## S1 Supplementary Meterial

## S1.1 Planetary Waves

The azonal component describes quasi-stationary planetary waves. The calculation depends on the level of height. At the equivalent barotropic level, azonal components of horizontal velocity are computed employing the definition of the stream function

$$\langle u_{EBL}^*(z) \rangle = -\nabla_{\phi} \langle \psi_{EBL}^* \rangle$$
 (S1)

$$\langle v_{EBL}^*(z) \rangle = \nabla_{\lambda} \langle \psi_{EBL}^* \rangle \tag{S2}$$

whereby the azonal component are computed assuming isothermal expansion of air parcels in planetary waves

$$\langle p_z^* \rangle = \langle p_{EBL}^* \rangle \exp[(z - z_{EBL})/H_0] + \frac{p_* g}{\Gamma R} \exp[-z/H_0] \left\{ \ln \left[ \frac{T(z)}{T(z_{EBL})} \right] - \ln \left[ \frac{\overline{T(z)}}{T(z_{EBL})} \right] \right\}$$
 (S3)

and

$$\langle p_{EBL}^* \rangle = \rho \left\{ \overline{\langle u_{EBL} \rangle} \right\} \nabla_{\phi} \langle \psi_{EBL}^* \rangle + 2 \left( \frac{\overline{\langle u_{EBL} \rangle}}{a \cos(\phi)} + \Omega \right) \sin(\phi) \langle \psi_{EBL}^* \rangle$$
 (S4)

## S1.1.1 Planetary Waves – orographically stream function:

For the waves excited by the orography, the stream function is calculated by

$$\beta \nabla_{\lambda} \langle \psi_{or,0,EBL}^* \rangle = -\frac{f}{H_0} \langle w_{or} \rangle + \frac{f^2}{g} \frac{\partial \langle u'v' \rangle^*}{\partial z}$$
(S5)

where f is the Coriolis parameter and  $\beta = \nabla_{\phi} f$  and

$$w_{or} = \langle u \rangle \nabla_{\phi} h_{or} + \langle v \rangle \nabla_{\lambda} h_{or} + a_{std} (\langle u \rangle^2 + \langle v \rangle^2 + \langle u'^2 \rangle + \langle v'^2 \rangle)^{1/2} h_{std}.$$
(S6)

The variable  $h_{or}$  describes the grid cell averaged orography height  $h_{std}$  the subgrid scale standard deviation of the height of mountains, and  $a_{std}$  is an additional tuning parameter.

The azonal component describes quasi-stationary planetary waves and is subdivided into a geostrophic and ageostrophic term:

$$u^* = u^*_{aeos} + u^*_{aaeos}$$

$$v^* = v_{geos}^* + v_{ageos}^*$$

## S1.2 Derivation of the zonal mean meridional wind velocity

The zonal mean meridional wind velocity  $\overline{\langle v(z,\phi)\rangle}$  which also accounts for convective contribution is calculated by

$$\overline{\langle v(z,\phi)\rangle}$$

$$=\frac{d1*(-2\tan(\phi)\left(\overline{\langle u^*v^*\rangle}+\overline{\langle u'v'\rangle}\right))+d2*\left(\frac{\partial}{\partial \phi}\left(\overline{\langle u^*v^*\rangle}+\overline{\langle u'v'\rangle}\right))+d3*\left(\left(-\frac{dK_z}{z}+\frac{K_z}{H_0}\right)\frac{\partial\overline{\langle u\rangle}}{\partial z}a\right)+d4*(A)}{n1*(\tan(\phi)\overline{\langle u\rangle})+n2*\left(-\frac{\partial\overline{\langle u\rangle}}{\partial \phi}\right)+n3*(2\Omega a\sin(\phi))}$$

With  $K_z = 0.005 z$  and In (4)

$$A = \left(\frac{P_{conv} L}{(\Gamma_a - \Gamma)} - \frac{1}{H_0}\right) \langle u_{s\_profile} \rangle$$

Whereby  $\Gamma$  is the lapse rate in the troposphere calculated by using the formula from Petoukhov (Petoukhov et al., 2000),  $P_{conv}$  by the cloud module implemented by Eliseev at al. (Eliseev, n.d.) and

$$\langle u_{s\_profile} \rangle = \left\{ \begin{array}{cc} 2, & |\phi| > 40 \\ -2 \, \cos \left(\phi \frac{\pi}{40^{\circ}}\right), & \text{otherwise} \end{array} \right.$$

The additional calculating of  $\langle u_{s\_profile} \rangle$  instead of using the calculated surface zonal velocity is done to avoid instabilities.

For the derivation we start with the differential equation of the zonal wind component

$$\frac{du}{dt} = \frac{\tan\phi}{a}uv + fv - \frac{1}{\rho}\Delta_{\lambda}p + F_{u} \tag{S9}$$

Whereby a is the Earth radius, f is the Coriolis factor and  $F_u$  is the frictional force in u-direction. Multiplying the equation with  $\rho$  and using that  $\rho \frac{du}{dt} = \frac{d(\rho u)}{dt} - u \frac{d\rho}{dt}, \frac{d(\rho u)}{dt} = \frac{\partial(\rho u)}{\partial t} + \mathbf{V} \cdot \mathbf{\Delta} (\rho u)$  and  $\mathbf{V} \cdot \mathbf{\Delta} (\rho u) = \mathbf{\Delta} (\rho u \mathbf{V}) - (\rho u) \mathbf{\Delta} \cdot \mathbf{V}$ , we get

$$\frac{\partial(\rho u)}{\partial t} + \Delta \left(\rho u \mathbf{V}\right) - u \left(\frac{d\rho}{dt} + (\rho u) \mathbf{\Delta} \cdot \mathbf{V}\right) = \frac{\tan \phi}{a} \rho u v + f \rho v - \Delta_{\lambda} p + \rho F_{u}$$

With the continuity equation and using spherical coordinates, the equation simplifies to

$$\frac{\partial(\rho u)}{\partial t} + \frac{1}{a\cos\phi} \frac{\partial(\rho u^2)}{\partial \lambda} + \frac{1}{a\cos\phi} \frac{\partial(\rho\cos\phi uv)}{\partial \phi} + \frac{\partial(\rho wu)}{\partial z} 
= \frac{\tan\phi}{a} \rho uv + f\rho v - \frac{1}{a\cos\phi} \frac{\partial p}{\partial \lambda} + \rho F_u$$
(S10)

We calculate the zonal average (...), take into account that  $\frac{\partial \overline{x}}{\partial \lambda} = 0$  and assume a vertical dependence of the density  $(\rho = \rho_0(z))$ :

$$\frac{\overline{\partial(\rho_0 u)}}{\partial t} + \frac{1}{a} \frac{\overline{\partial(\rho_0 uv)}}{\partial \phi} + \frac{\overline{\partial(\rho_0 wu)}}{\partial z} = 2 \frac{\tan \phi}{a} \rho \overline{uv} + f \rho \overline{v} + \rho_0 \overline{F_u}$$

We split the wind variables into an synoptic scale waves, planetary waves and zonal mean wind  $(u = \bar{u} + u^* + u')$ . Under the assumption that  $\bar{u}$  and  $v^*$  are independent, the result of the zonal mean over the azonal component is zero:

$$\overline{uv} = \overline{u}\overline{v} + \overline{u}v^* + \overline{u}v' + u^*\overline{v} + u^*v^* + u^*v' + u'\overline{v} + u'v^* + u'v'$$

$$= \overline{u}\overline{v} + \overline{u}v' + u^*v^* + u'\overline{v} + u'v'$$

We average eq. (10) over time and phase speed ( $\langle ... \rangle$ ). By assuming independency of the variables, we can simplify the terms  $\langle \bar{u}v' \rangle = \langle u'\bar{v} \rangle = 0$ . In addition, it is  $\overline{u}\bar{v} = \bar{u}\bar{v}$  due to quasi stationarity of both terms. It is also  $\langle \frac{dx}{dt} \rangle = 0$ 

and  $\langle \bar{u}\bar{v}\rangle = \langle \bar{u}\rangle\langle \bar{v}\rangle$  since the oscillations of  $\bar{u}$  and  $\bar{v}$  are very small and independent of each other. By using the continuity equation  $\frac{\rho_0}{a}\frac{\partial \langle \bar{v}\rangle}{\partial \phi} - \frac{\tan\phi}{a}\rho_0\bar{v} + \frac{\partial(\rho_0\langle \bar{w}\rangle)}{\partial z} = 0$ , we can simplify eq. (S10) to

$$\frac{1}{a}\rho_{0}\langle\bar{v}\rangle\frac{\partial\langle\bar{u}\rangle}{\partial\phi} + \frac{\rho_{0}}{a}\frac{\partial(\overline{\langle v^{*}u^{*}\rangle} + \langle\overline{v'u'}\rangle)}{\partial\phi} + \rho_{0}\langle\bar{w}\rangle\frac{\partial\langle\bar{u}\rangle}{\partial z} + \frac{\partial(\rho_{0}\langle\overline{w^{*}u^{*}\rangle} + \langle\overline{w'u'}\rangle)}{\partial z} \\
= \frac{\tan\phi}{a}\rho_{0}\langle\bar{u}\rangle\langle\bar{v}\rangle + 2\frac{\tan\phi}{a}(\overline{\langle v^{*}u^{*}\rangle} + \overline{\langle v'u'\rangle}) + f\rho\bar{v} + \rho_{0}\bar{F}_{u}$$
(S11)

With the assumption that  $\rho_0 = e^{-z/H_0}$  and  $\rho_0 \overline{F_u} = \frac{\partial \, \overline{\tau}}{\partial z} = \frac{\partial}{\partial z} \left( \kappa \rho_0 \frac{\partial \langle \overline{u} \rangle}{\partial z} \right) = \kappa \frac{\partial \, \rho_0}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \kappa \frac{\partial^2 \langle \overline{u} \rangle}{\partial z^2} = -\kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z}$ , we obtain

$$\begin{split} & \rho_0 \langle \overline{v} \rangle \left( \frac{1}{a} \frac{\partial \langle \overline{u} \rangle}{\partial \phi} - \frac{\tan \phi}{a} \langle \overline{u} \rangle - f \right) = \\ & 2 \frac{\tan \phi}{a} \left( \overline{\langle v^* u^* \rangle} + \overline{\langle v' u' \rangle} \right) - \frac{\rho_0}{a} \frac{\partial \overline{\langle v^* u^* \rangle} + \overline{\langle v' u' \rangle}}{\partial \phi} - \rho_0 \langle \overline{w} \rangle \frac{\partial \langle \overline{u} \rangle}{\partial z} - \frac{\partial \left( \rho_0 \overline{\langle w^* u^* \rangle} + \overline{\langle w' u' \rangle} \right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \overline{\langle u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \overline{\langle u} \rangle}{\partial z} \end{split}$$

The contribution to the vertical exchange of the atmospheric momentum from stationary eddies described in our case by zonally averaged  $\langle \overline{w}^* u^* \rangle$  is shown negligibly small (Hantel and Hacker, 1978). Also, the scale analysis attests that Also, the scale analysis attests that  $\langle \overline{w} \rangle \frac{\partial \langle u \rangle}{\partial z}$  are small:

$$-\rho_0 \langle \overline{w} \rangle \frac{\partial \langle \overline{u} \rangle}{\partial z} - \frac{\partial \left(\rho_0 \langle \overline{w^*u^*} \rangle + \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} \approx - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - 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\frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \langle \overline{u} \rangle}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u'} \rangle\right)}{\partial z} = - \frac{\partial \left(\rho_0 \langle \overline{w'u$$

Hence the eq. (S12) can be rewritten into

$$\begin{split} & \rho_0 \langle \bar{v} \rangle \left( \frac{1}{a} \frac{\partial \langle \bar{u} \rangle}{\partial \phi} - \frac{\tan \phi}{a} \langle \bar{u} \rangle - f \right) = \\ & 2 \frac{\tan \phi}{a} \left( \overline{\langle v^* u^* \rangle} + \overline{\langle v' u' \rangle} \right) - \frac{\rho_0}{a} \frac{\partial \overline{\langle v^* u^* \rangle} + \overline{\langle v' u' \rangle}}{\partial \phi} - \rho_0 \langle \overline{w} \rangle \frac{\partial \overline{\langle u} \rangle}{\partial z} - \frac{\partial \left( \rho_0 \overline{\langle w^* u^* \rangle} + \overline{\langle w' u v \rangle} \right)}{\partial z} - \kappa \frac{\rho_0}{H_0} \frac{\partial \overline{\langle u} \rangle}{\partial z} + \rho_0 \frac{\partial \kappa}{\partial z} \frac{\partial \overline{\langle u} \rangle}{\partial z} \end{split}$$

With  $\langle \overline{u'w'} \rangle = -\kappa' \frac{\partial \langle \overline{u} \rangle}{\partial z}$ , whereby  $\kappa'$  is the coefficient of large-scale turbulent exchange for the momentum due to transient synoptic eddies (Williams and Davies, 1965), we get

$$\begin{split} \rho_0 \langle \bar{v} \rangle \left( \frac{1}{a} \frac{\partial \langle \bar{u} \rangle}{\partial \phi} - \frac{\tan \phi}{a} \langle \bar{u} \rangle - f \right) \\ &= 2 \frac{\tan \phi}{a} \left( \overline{\langle v^* u^* \rangle} + \langle \overline{v' u'} \rangle \right) - \frac{\rho_0}{a} \frac{\partial \left( \overline{\langle v^* u^* \rangle} + \langle \overline{v' u'} \rangle \right)}{\partial \phi} - (\kappa + \kappa') \frac{\rho_0}{H_0} \frac{\partial \langle \bar{u} \rangle}{\partial z} \\ &+ \rho_0 \frac{\partial (\kappa + \kappa')}{\partial z} \frac{\partial \langle \bar{u} \rangle}{\partial z} \end{split}$$

With  $\tilde{\kappa} = \kappa + \kappa'$  we can simplify the equation to

$$\overline{\langle v(z,\phi)\rangle} = \frac{-2\tan(\phi)\left(\overline{\langle u^*v^*\rangle} + \overline{\langle u'v'\rangle}\right) + \frac{\partial}{\partial\phi}\left(\overline{\langle u^*v^*\rangle} + \overline{\langle u'v'\rangle}\right) + \left(-\frac{dK_z}{z} + \frac{K_z}{H_0}\right)\frac{\partial\overline{\langle u\rangle}}{\partial z}a}{\tan(\phi)\overline{\langle u\rangle} - \frac{\partial\overline{\langle u\rangle}}{\partial\phi} + 2\Omega a\sin(\phi)}$$

. (S13)