СООБЩЕНИЯ ОБЪЕДИНЕННОГО ИНСТИТУТА ЯДЕРНЫХ ИССЛЕДОВАНИЙ ДУБНА



E2 - 8149

A.Uhlmann

PROPERTIES OF THE ALGEBRAS L + (D)

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Препринты, сообщения и депонированные публикация ОИЯИ имеют единую нарастающую порядковую нумерацию, составляющую последние 4 цифры индекса.

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"Р" - издание на русском языке;

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Индексы, описанные выше, проставляются в правом верхнем углу на обложке и титульном листе каждого издания.

Ссылки

В библиографических ссылках на преприиты и сообщения ОИЯИ мы рекомендуем указывать: инициалы и фамилию автора, далее сокращенное наименование института-издателя, видекс, место и год издания.

Пример библиографической ссылки:

И.И.Иванов. ОИЯИ, Р2-4985, Дубна, 1971.

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PROPERTIES OF THE ALGEBRAS L $^+$ (D)

Ульман А.

E2 - 8149

Свойства алгебр $\mathfrak{L}^{^{+}}(\mathfrak{D})$

Рассматриваются свойства алгебры всех операторов, которые вместе со своими сопряженными операторами отображают в себе данное пинейное подмножество гильбертового пространства. Каждый автоморфизм и каждая производная этой алгебры являются внутренними. Их можно определить алгебраическим образом.

Сообщение Объединенного института ядерных исследований Дубна, 1974

Uhlmann A.

E2 - 8149

Properties of the Algebras \$ +(5))

We consider properties of the algebra of all operators which together with its abjoints transform a given dense linear manifold of an Hilbert space into itself. This algebra admits inner *-automorphisms and derivations only and there is an algebraic characterisation of this algebra.

Communications of the Joint Institute for Nuclear Research.

Dubna, 1974

1. Definitions, results.

Let # be a dense linear submanifold of the Hilbert space γ . With $\mathcal{L}^{\bullet}(\mathcal{S})$ we denote the set of all such linear operators a from $\mathcal J$ into $\mathcal J$, a $\mathcal J$ § $\mathcal J$, for which $\mathcal J$ is in the domain of definition of a^* and $a^*J:J. f^*(J)$ is an algebra with respect of the ordinary addition and multiplication of operators. L'(J) becomes a *-algebra by the involution $\alpha \rightarrow \alpha^{+}$, where α^{+} is defined to be the restriction of a onto D .

We shall prove the following theorems:

Theorem 1: Let τ be a *-isomorphism from $\mathcal{L}'(\mathcal{J}_i)$ onto $\mathcal{L}'(\mathcal{J}_i)$ Then there exists a unitary map u from \mathcal{J}_{s} onto \mathcal{J}_{t}

Theorem 2: Every Lautomorphism v of L'(D) is an inner one, i.e., there is a unitary element u & L'(D) with ray = uau for all a & L+(D).

Theorem 2 is an obvious consequence of theorem 1. Note that these theorems auggest the existence of a "space-free" definition of $f^{\dagger}(D)$ (theorems 4 - 6).

Let us now remind that a derivation of $f(\mathcal{S})$ is a linear map of L (a) into itself satisfying

(3)
$$g(ab) = g(a) \cdot b + a \cdot g(b)$$
.

Theorem 3 (P.Kröger): Is φ a derivation of $\mathcal{L}(D)$, then there exists an element $x \in \mathcal{L}(\mathcal{S})$ with

$$\varphi(\alpha) = x\alpha - \alpha x.$$

Hence every derivation is an inner one. [4]

One knows [1] that $\mathcal{L}'(\mathcal{X})$,where \mathcal{H} is a Hilbert space, is the von Leumann algebra of all bounded operators. Von Noumann has proved that every left ideal of this algebra is generated by a projection, i.e., an operator p with $p \circ p^4 \circ p^4$ (see for instance [3]). The technique of this proof also works in the more general case of the $\mathcal{L}^*(\mathcal{J})$ algebras. We now explain shortly, how one can use these techniques to characterise the algebras $\mathcal{L}''(\mathcal{J})$ abstractly. Definition 1: Let \mathcal{A} be a *-algebra. \mathcal{A} is called an alrebra with "property I" if and only if

- (i) every proper left ideal contains a minimal left ideal.
- (ii) every minimal left ideal is generated by a minimal projection, and
- (iii) every element of every subalgebra \mathcal{A}_{o} , which contains an identity e_{o} , has a non-empty spectrum.

Let us 'irst add some remarks. A projector p is minimal in \mathcal{A} iff $p \neq 0$ and $pq \cdot qp$ implies $pq \cdot p$ for every rojector q of \mathcal{A} . If \mathcal{A} , is an algebra with identity e, then the spectrum of one of its elements a is the set of all complex numbers λ such, that $(a - \lambda e)^{-1}$ does not exist in \mathcal{A} .

We now construct an example of a *-algebra with property I. Let \top be an index set (an abstract set) and assume to be associated to every $t \in T$ an algebra $f^*(D_t)$. Then the *-algebra

(5)
$$\prod_{t \in T} \mathcal{I}^{+}(\mathcal{D}_{t}) = \mathcal{I}^{+}(\mathcal{D}_{t}, t \in T)$$

consists of all functions $t \to \kappa(t)$ defined on T with $\kappa(t) \in \hat{\mathcal{L}}^*(\mathcal{J}_t)$ together with the composition laws $(\kappa_* + \kappa_*)(t) = \kappa_*(t) + \kappa_*(t)$, $(\kappa,\kappa_*)(t) = \kappa_*(t) \kappa_*(t)$, $(\kappa^*)(t) = \kappa(t)^*$, $(\lambda \kappa)(t) = \lambda \kappa(t)$

This construction provides us with a Lalgebra. Theorem u_t $f^*(J_t, t \in T)$ satisfies property I.

Theorem 5: Let $\mathcal A$ be a *-algebra with property I . Then there exists up to *-isomorphisms one and only one algebra $\mathcal L'(\mathcal J_{\epsilon}, t \cdot \mathsf T)$ and a *-isomorphism ε of $\mathcal A$ into $\mathcal L'(\mathcal J_{\epsilon}, t \cdot \mathsf T)$ which maps the set of all minimal projectors of $\mathcal A$ onto the set of all minimal projectors of $\mathcal L'(\mathcal J_{\epsilon}, t \cdot \mathsf T)$.

Definition 2: A *-sigebra is called a "type I a algebra" if the following two conditions are fullfilled:

- 1) A has property I
- 2) Let τ be a *-isomorphism from $\mathcal A$ into a *-elgebra $\mathcal B$ with property I. If τ maps the set of all minimal projectors of $\mathcal A$ cuto the set of all minimal projectors of $\mathcal B$, then τ maps $\mathcal A$ onto $\mathcal B$.

Theorem 6: A *-algebra is a type I_d algebra if and only if it is *-isomorph to a certain algebra $\mathcal{L}'(J_t, \iota \in \mathcal{T})$.

According to theorem 6 the centre of a type I_d algebre is a discrete one, i.e., it is generated by its own minimal projectors. Especially, a type I_d algebra, which is to an algebra of bounded operators isomorphic, is a \(\mathbb{V}^4 \)—algebra with discrete centre.

2. Algebras with property I.

To prove the theorems we need some further insight in the considered class of algebrus.

Theorem 7: For every *-algebra with property I the following statements are true:

- If p is a minimal projector, then there exists a
 positive linear form f with
- (6) pap = f(a) p for all a est
 - 2) If A contains only one minimal projector p., then p. is the identity element of A and A is isomorphic to the algebra of complex numbers.

We beginn with the second assertion. For every non-zero a. A the left ideal Aa contains a minimal projector p. The case Aa = 0 can be excluded, because in this situation or and the zero form a left ideal, that has to contain a minimal projector and this is impossible. Now there is an element a with a = a'p. and thus (a-a')p. =c . By the same reasoning a-a'= bp, and from p. = p it follows a = a'. So we see ap = a , p a = a for all a d and p is the identity of A . For every as A there should be a complex number λ such that α - λp_p is not inversible. It follows a = \ \ \ \ because otherwise A (a - \ \ \ \ \ \) > \ \ wich contradicts the assumption that λ belongs to the spectrum of α . The second assertion of the theorem is now available and the first assertion becomes obvious: The subalgebra b. Ar - A. where P is a minimal projector of A , has to satisfy property I too. In virtue of the minimality of p , no projector different from p is in \mathcal{A} . Therefore, \mathcal{A} . is isomorphic to the algebra of complex numbers and pap = f(a)p with some number f(m). Clearly, f depends linearly on a and

page of p has to be a positive element of \mathcal{A} . Hence is a positive linear form.

The property (6) is an essential characteristicum of minimal projectors for property I algebras. This shows

Theorem 8: Let A be a -algebra. Denote by M(A) the set of all such projectors p of A for which (6) is fulfilled with a certain linear form #.

A has property I if and only if

implies $\alpha = 0$ in \mathcal{A} .

The proof proceeds in two steps. Firstly we need Lemma 1: $\pi(A)$ consists of minimal projectors of A. From pap=f(a)p for all a 4 and $f(b^2b)$ to we have

(7)
$$q = bpb^4/f(b^4b) \in \mathfrak{M}(A)$$

and

(8)
$$q \alpha q = \frac{f(b^a b)}{f(b^a b)} \cdot q$$

We see this in the following way: pe M(A) and pq = q implies $\{(\vec{q}) p = p\vec{q}p = \vec{q}p = \vec{q}$ for projectors \vec{q} and thus $p = \tilde{q}$. Therefore $\mathfrak{M}(\mathcal{A})$ consists of minimal projectors only. The other part of the lemma is a straight-forward application of equ. (6).

We can now be sure that m(4) consists of all minimal projectors if A has property I . In this case A 2 Ap with a certain be M(A) for a given ato and we get ba = p . Now f(pba) +0 implies by positivity & (bpb) #0 and we obtain bpbabpb=bab #0. According to lemma 1 it is q . Lobe M with some A and 10.4+0 . To prove the other part of the theorem 8 we choose an element a * o out of a given left tdeel } . According to the assumption we can find $p \in M$ with $p = p \neq 0$. By (6)

one shows $f(\alpha) \neq 0$ and the positivity of f implies $\chi^* \cdot f(\alpha^*) \neq 0$. Now $g \cdot \lambda \circ f(\alpha \cdot f) = 0$ shows that g contains the minimal subjiced $\mathcal{A}g$ and theorem 8 in proved.

As a consequence of theorem 8, every *-algebra with property I is a reduced one [3].

Theorem 8 implies theorem 4 in virtue of Lemma 2: Let $A = \mathcal{L}(\mathcal{I}_t, t \cdot \mathcal{I})$. For every $\{e \in \mathcal{I}_t, (f_t, f_t) = 1\}$ the element (px)(t') = 0, $t \cdot t'$ $(px)(t) \cdot \gamma_* = (f_t, \gamma_t) \cdot f_t$, $\gamma_* \in \mathcal{I}_t$

is a minimal projector and there are no other minimal projectors in $\vec{\mathcal{A}}$.

Indeed, every projector \mathbf{q} of \mathcal{A} defines new projectors by $\mathbf{q}(t) = \mathbf{q}_t(t)$, $\mathbf{q}_t(t') = \mathbf{0}$ for t + t'. \mathbf{q}_t is smaller than \mathbf{q} and if \mathbf{q} was minimal and $\mathbf{q}_t + \mathbf{0}$ then $\mathbf{q} = \mathbf{q}_t$. One sees that \mathbf{q}_t projects \mathcal{T}_t onto a one-dimensional subspace of \mathcal{T}_t provided \mathbf{q}_t is a minimal projector. On the other hand, every one-dimensional subspace of \mathcal{T}_t defines its projector and this projector is a minimal one.

Let us mention two further properties of $\mathcal{L}'(\mathcal{J}_{t},t\in T)$. For every pair of projectors $p,q\in M$ we distinguish two possibilities: Either they project into the same or in different \mathcal{J}_{t} . Let us denote by \mathcal{M}_{t} the set of all minimal projectors that are defined according to lemma 2 by the subspaces of \mathcal{J}_{t} . Then \mathcal{M}_{t} is the union of the \mathcal{M}_{t+1} teT and $\mathcal{M}_{t} \wedge \mathcal{M}_{t'}$ is empty for $t \Rightarrow t'$. One immediately sees that two projectors belong to the same \mathcal{M}_{t} if and only if there is an \mathbf{Q}

with page. Of course, the later condition can be axtended to an arbitrary property I algebra, the proof of this fact is evident.

Lemma 3: Let 4 be a Lalgebra with property I. There is an index set T and a decomposition of m() in disjunct sets M.(4), t∈T such, that q.p∈M(4) belong to the same t if and only if there is an and with pagto. Now suppose q bp $\neq 0$ for $q, p \in \mathfrak{M}_{\epsilon}(\mathcal{A})$. The element d=qhsatisfies Apd = qbpbq = Aq and A +0 , for A is reduced and $\lambda q = (qbp)(qbp)^*$. This gives Lemma 4: p.q. (4) if and only if there is a positive linear form f and an element be A such, that

3. Representations.

Let

equ. (7) and (8) are valid.

be a *-representation of the *-algebra A with domain of definition J_{τ} . If $g \in \mathcal{R}(\mathcal{A})$ and $r(g) \neq 0$, then the functional q defined by qq=q'a) c is a vector state of γ . Indeed, for $\overline{\Phi} \in \overline{U}_{\tau}$ and $\widehat{\Psi} = \tau(q) \Phi + 0$ we have $\langle \vec{T}, \tau(\mathbf{a}) \vec{T} \rangle = g(\mathbf{a}) \langle \vec{T}, \vec{T} \rangle$. If now (7) and (8) is valid for the projector $p \in \mathcal{M}(\mathcal{A})$, we conclude $\tau(p) \neq 0$ and with fas defined by (6) we have $\langle T, \tau(\alpha) T \rangle = f(\alpha) \langle T, T \rangle$ with a vector $\Psi'=\pi(p)\Psi'$. Now $\pi(p)$ is a projector and hence

ror all **4**、. Setting **5**。 子 wo get 9(*) * パナ・ナッド/(理)/(理)

and the equality sign holds for Ψ' - $\tau(P)$ \mathcal{T} .

Theorem 9: For any P. 9 = M(A) and

(10) pap = f(a)p , qu q = g(a)q , a & A

every *-representation r of A with r(p) +0 satisfies

(11)
$$g(p) = f(p) = \sup_{(X,Y)(Y,Y)} \frac{|(Y,Y)|^2}{(X,Y)(Y,Y)}$$

where the supremum runs over all $\Psi_t \Psi^t \mathcal{J}_{\mathbf{r}}$ with the restriction

(12) \(\tau(p)\T = \T' \)

We are now in the position to show theorem 5. Let \mathcal{A} be a *-algebra with property I. With T we denote the index set given by lemma 3. For every $t \in \mathsf{T}$ we choose $\mathsf{P}_t \in \mathsf{M}_t(\mathcal{A})$ and define f_t by $\mathsf{P}_t \cap \mathsf{P}_t = \mathsf{f}_t(\bullet) \, \mathsf{P}_t$. Let us now perform the GNS-representation T_t of \mathcal{A} determined by f_t with domain of definition \mathcal{D}_t and cyclic vector $\mathsf{f}_t \in \mathsf{J}_t$, $\mathsf{f}_t(\mathsf{a}) = (\mathsf{f}_t, \mathsf{f}_t(\mathsf{a}), \mathsf{f}_t(\mathsf{a}))$. It is $\mathsf{T}_t(\mathsf{P}_t) \mathsf{f}_t = \mathsf{f}_t$. If for some $\mathsf{f}_t \in \mathcal{J}_t$ we have $\mathsf{T}_t(\mathsf{f}_t) \mathsf{f}_t = \mathsf{f}_t$, then $\mathsf{T}_t(\mathsf{P}_t) \mathsf{f}_t = \mathsf{T}_t(\mathsf{P}_t) \mathsf{f}_t$ and with the help of (6) we find f depending linearly on f_t . This shows that $\mathsf{T}_t(\mathsf{P}_t)$ is a one-dimensional projector. The same conclusion can be drawn for every $\mathsf{T}_t(\mathsf{f}_t)$ with $\mathsf{f}_t \in \mathsf{M}_t(\mathcal{A})$ by similar arguments. Lemmata 1 and 4 now indicate a one-to-one correspondence between $\mathsf{M}_t(\mathcal{A})$ and the set of all one-dimensional subspaces of \mathcal{J}_t .

Hence the vectors (12) form one-dimensional spaces and one. (12) is valid without performing the operation "sup" ! We construct the direct sum τ of the representations τ_{ϵ} , $t \in T$, and the result is a *-isomorphism of \mathcal{A} into $\mathcal{L}^{t}(\mathfrak{F}_{\epsilon}, t, \tau)$ with properties required by theorem 5. We consider now a second *-representation $\tilde{\tau}$ into $\tilde{\mathbf{L}}^{t}(\tilde{\mathfrak{F}}_{\epsilon}, t, t^{T})$ with the same properties. Then the one-dimensional subspaces of \mathfrak{D}_{ϵ} and $\tilde{\mathfrak{F}}_{\epsilon}$ are given by $\tau_{\epsilon}(\mathfrak{F}_{\epsilon})$ $\tilde{\mathfrak{D}}_{\epsilon}$ and $\tilde{\tau}(\mathfrak{F}_{\epsilon})$ $\tilde{\mathfrak{D}}_{\epsilon}$ and

there is a one-to-one correspondence
(13)
$$\widetilde{\tau}(\mathbf{p}_{i})\widetilde{\lambda}_{i} \leftrightarrow \tau(\mathbf{p}_{i})\lambda_{i}$$

As proved above, the transition probabilities between one-dimensional subspaces remain unchanged by the mapping (13). Applying a theorem of Wigner [4] there is a unitary or antiunitary one-to-one mapping $\mathbf{U}_{\mathbf{t}}$ from $\hat{J}_{\mathbf{t}}$ onto $\widetilde{J}_{\mathbf{t}}$ with

Considering now with the help of (14)the validity of

 $\widehat{\tau}(q)\left\{\widehat{\tau}(\alpha)u_t-u_t\tau(\alpha)\right\}\tau(q) = \left\{\widehat{\tau}(q\alpha q)u_t-u_t\tau(q\alpha q)\right\} = 0$ for every minimal projector q we get

Applying this to id too, one proves linearity of α . By this way we have not only proved theorem 5 but also a generalisation of theorem 1. Indeed, let $\mathcal{A} \circ f^+(\lambda_{\epsilon}, \epsilon \circ T)$,

au the identic automorphism and $\widehat{\tau}$ a sisomorphism onto $\mathcal{L}^t(\widetilde{\mathcal{S}}_{\epsilon,t}\epsilon T)$. There is a unitary map u of the direct sum of all $\widehat{\mathcal{S}}_{\epsilon}$ which impliments $\widetilde{\tau}$.

The last part of the proof of theorem 5 contains the following statement:

Theorem 10: Let τ be a *-isomorphism of $\mathcal{L}'(\mathcal{S}_{\epsilon'}, \epsilon' \epsilon \widetilde{\mathcal{T}})$ onto $\mathcal{L}''(\widetilde{\mathcal{S}}_{\epsilon'}, \epsilon' \epsilon \widetilde{\mathcal{T}})$. Then there exists a unitary map u from $\Sigma \mathcal{S}_{\epsilon_1} \epsilon \epsilon \mathcal{T}$ onto $\Sigma \widetilde{\mathcal{S}}_{\epsilon'}, \epsilon' \epsilon \widetilde{\mathcal{T}}$ and a map j from \mathcal{T} onto $\widetilde{\mathcal{T}}$ with $u \mathcal{S}_{j,\epsilon'}$

and

Theorem 10 implies the theorems 1 and 2 and shows how to prove theorem 6: We have to consider an imbedding

 $A = L^*(B_t, t:T) \leq L$ with m(A) = m(B). Theorem 5 tells us, that we need to consider the case

 $\mathcal{A} = \mathcal{L}^*(\mathcal{S}_{\epsilon}, \epsilon \in T)$ s $\mathcal{L}^*(\widetilde{\mathcal{S}}_{\epsilon}, \epsilon \in T) = \mathcal{L}$, $m(\mathcal{A}) = m(\mathcal{L})$ only. Further, \mathcal{A} and \mathcal{L} have to be *-isomorph (theorem 5) and hence there is a *-isomorphism from \mathcal{L} onto \mathcal{A} , i.e., into \mathcal{L} that leaves stable the set of all minimal projectors as a whole. This *-isomorphism has therefore to be an *-automorphism and it follows $\mathcal{L} = \mathcal{A}$.

4. Proof of theorem 3.

Let φ be a derivation of $\mathcal{L}'(\mathcal{S})$. Using an idea of P.Kräger we construct the element X of eq. (4) explicitely. For any two vectors ξ, η of \mathcal{S} we define $P_{\xi, \eta}$ by

Now & Pin is a linear map of a into L(B) and we have apy. Pas, n for all a. L'(1). Now we define

xy = 9(Pms) &

and get a linear map $\eta \to r \gamma$ from ${\mathcal J}$ into ${\mathcal J}$. Now

is a map of I into I for every at L (I) and

9, (α) 7 = 9(Pan, ξ) ξ - α 9(Pn, ξ) ξ = { γ(α pn, ξ) - α φ(Pn, ξ)} ξ shows that

Hence $\varphi = \varphi$, Substituting $\alpha = P_{\eta, \xi}$ we get $\langle \xi, x, \xi \rangle = 0$ Next we consider *(a) = *p(a*)* . * is again a derivation and we construct as above y7 = 9(2,) so that 4(a) = [y,a] and

we obtain with ({ , x { } } = ({ } , y , { }) = 0 Choosing y = } , a = Par ⟨Yō,n,⟩ = - ⟨ō,×n,>.

Now y maps \mathcal{J} into \mathcal{J} and $x^+ = -y$ so that $x,y \in \mathcal{L}'(\mathcal{S})$ and the theorem is proved.

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Адреса

Письма по всем вопросам обмена публикациями, а также запросы на отдельные издания следует направлять по адресу:

> 101000 Москва, Главный почтамп, п/я 79. Издапельский опдел Объединенного инспипупа ядерных исследований.

Адрес для посылки всех публикаций в порядке обмена, а также для бесплатной подписки на научные журналы:

101000 Москва, Главный почтамт, п/я 79. Научно- техническая библиотека Объединенного института ядерных исследований.

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