ_i is the incidence angle and ε is the bulk
192 snowpack permittivity. For dry snow, ε'' is negligible compared to ε' and the relationship
193 between snow density ρ_s [kgm^{-3}] and permittivity can be expressed according to
194 Matzler, (1996) and Wiesmann and Mätzler (1999) as follows:

$$195 \quad \varepsilon = 1 + 1.6 * 10^{-3} \rho_s + 1.8 * 10^{-9} \rho_s^3 \quad (2)$$

196 Interferometric coherence is important to assess the uncertainty in the retrievals
197 of snow depth, as the retrieval errors increase with decreases in coherence. Ruiz et al.
198 (2022) used a ground based 1-10 GHz SAR system with InSAR capabilities to examine
199 the environmental impact on the observed coherence for snow covered surface. For
200 example, increases in air temperature leading to snow melt are associated with large
201 drops in snow coherence, besides wind, precipitation and large changes in
202 temperature gradients. Compared to X, C and S-band, L-band measurements exhibit
203 higher coherence over longer temporal baselines, and lower error in SWE retrieval,
204 indicating better suitability for InSAR applications.

205 The estimation of Δz_s following Eq. (1) assumes that the density of the snowpack
206 is uniform with depth and that the underlying profile does not change with time. The
207 latter assumption is problematic as the snow density of the underlying profile could
208 change due to physical processes (e.g. compaction) depending on the temporal



209 baseline of the repeat pass and fresh snow. Besides, natural snowpacks are
210 characterized by multi-layer vertical stratigraphy with varying snow density and the
211 phase delay is an integral of the phase delay over the multiple layers (Liens et al.
212 2015). Using $\Delta SWE = \sum_{j=1}^N \Delta z_{s,j} \rho_{s,j} / \rho_w$, where ρ_w is the density of water, and $i=1, N$
213 are the multiple layers, Liens et al. (2015) proposed a linear relationship between
214 InSAR phase change and SWE change as follows:

215

$$216 \quad \Delta SWE = -\Delta \phi_s \left(\frac{\lambda}{2\pi\alpha} \right) \left(1.59 + \theta_i^{\frac{5}{2}} \right)^{-1} \quad 3$$

217 where α is an optimal correction factor ranging from 0.92 – 1.07 for a wide range
218 of incidence angles (up to 65°) and snow densities (up to 900 kgm⁻³). With this
219 formulation and using an optimal α , they estimated a maximum error of 10%. To reduce
220 the uncertainty in snow density, the above method could be directly used to estimate
221 changes in SWE. However, errors due to variations in density profile tied to the
222 temporal baseline between the repeat passes remain to be addressed.

223 Since we evaluate the model results with snow depth measurements from the
224 lidar and ground-based measurements, we employ Eq. 1 for the estimation of snow
225 depth change in this study. Using the atmospherically corrected unwrapped phase
226 images from the UAVSAR data, the snow depth was retrieved over the GM domain in
227 the native grid resolution (approx. 5 m) using average bulk snow density between two
228 repeat pass dates from MSHM reference runs. Note that the estimated change in snow
229 depth is also well below the limit for possible phase wrapping effect in L-band, which
230 is around 69 cm for $\lambda = 23.6 \text{ cm}$ and $\theta_i = 23^\circ$ (Deeb et al., 2011). Here, it is also
231 important to note that the estimated change in snow depth is a relative change, and
232 without a snow-free scene or known point change in snow depth, it's not possible to
233 relate the relative change in snow depth to absolute snow depth change. Previous



234 studies (e.g. Bonnell et al., 2024; Conde et al., 2019; Hoppinen et al., 2023; Palomaki
235 and Sproles, 2023; Tarricone et al., 2022) have used different methods (e.g. finding
236 pixels with no changes or using pixels with known changes) to calibrate the InSAR
237 retrievals to obtain absolute change in snow depth or SWE. In this study we use the
238 snow pole measurements over grasslands for the calibration. For cases, where the
239 measurements cannot be collocated due to missing retrievals, we use the snow pole
240 measurement over the sparsely forested areas. In addition, we use an average over a
241 3x3 square box in the UAVSAR scene to reduce any uncertainty due to GPS location
242 of snow pole measurements.

243 **2.4 MPDAF and Experiment Setup**

244 The Multi-Physics Data Assimilation Platform (MPDAFv1.0; Shrestha and Barros,
245 2024) employs a coupled framework of Multilayer Snow Hydrology Model (MSHMv3.0;
246 Cao and Barros, 2020; Kang and Barros, 2011b, 2011a; Shrestha and Barros, 2024)
247 and the NCAR Data Assimilation Research Testbed (DART; Anderson et al., 2009;
248 DART, 2023). MSHM is a distributed 1D-column model, that solves the mass and
249 energy budgets of the snowpack. Key physical processes of snow hydrology -
250 snow/rain partitioning, snow accumulation, compaction, melting, melt-runoff including
251 snow microstructure evolution are well represented in the model to simulate the
252 macroscopic and microscopic snow properties. More details about the
253 parameterizations can be inferred from the studies mentioned above. Following Cao &
254 Barros (2020), the snow albedo is provided externally using the NLDAS Mosaic Land
255 Surface Model L4 v2.0 albedo data (Xia et al., 2012a; Xia et al., 2012b).

256 In DART, we use the Ensemble Adjustment Kalman Filter (EAKF; Anderson, 2003)
257 with enhanced spatially varying state space inflation (Anderson, 2009; El Gharamti,
258 2018). Assimilation is carried out with observed integrated quantities like total SWE or



259 total snow depth, and the increments are then distributed vertically to the model states
260 (snow depth, snow density and SWE) using a repartition algorithm(Shrestha & Barros,
261 2024). Besides, the cutoff radius that determines the region of spatial impact of the
262 assimilated variable was set at approximately 100 m (close to the model resolution).

263 The snow hydrology model is setup over the GM domain using approximately 90
264 m resolution with 66×165 grid points. The maximum number of snow layers in the
265 model was set to 30. The merged atmospheric forcing data are also interpolated to
266 regular geographic grid and disaggregated to 90 m resolution. Here, no downscaling
267 algorithms are applied to the forcing data and the disaggregation technique applies
268 homogeneous forcing over the subgrid pixels – this also allows us to highlight the
269 impact of hyper-resolution data assimilation.

270 The MSHM reference run (CTRL) was integrated from Oct 1, 2019, to Apr 1, 2020
271 using the default HRRR forcing data. For data assimilation (DA) runs, 48 ensemble
272 members were generated by perturbing the model forcing data. The precipitation is
273 perturbed using multiplicative noise drawn from a uniform distribution $U[-0.4, 0.4]$. The
274 incoming shortwave and longwave are also perturbed using a multiplicative noise from
275 a uniform distribution $U[-0.05, 0.05]$ and $U[-0.1, 0.1]$ respectively.

276 Figure 2 synthesizes the availability of ASO Lidar retrievals and L-band InSAR
277 retrievals for assimilation and evaluation of model runs. Here, we use part of the data
278 for assimilation and the remainder are used for evaluation. As stated earlier, the L-band
279 InSAR retrievals only provide information about relative changes in snow depth or
280 SWE, which need to be referenced and calibrated to obtain absolute values needed
281 for assimilation. In the context of distributed modelling at a given resolution, this would
282 require a spatial map of snow depth or SWE for referencing. In this study, we use the
283 ASO Lidar snow depth data at 50 m resolution (Feb 1) as a reference and combine
284 them with aggregated InSAR retrievals of snow depth change I1 (Feb 1-12) , I2 (Feb



285 1-19) and I3 (Feb 1-26) at 50 m resolution to obtain the absolute snow depth pattern
286 over the GM domain on Feb 12, 19 and 26 respectively. Two DA experiments are
287 conducted by assimilating total snow depth: 1) ASO Lidar retrieval on Feb 1, and 2)
288 ASO Lidar retrieval on Feb 1 and referenced InSAR retrievals on Feb 12,19 and 26.
289 We reference the InSAR retrievals by aggregating the data to 50 m resolution grid of
290 the ASO Lidar retrievals from Feb 1, which matches the date of the first InSAR pair in
291 both cases. InSAR retrievals of snow depth change on I5 (Feb 12-19), I6 (Feb 19-26)
292 and I7 (Feb 26-Mar12) are reserved for independent evaluation. In both DA
293 experiments, we assign an observational error of 10 % for the snow depth retrievals at
294 50 m resolution, that is consistent with the errors from the InSAR retrievals using the
295 UAVSAR data in this study.

296 **3 Results**

297 **3.1 Meteorological Settings**

298 The meteorological conditions based on the HRRR forcing data including air
299 temperature, precipitation and wind speed were analysed for the GM domain (2*5
300 HRRR grids at 3 km resolution). These environmental forcings along with temporal
301 baselines are also the source of variability in interferometric coherence and errors in
302 the retrievals. Figure 3 shows the time-series of air temperature, wind speed and
303 precipitation intensity for the month of February including the first two weeks in March
304 for the NW corner of the GM domain. The month of February was generally cold and
305 windy with temperatures dropping below -20 °C, and wind speeds reaching up to 15
306 m/s. The time-series show cooling and warming periods at a weekly time scale, with
307 some days where the air temperature reached above zero. However, the amplitude of
308 cooling decreases gradually from the end of February to mid-March with more frequent



309 warm periods. There were a few snowfall events between Feb 1-12, Feb 19-26 and
310 Feb 26-Mar 12, which varied in intensity along the GM domain.

311 **3.2 Snow Density**

312 A spatial pattern of bulk snow density is required to compute the snowpack
313 permittivity needed for the InSAR retrieval technique. Uncertainty in snow density
314 estimates can lead to errors in snow depth retrieval. Figure 4 shows the snow density
315 distribution for the InSAR pair (Feb 1-12) using the 50 m resolution ASO Lidar data,
316 snow pit data and model estimates using a reference run (CTRL) for the GM domain.
317 Only the snow pit data within GM domain collected within ± 1 day of the InSAR flights
318 were used for analysis. All three data sets show compaction of snow between the two
319 dates, but the model simulates slightly higher snow density for both flight dates and
320 underestimates the spatial variance as observed in the snow pit data and ASO Lidar
321 data as expected given the coarse resolution of the HRRR precipitation forcing (i.e.
322 3km). Note that the snow density in ASO Lidar data is also from a model estimate but
323 it was bias corrected (i.e., locally calibrated) using the snow pit data from SnowEX'20
324 campaign. In the 11-day temporal baseline, the average snow density changes by
325 5.6 %, 11 % and 4 % respectively among the lidar, snow pit and model data.

326 To examine the error in snow depth retrieval associated with error in density, we
327 used Eq. 1 to retrieve snow depth change for a fixed phase change due to snow. Figure
328 4d shows the variability in InSAR retrieval of snow depth change as a function of
329 incidence angle, for a phase change of -0.17π using the average snow density from
330 ASO Lidar, snow pit and the MSHM CTRL run. The error generally decreases with
331 increasing incidence angle. The synthetic simulation shows that a 10 % error in snow
332 density can lead to approximately 10 % error in snow depth estimates at lower
333 incidence angles, everything else being the same.



334 **3.3 L-band retrieval of snow depth**

335 The temporal baselines for the L-band retrieval range from 7 to 40 days, and the
336 interferometric coherence generally decreased with increasing temporal base lines as
337 expected. For treeless and forested areas, the mean coherence for 7-day temporal
338 baseline (Feb 12-19) was 0.7 ± 0.15 and 0.65 ± 0.18 respectively. Similarly, for the Feb
339 19-26 pair, it was 0.6 ± 0.18 to and 0.5 ± 0.2 respectively. The coherence decreased to
340 0.39 ± 0.16 and 0.36 ± 0.17 for the 40-day temporal baseline. These values are for the
341 HH polarization, as it was available for all dates. The lower coherence for the Feb 19-
342 26 pair compared to Feb 12-19 pair could be attributed to environmental factors, e.g.,
343 larger wind speeds, precipitation event, and intermittent warming (see Fig. 3). The
344 forested area exhibits lower coherence than the treeless area suggesting possible
345 higher uncertainty in the retrievals. The above statistics are based on the NLCD
346 landcover data at 30 m resolution, whereas the native resolution of InSAR retrievals
347 from UAVSAR is in the order of 5 m resolution, and the retrievals over forest contain
348 information from snow depth in tree clearings as well.

349 **3.3.1 Evaluation with ASO Lidar data**

350 The InSAR pair of Feb 1-12 with a temporal baseline of 11 days provides the
351 closest concurrent pair with the ASO Lidar retrieval based on Feb1/2 and Feb 13 to
352 compare the snow depth difference at a scale of 3-5 m resolution. Figures 5a-b show
353 the spatial pattern of interferometric coherence and snow depth change at VV
354 polarization. Figure 5c shows the change in snow depth based on ASO Lidar data for
355 the same region. The western part of this GM subdomain is mostly dominated by snow
356 cover over grasslands, while the eastern part contains snow cover in forested areas
357 with relatively lower coherence. Both the Lidar and L-band retrieval capture the wavy
358 roll like pattern due to scouring and drifting of snow over the grasslands shown earlier



359 by Marshall et al. (2021) for a smaller area. Over the eastern part of the subdomain,
360 which is dominated by forest, there are significant discrepancies: in regions with no
361 snow depth change in the ASO Lidar data, a decrease in snow depth is observed in
362 the L-band retrieval.

363 The average coherence values for this subdomain were 0.51, 0.46, 0.39 and 0.39
364 for VV, HH, HV and VH polarization respectively. Also, the missing retrievals in the
365 radar scene were 8, 11, 36 and 54 % of the area respectively for the different
366 polarizations. The distribution of snow depth change for co-polarization better matches
367 with the ASO Lidar data compared to cross-polarization (Fig. 5d). The average
368 changes in snow depth for the scene were -2.42, -1.13 and -0.1 cm respectively for
369 ASO Lidar and InSAR VV and HH polarizations. The HV and VH polarization show
370 rightward and leftward shifted peaks respectively.

371 While the results were similar for other subdomains (not presented here), the L-
372 band retrievals were found to show a general decrease in snow depth in the western
373 most part of GM domain dominated by forest cover, while the Lidar data shows a
374 contrasting increase in snow depth. Thus, the retrievals show higher uncertainty over
375 the forest areas and further evaluation is needed.

376 **3.3.2 Evaluation with snow pole and snow pit time-series data**

377 The snow pole data provide a time-series of snow depth measurements for
378 locations which are treeless or have sparse/dense trees and can be used for
379 comparison with all available InSAR pairs over the GM domain. We use the linearly
380 interpolated snow pole data in time to reference the InSAR retrievals in HH polarization
381 and obtain absolute snow depth for comparison. Figure 6 shows the evaluation of
382 referenced InSAR retrievals with snow pole data for treeless landcover: a-c), sparse
383 trees : d-f), and dense trees : g-m). In most cases, the L-band InSAR retrievals capture



384 the trend in snow depth change very well for different landcover types. The root mean
385 square errors (RMSE) were similar for different landcovers with approximate values of
386 4-6 cm. We also explored the errors in terms of InSAR pairs. The RMSEs of InSAR
387 estimates were 5.0, 4.9, 4.4, 6.2, 7.3 and 4.2 cm respectively for Feb 1-12 (11d), Feb
388 1-19(18d), Feb 1-26(25d), Feb 12-19(7d), Feb 19-26(7d) and Feb 26-Mar 12(18d)
389 retrievals at the 12 stations. The errors in InSAR retrievals are within 4-8 % of the
390 absolute snow depth.

391 The time-series from snow pits in the north-western part of the GM domain also
392 provide valuable snow depth measurements to evaluate the InSAR estimates. The
393 time-series contains data across treeless and forest areas (Fig. 7). Here, again we use
394 the snow pit measurements to reference the InSAR retrievals and obtain the absolute
395 snow depth. It must be noted that snow pit measurements were carried out at different
396 locations, but within a few meters. The snow depth was slightly higher for the treeless
397 area compared to the forested area, which were within 0.25 km of each other. The
398 InSAR retrievals can capture some of the trends very well, while showing contrasting
399 results for others like for the case of the snow poles. The coherence was within 0.12-
400 0.54 and 0.42-0.79 for the treeless and forested areas, respectively. The forested areas
401 exhibited higher coherence for these measurements, and the errors were 2-9 % and
402 3-31% respectively for treeless and forest areas. Based on the two comparisons of
403 InSAR retrievals against snow pole and snow pit data, the errors are within 10 % for
404 most of the retrievals with few exceptions.

405 **3.4 Data Assimilation and Evaluation**

406 In this section, we explore the impact of assimilating L-band InSAR retrievals on
407 modeled SWE and particularly modeled snow depth. As already discussed in Section
408 2.4, we use two assimilation experiments including an open loop (without assimilation)



409 and a reference run to explore the time evolution of modeled snowpack over Grand
410 Mesa for the accumulation season in the water year 2020. Figure 8 shows the time-
411 series of spatially averaged modeled snow depth from the different runs. The spatial
412 averaging was done for the grids without trees and open water over the GM domain.
413 The dotted lines indicate the total spread of the ensemble runs. The assimilation of the
414 ASO lidar snow depth on Feb 1 shifts the ensembles upwards and reduces the spread
415 for both DA and DAU runs. It shows that the reference run (CTRL) was largely
416 underestimating snow depth. While some of the ensemble members with positive
417 perturbation of precipitation were able to capture the actual snow depth,
418 the ensembles with negative perturbation of precipitation underestimated the total
419 snow depth (see the spread in OL run). The assimilation of referenced InSAR retrievals
420 for Feb 12, 19 and 26 (DAU runs) exhibit a small increase in snow depth for the
421 ensemble averages compared to DA runs.

422 The modeled snowpack was also compared with in-situ measurements to assess
423 the impact of data assimilation. The modeled snow depth and SWE at 90 m resolution
424 were compared to snow pit data (IOP and TSD) in locations without trees. The land
425 cover filtered IOP data contained snow depth and SWE from 28 Jan 2020 to 12 Feb
426 2020. Similarly, the land cover filtered TSD contained snow depth from 19 Dec 2019
427 to Apr 17, 2020. There were 68 IOP and 12 TSD snow pit data available for comparison
428 across the GM domain based on the model simulation spatial extent. The RMSE
429 decreased from 35.2 cm to 18.3 cm for snow depth, and for SWE it decreased from
430 8.9 cm to 5.9 cm. The differences in RMSE between DA and DAU runs for these pits
431 were negligible. The modeled snow depth was also compared against snow pole
432 measurements for locations without trees (3 locations, W1A, W1B and W3A) for the
433 entire model simulation period. The RMSE were 17.6, 21.2 and 27.2 cm for the CTRL
434 run, and decreased to 8.1, 21, and 20.8 cm for the DA runs. For DAU runs, the rmse



435 were 8.5, 22.2 and 19.2 cm respectively.

436 The spatial pattern of the modeled snow depth can be evaluated using the
437 reserved InSAR retrievals from Feb 12-19, Feb 19-26 and Feb 26-Mar12 pairs, that
438 were not used for assimilation. Figure 9 shows the spatial pattern of snow depth
439 change for these repeat pass retrieval dates along with their distribution for the entire
440 GM domain. The estimates are shown for the retrievals and all the model runs. The
441 InSAR data were aggregated to 90 m resolution for comparison. And the grids with
442 open water bodies and tree covers (sparse or dense) were all masked out. Additionally,
443 for the ensemble runs, the spatial maps were obtained by averaging the ensembles,
444 and the distributions are for the averaged ensembles.

445 The InSAR retrievals for Feb 12-19 and Feb 19-26 exhibit both increase and
446 decreases in snow depth for the GM domain, while the retrievals for Feb 26-Mar 12
447 show increase in snow depth only (Fig. 9a-c). As expected, the ensemble average for
448 the open loop (OL) run shows spatial variability at the scale of the atmospheric forcing.
449 but shows similar tendency except for Feb 12-19 pair, where it shows decrease in snow
450 depth (Fig. 9d-f). While the DA runs improve the total snow depth and SWE, no
451 improvement in the snow depth change is achieved for the Feb 12-19 pair (Fig. 9g). In
452 addition, there are more grids with decrease in snow depth for the remaining two pairs
453 (Fig. 9h-i) compared to the OL run. Note that the DA does increase the modeled spatial
454 variability in snow depth change.

455 Compared to other model runs, DAU produces best results with positive increase
456 in snow depth change (Fig. 9j-k), also seen in the widening of the distribution in the
457 positive direction (Fig. 9m-n). This is due to the assimilation of InSAR data on Feb 19
458 and 26. Since there was no assimilation of InSAR data on Mar 12, there is no
459 improvement in the modeled snow depth change for Feb 26-Mar 12 even in DAU runs
460 (Fig. 9i and Fig. 9l). The increase or relatively larger increase in snow depth change



461 for DAU runs (Fig. 9j-m) are mostly for the grids where the InSAR data were available
462 for assimilation (Feb 19 and Feb 26). However, the impact of this assimilation appears
463 local in time, and it does produce any significant improvement for the Feb 26-Mar 12
464 pair compared to DA runs. Despite the data constraints, these results indicate that the
465 assimilation of InSAR estimates has the potential to improve the spatial pattern of
466 modeled snow depth change. Because the snow depth evolution is accumulative,
467 these changes will impact the overall seasonal evolution of the snowpack.

468 **4 Discussion**

469 The hyper-resolution InSAR retrievals resolve the wavy roll like patterns due to
470 scouring and drifting of snow over the grasslands as captured by the ASO lidar data
471 over the grasslands in the NW part of GM domain, also shown earlier by Marshall et
472 al. (2021). However, over forested regions, there are disagreements between the lidar
473 and the InSAR estimates with possible uncertainty in both data sets. The average
474 coherence was similar for VV and HH polarization with slightly higher values for VV
475 polarization and lower for HV and VH polarizations. This resulted in higher percentage
476 of missing retrievals in cross-polarizations. The scene-wide average coherence in HH
477 polarization for the 7-day temporal baseline (treeless area) in the GM domain is around
478 0.6-0.7 which is consistent with values reported by Ruiz et al. (2022). Similarly, the
479 coherence was around 0.5-0.65 for the forested area indicating that the L-band can
480 maintain good coherence over canopy and, with sufficient penetration depending on
481 tree density and canopy architecture, it can be useful in measuring ground snow depth
482 changes. The forested areas generally exhibited lower coherence as expected and the
483 coherence differences between treeless and forested areas were around 14-23% to
484 8 % for 7-day and 40-day temporal baselines, respectively. Overall, the InSAR



485 retrievals generally compare well with in-situ measurements from snow pole and snow
486 pit over sparse and dense forests.

487 The interferometric coherence across the GM domain generally decreased with
488 increasing temporal baseline (e.g. by 44 % from 7 to 40-day temporal baseline). This
489 indicates that the retrieval uncertainty and retrieval error will increase with larger time
490 between the repeat passes as expected. Since the underlying density of snowpack will
491 also change between the repeat passes, the retrieval error will also increase when
492 using a constant density in Eq. 1. In this study, the depth weighted density averages
493 or the average bulk density between two repeat pass dates from the reference MSHM
494 model runs were used for the InSAR retrievals. The reference runs generally
495 underestimated the total snow depth and SWE compared to the ASO lidar data and
496 snow pit measurements, but the bulk snow density was slightly higher than the snow
497 pit observations during the IOP over Grand Mesa. This indicates that the HRRR forcing
498 used for the study underestimates the snowfall events, besides model uncertainty
499 associated with wind redistribution of snow which is not accounted for. The modelled
500 higher bulk density could again indicate uncertainty in the fresh snow density (Cao and
501 Barros, 2020; Shrestha and Barros, 2024) and compaction parameterization (e.g.
502 Abolafia-Rosenzweig et al., 2024). The modelled layered snowpack generally shows
503 a two-layer density profile, with an upper layer exhibiting a gradient and near constant
504 density profile in the lower layer. Upon examining density profiles, the difference in
505 snow density profile in the lower layer varied between 1.5-1.8 % (Feb 19-26) and 6-
506 7 % (Feb 1-26) for 7-day and 25-day temporal baseline. This could be still a lower
507 estimate than the actual change in snow density, as shown earlier for 11-day temporal
508 baseline, which was 4 and 11 % for model and snow pit observations. Therefore, the
509 variability in snow density profiles is small for the 7-day base line, and it is large for 25-
510 day base line during the accumulation period. Besides the modelled density has its



511 own bias compared to actual snowpack density due to forcing and model structural
512 uncertainty. However, the calibration of the retrievals to obtain absolute snow depth
513 change from the relative snow depth change could also compensate for these errors.
514 Further in-depth studies are needed to better understand the sources of error.

515 Data assimilation of the ASO Lidar snow depth reduces the error and uncertainty
516 in the modeled snow depth. This also reduced the bulk snow density for the ensemble
517 members with lower snow depth (compared to CTRL run) by 4-5 %, as new snow with
518 lower density is added on the top by the repartition algorithm (Shrestha and Barros,
519 2024). These ensemble members (DA; Fig. 9h-i) also exhibited lower or negative snow
520 depth change for Feb 19-26 and Feb 26-Mar 12 compared to OL ensembles, which is
521 reflected in the ensemble averages over the GM domain. However, the assimilation of
522 referenced InSAR retrievals (DAU) produces increase in snow depth changes in the
523 ensemble average compared to DA runs. The impact is most apparent in the grids of
524 the GM domain where the data were available for assimilation. This produced the best
525 distribution of snow depth change compared to observations, showing the potential of
526 InSAR retrievals in improving the modeled snowpack. It also demonstrates HRRR
527 underestimation of snowfall between the dates of the InSAR pairs (e.g. between Feb
528 26 and Mar 12) and it explains the small snow depth differences in the OL runs
529 compared to InSAR retrievals. The OL shows the increase in snow depth due to
530 snowfall just before Mar 12 (see Fig. 3) albeit underestimated as indicated by the
531 difference in magnitude between the InSAR retrievals and the OL snow depth changes.
532 Likewise, the impact of assimilating InSAR retrievals which improves the simulated
533 snow depth changes (as seen for the first two pairs) highlights the need for high
534 temporal resolution of SAR measurements.



535 **5 Conclusion**

536 This study shows that InSAR retrievals are useful to improve the snowpack
537 simulation and capture its spatial and temporal variability. The assimilation of hyper-
538 resolution retrievals of snow depth is equivalent to a downscaling of precipitation
539 forcing with a bias correction. The RMSE of the InSAR retrievals of absolute snow
540 depth change at native resolution compared to snow pole measurements over different
541 land covers were within 4-6 cm, which corresponds to less than 10 % of the absolute
542 snow depth. However, reference snow depth or SWE is essential to obtain absolute
543 snow depth or SWE for assimilation purposes, which poses a challenge in an
544 operational context. In this situation, one would start from snow-free conditions and
545 build up the absolute snow depth from InSAR retrievals using the prior estimates as
546 reference. Accurate calibration of the estimated relative snow depth change, or SWE
547 will be important to minimize retrieval errors. Future studies are needed to advance a
548 general framework for calibrating InSAR retrievals and obtaining absolute snow depth
549 or SWE for assimilation into the models.

550



551 **Code availability**

552

553 The MPDAF v1.0 software with experiment setups is available from
554 <https://github.com/mpdaf23/mpdaf.git>. MSHM v3.0 used here is documented in Kang
555 and Barros (2011a, 2011b); Cao and Barros (2020) including the updates described in
556 this paper. MEMLS can be downloaded from
557 <http://www.iapmw.unibe.ch/research/projects/snowtools/memls.html>. The NCAR
558 DART can be downloaded from <https://github.com/NCAR/DART.git>.

559 **Data availability**

560

561 The NASA SnowEx 2020 observation data can be downloaded from NASA
562 National Snow and Ice Data Center Distributed Active Archive Center and ASF DAAC.
563 HRRR atmospheric forcing data can be now downloaded from Amazon Web Services
564 (AWS) courtesy of National Oceanic and Atmospheric Administration (NOAA) and the
565 Registry of Open Data on AWS. The NLDAS albedo data can be downloaded from the
566 NASA GES DISC. Model data and software used for visualization is available from
567 <https://uofi.box.com/v/InSARmodeldata>.

568 **Author contribution**

569

570 PS and APB conceptualized the study. PS designed the study, processed the
571 data, conducted the model simulation with data assimilation, carried out the analysis,
572 and wrote the paper. APB acquired the grant for the study and contributed to editing of
573 the manuscript.

574 **Competing interests**

575

576 The authors declare that they have no conflict of interest.

577



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579

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591



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749



750 **Appendix A1**

751

752 The atmospheric delay experienced by a microwave signal can be estimated by
753 integrating the atmospheric refractivity along the line of sight from the surface to the
754 airborne sensor height. Neglecting the impact of ionosphere for the UAVSAR flying at
755 a height of z_s , the scaled up atmospheric refractivity of moist air [$N=(n-1)10^6$], where n
756 is the refractive index, is given by

$$757 \quad N(x, z) = k_1 \frac{P}{T} + (k_2 - k_1) \frac{e}{T} + k_3 \frac{e}{T^2} + k_4 W_{cl}$$

758 where P is pressure [hPa], T is air temperature [K], e is vapor pressure [hPa], W_{cl}
759 is liquid water content [kgm^{-3}], n_e is ionization and f is frequency. The remaining term
760 are constants: $k_1 = 0.776 \text{ KPa}^{-1}$, $k_2 = 0.716 \text{ KPa}^{-1}$, $k_3 = 3750 \text{ K}^2 \text{ Pa}^{-1}$, $k_4 =$
761 $1430 \text{ m}^3 \text{ kg}^{-1}$. Based on the works of Smith and Weintraub (1953), the above relation
762 is restricted to certain limits of the variables for an accuracy of 0.5 percent in $N(x, z)$.
763 The limits in this case restrict its use to temperatures of -50 to $+40^\circ \text{ C}$, total pressures
764 of 200 to 1100 mb, water-vapor partial pressures of 0 to 30 mb, and a frequency range
765 of 0 to 30 GHz.

766 $N(x, z)$ can be further decomposed into the mean and turbulent part for a radar
767 scene as:

$$768 \quad N(x, z) = \bar{N}(z) + N'(x, z)$$

769 where $\bar{N}(z)$ is the average vertical stratification for the given resolution of the
770 atmospheric model (here 3 km) and $N'(x, z)$ is the deviation from the average profile
771 along the location x in the radar scene (within the atmospheric grid). Neglecting the
772 turbulent terms, zenith delay L for the mean part can be computed as

$$773 \quad L = \int_{z_{ref}}^{z_s} \left(k_1 \frac{P}{T} + (k_2 - k_1) \frac{e}{T} + k_3 \frac{e}{T^2} \right) dz$$

774 Using $dP = -\rho g dz$ and $\rho = P/R_d T$, where ρ is air density [kgm^{-3}], $R_d =$



775 $287.053 \text{ Jkg}^{-1}\text{K}^{-1}$ is the dry gas constant, and g is acceleration due to gravity, we
776 obtain:

$$777 \quad L = -10^{-6} \left(k_1 \frac{R_d}{g} (P(z_s) - P(z_{ref})) \right) + 10^{-6} \int_{z_{ref}}^{z_s} \left((k_2 - k_1) \frac{e}{T} + k_3 \frac{e}{T^2} \right) dz$$

778 The first term of the right side is the hydrostatic correction term, and the second
779 term is the wet correction term. The atmospheric phase delay along the line of sight
780 (LOS) can then be estimated using the microwave wavelength (λ) and incidence angle
781 (θ_{inc}) as:

$$782 \quad \Phi_{atm} = \frac{4\pi}{\lambda} \frac{L}{\cos(\theta_{inc})}$$

783 The above simple approximation for computing atmospheric phase delay along
784 the LOS could introduce additional uncertainty (Wang et al., 2021). More importantly,
785 since SAR interferograms are not sensitive to image-wide phase biases, there will be
786 no horizontal delay differences over flat terrain. However, for a radar scene with terrain,
787 the differences in the vertical refractivity during both acquisitions will affect phase
788 difference between two arbitrary resolution cells with different topographic
789 height (Hanssen, 2001). Therefore, the contribution of tropospheric stratification in the
790 interferogram will only be present if the radar scene has resolution cells with different
791 elevations. So, we compute the differential atmospheric phase delay between location
792 with maximum elevation ($z_{ref} = p$) and all other locations ($z_{ref} = q$) in the radar scene
793 for two SAR acquisition time t_1 and t_2 as:

$$794 \quad \Delta\Phi_{atm} = \frac{4\pi}{\lambda \cos\theta_{inc}} [(L_p^{t_1} - L_q^{t_1}) - (L_p^{t_2} - L_q^{t_2})]$$

795 Then the phase change contribution due to snowpack is estimated as:

$$796 \quad \Delta\Phi_s = \Delta\Phi_{InSAR} - \Delta\Phi_{atm}$$

797



798 **Tables**

799

800 **Table 1:** UAVSAR flight retrieval dates for Grand Mesa during SnowEx'20 campaign.

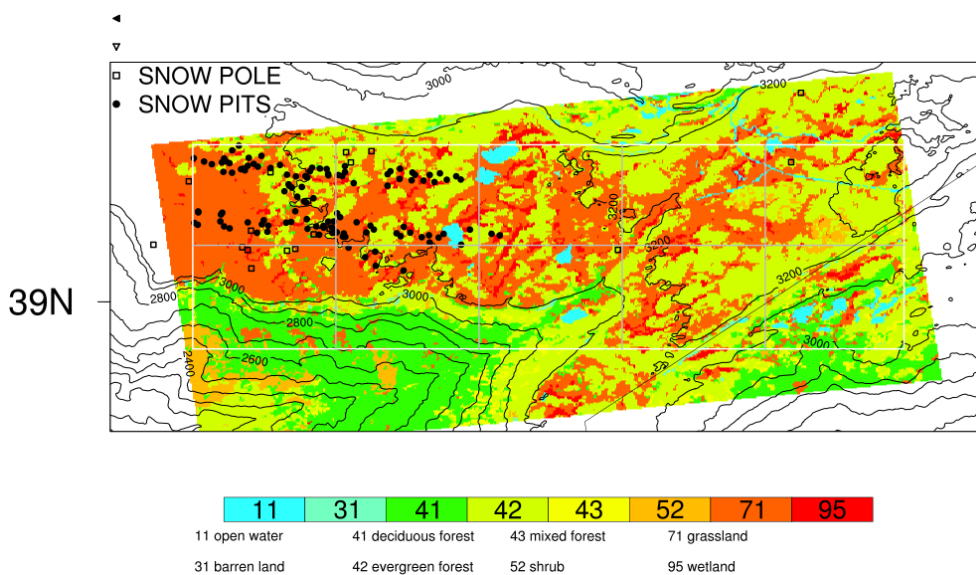
Flight track	Acquisition Date
3	Feb 01 2020 (02:13:36 – 02:15:58 UTC)
5	Feb 12 2020 (16:47:20 – 16:49:45 UTC)
8	Feb 19 2020 (17:24:18 – 17:27:07 UTC)
13	Feb 26 2020 (17:40:54 – 17:43:34 UTC)
17	Mar 12 2020 (18:17:08 – 18:20:28 UTC)

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803 **Figures**



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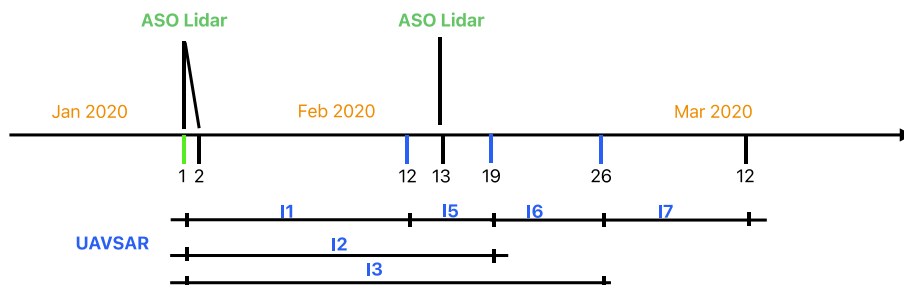
806 **Figure 1:** Spatial pattern of land cover and topography over the Grand Mesa (GM)

807 domain (white outline). The gray boxes outline the 3 km atmospheric grids. The solid

808 black and square markers show the location of snow pit and snow pole measurements

809 available from SnowEx'20 campaign.

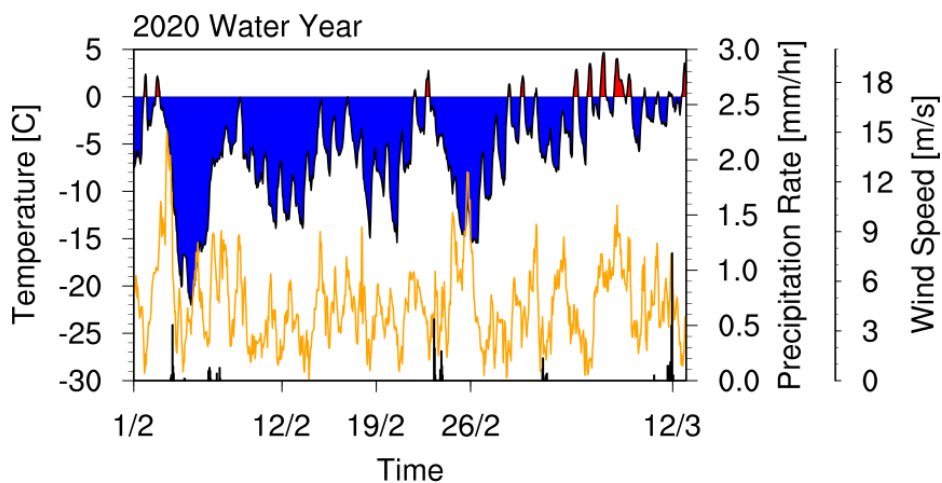
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812 **Figure 2:** Timeline of availability of UAVSAR interferometric products and ASO Lidar
813 retrievals of snow depth and SWE for SnowEx'20 campaign over Grand Mesa. I1, I2,
814 I3 and I5, I6, I7 indicate the six InSAR pairs used for data assimilation and model
815 evaluation respectively. The dates with green and blue tick mark represent days when
816 the retrievals were used for assimilation in the data assimilation experiments.

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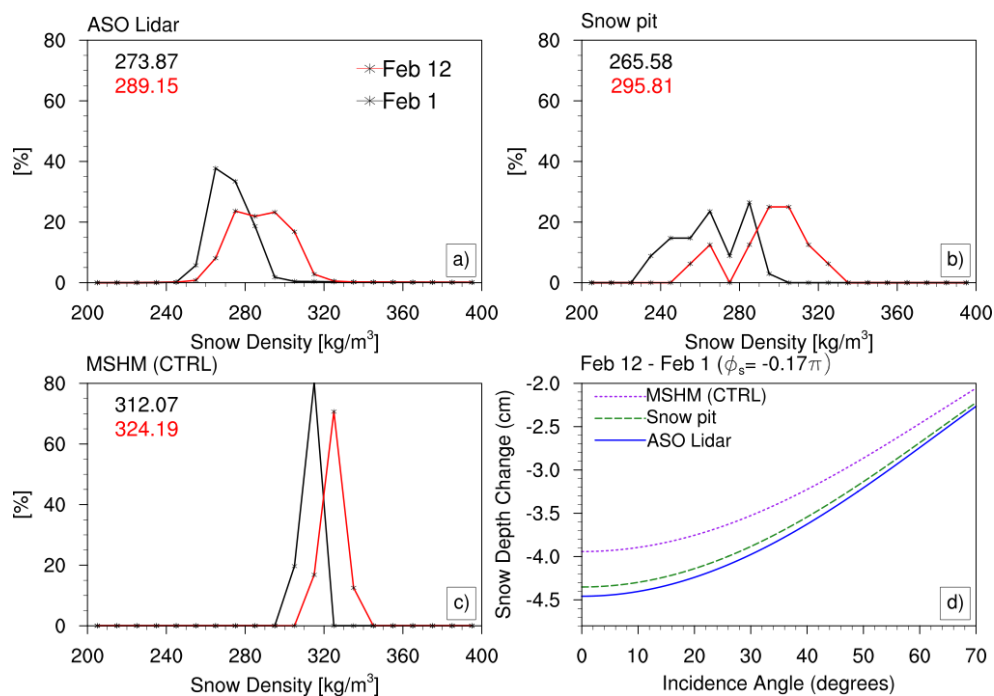


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819 **Figure 3:** Meteorological data from atmospheric model for north-west GM subdomain
820 showing air temperature (blue/red), wind speed (orange) and precipitation rate (bar
821 plot). The time axis highlights the dates when the L-band UAVSAR flight data were
822 available for SnowEx'20 campaign.

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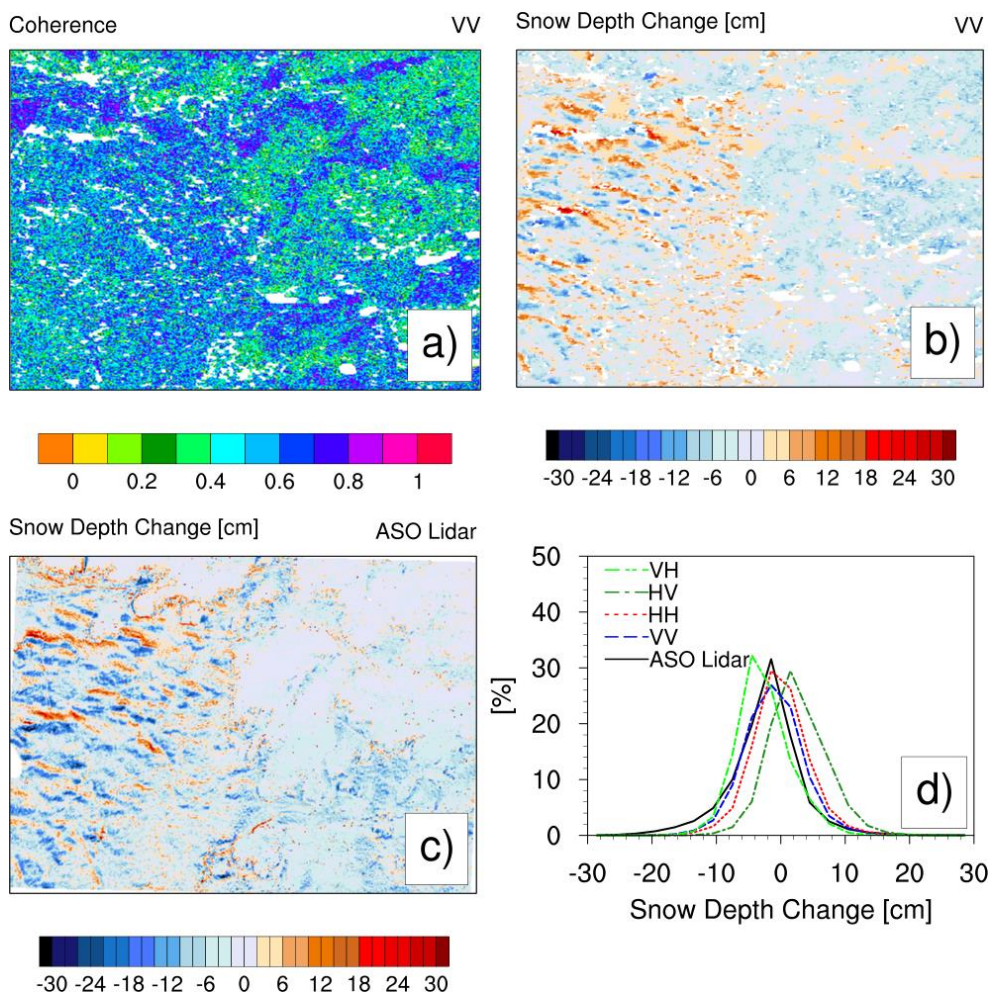
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827 **Figure 4: a-c)** Snow density distribution at two different dates from the ASO Lidar data,
828 snow pit measurements (Intensive Observation Period) and MSHM control run. **d)**
829 Impact of snow density on the L-band InSAR retrieval of snow depth change between
830 the two dates as a function of incidence angle for a fixed change in phase due to
831 snowpack ($\phi_s = 0.17\pi$). The dates for ASO Lidar in actual are Feb 1/2 and Feb 13. We
832 use Feb 1 and Feb 12, due to availability of InSAR phase data for these dates.

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837 **Figure 5:** a) Spatial pattern of coherence from L-band VV polarization InSAR retrieval

838 for north-west GM subdomain. b) Estimated spatial pattern of snow depth changes

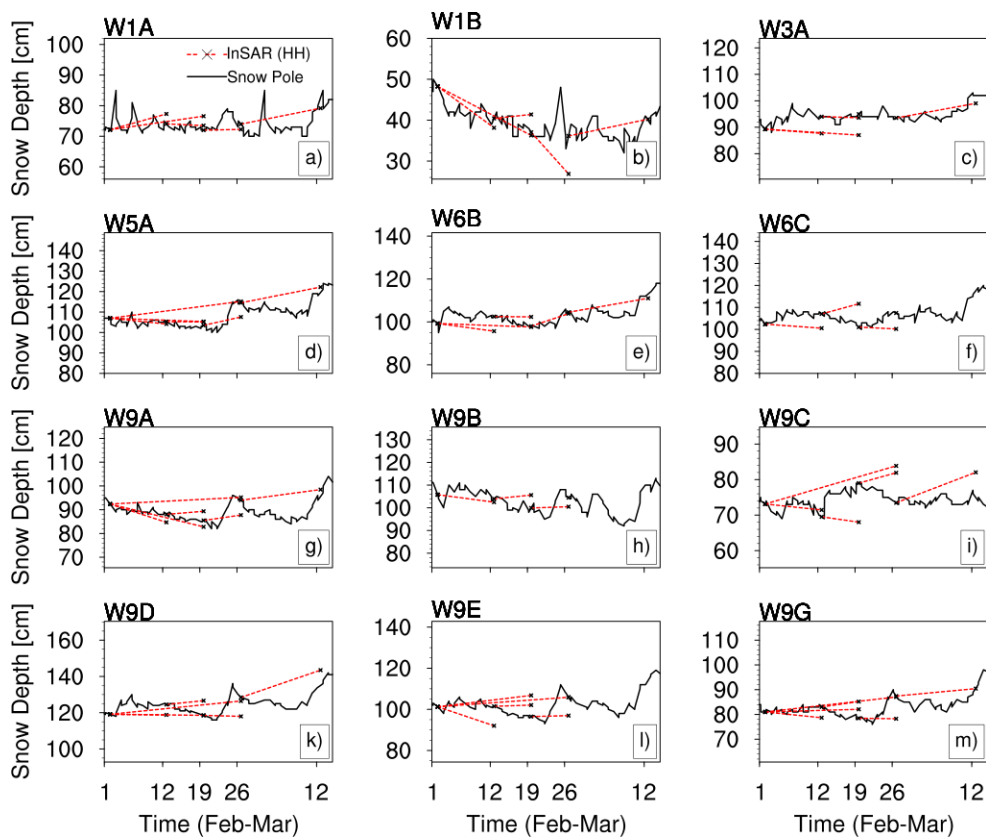
839 from the same retrieval. c) Spatial pattern of snow depth change from ASO Lidar data

840 (Feb 1/2–13). d) Distribution of change in snow depth for ASO Lidar and InSAR

841 retrievals for VV, HH, HV and VH polarizations. The InSAR retrievals were obtained

842 from UAVSAR flight pairs for Feb 1 and Feb 12.

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846 **Figure 6:** Comparison of L-band InSAR retrieval (HH polarization) of snow depth with

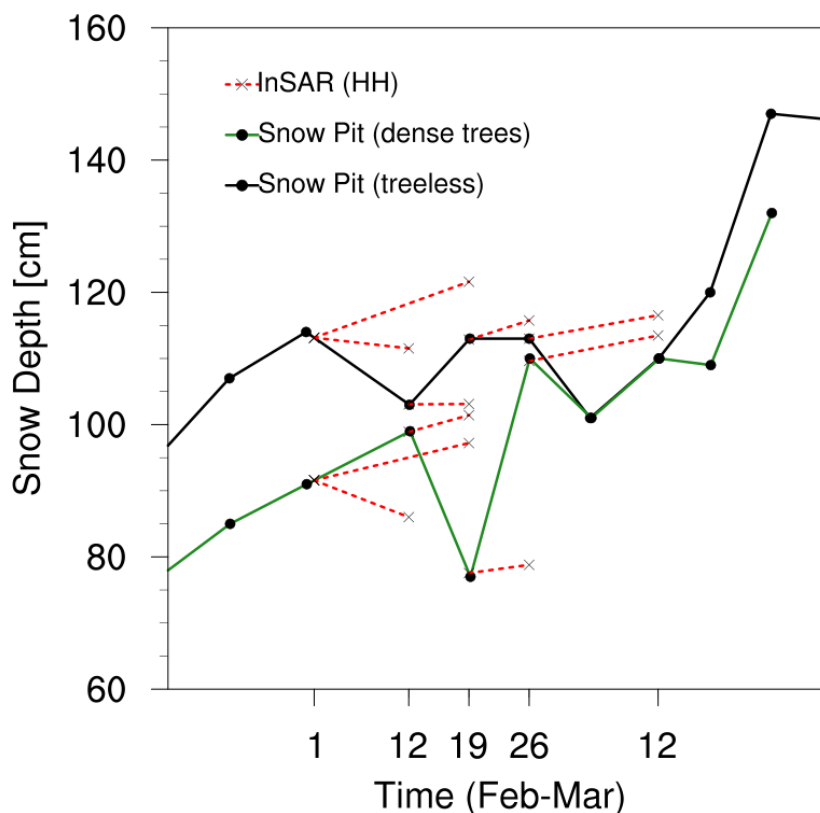
847 Snow Pole measurements for locations with different landcover within the GM domain

848 (a-c: Treeless; d-f: Sparse trees; g-m: Dense trees). For the InSAR retrieval, snow

849 depth measurements from Snow Pole sites were used a reference for the repeat pass

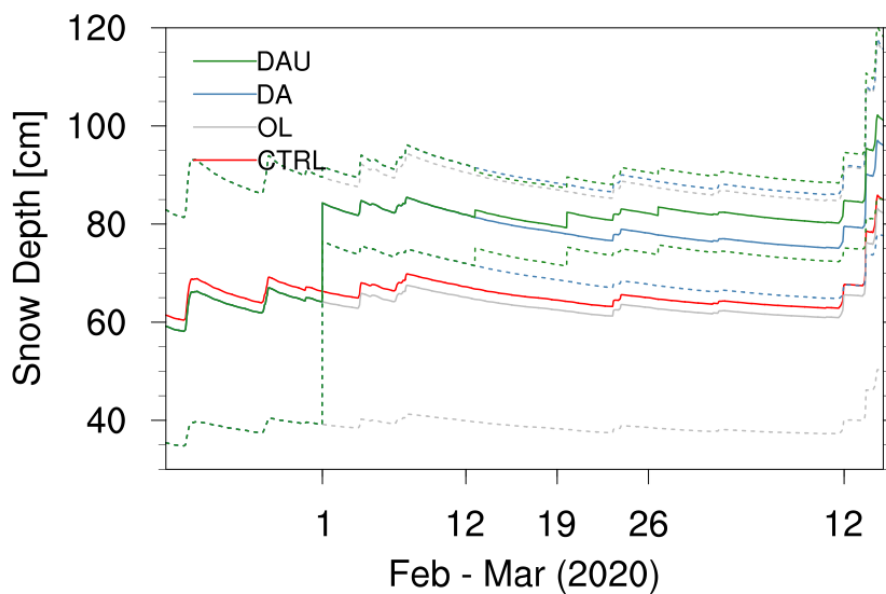
850 UAVSAR flight pairs.

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Figure 7: Comparison of L-band InSAR retrieval (HH polarization) of snow depth with snow pit time-series measurements for two locations with different landcover (treeless and dense trees) within the GM domain. For the InSAR retrieval, snow depth measurements from snow pit site were used a reference for the repeat pass UAVSAR flight pairs

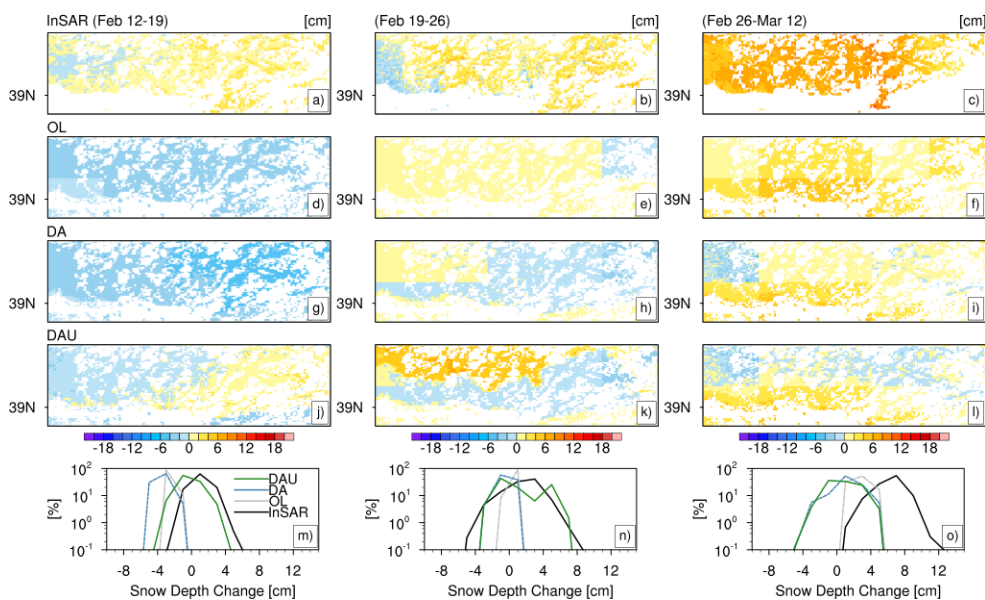


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Figure 8: Time series of modeled snow depth for CTRL, OL, DA and DAU run.

863 The dates when observation were assimilated are also shown by tick marks: DA (Feb
864 1) and DAU (Feb1, Feb 12 and Feb 26) are also shown by the tick marks. The
865 ensemble spread for OL, DA and DAU runs are shown by the dotted lines.

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869 **Figure 9:** Spatial pattern and histogram of change in snow depth over the GM domain
870 for Feb 12-19, Feb 19-26 and Feb 26-Mar 12: **a-c)** InSAR retrievals, **d-f)** ensemble
871 averaged open loop run (OL), **g-i)** ensemble averaged data assimilation run with ASO
872 Lidar data (DA), **j-l)** ensemble average data assimilation runs with ASO Lidar and
873 referenced InSAR data (DAU), and **m-p)** frequency distribution of snow depth change
874 for InSAR, OL, DA and DAU runs for respective pairs.

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