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Weak Interactions of Charmed Particles

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## WEAK INTERACTIONS OF CHARMED PARTICLES

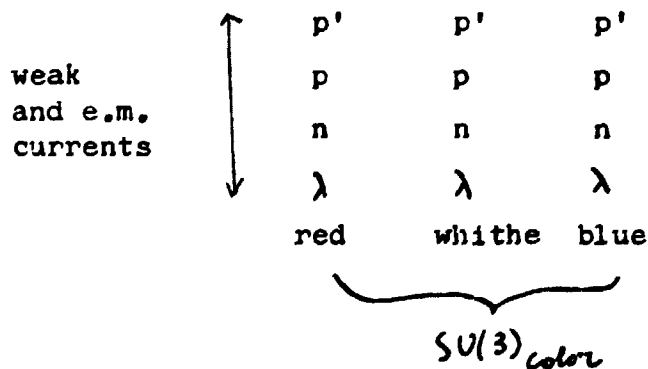
Subject of my talk will be an illustration of the expected features of weak production and weak decays of charmed particles.

There are at present various proposed models where, in formulating a theory of weak interactions, new hadronic degrees of freedom are introduced, leading to a new class of elementary particles (charmed particles). Time forbids me to make a survey of the various options available, and forces me to consider only one particular model, the one based on four fractionally charged colored quarks.

This is the simplest available model and also the most developed at the moment. Predictions derived in this model will provide, hopefully, useful guides to the experimental search for charm that we are witnessing in these days.

### 1. Four quarks make SU (4)

Mesons and baryons are assumed to be made out of four types of quarks <sup>(1,2)</sup> each type coming in three different colors <sup>(3)</sup>:



Weak and e.m. currents are assumed to be bilinear in quark fields, and color singlets. Hence weak and e.m. interactions are exactly invariant under the  $SU(3)$  color symmetry which could be associated to gauge fields mediating strong interactions. The natural symmetry of this scheme is  $SU(4) \otimes SU(3)_{\text{color}}$ . This symmetry could be further enlarged to include chiral transformations and/or embedded into a larger simple algebra, perhaps including leptons (4). This will not be discussed here.

Quantum numbers of the different quark types, relevant to a discussion of weak interactions, are assigned as shown in Table 1. If one further defines for all quarks :

$$B = \text{baryon number} = 1/3$$

the extension of the Gell-Mann-Nishijima formula to include charmed particles reads :

$$Q = I_3 + \frac{1}{2} (B + C + S)$$

A basic assumption of the model is that, at least at present energies, color degrees of freedom are not being excited. All hadrons to be considered are therefore assumed to be color singlet (5). They can be classified according to the quantum numbers conserved by strong interactions:  $B, I, I_3, S, C$ . In particular particles can be classified

according to the charm content as follows :

- i - Normal ( $C = 0$ ) states : particles made out of  $p$ ,  $n$  and  $\lambda$  quarks and/or antiquarks (e.g.  $\pi$ ,  $K$ ,  $N$ ,  $\Lambda$ , etc.)
- ii - Quasi-normal ( $C = 0$ ) states: particles made out of  $p'$   $\bar{p}'$  pairs (6) (e.g.  $\psi$ ,  $\psi'$ ,  $\eta_c$  etc.)
- iii - Charmed ( $C \neq 0$ ) states<sup>(7)</sup> : states containing  $p'$  and/or  $\bar{p}'$  quarks such that  $C = (\text{number of } p') - (\text{number of } \bar{p}') \neq 0$ .

Charm being conserved in strong and e.m. interactions, a number of  $C \neq 0$  particles must be stable except for weak decays. Which charmed particles, among the partners of the low-lying SU (3) multiplets, are indeed stable, is determined by SU(4) mass breaking.

If  $\psi(3104)$  is a pure  $p'\bar{p}'$  state, there is little doubt that charmed pseudoscalar mesons should be stable.

We expect three such mesons<sup>(8)</sup> (plus their antiparticles):

$$\left. \begin{array}{l} D^0 (p'\bar{p}) \\ D^+ (p'\bar{n}) \\ S^+ (p'\bar{\lambda}) \end{array} \right\} \begin{array}{l} S=0, I=1/2 \\ \\ S=1, I=0 \end{array} \left. \vphantom{\begin{array}{l} D^0 \\ D^+ \\ S^+ \end{array}} \right\} \begin{array}{l} \text{representation } \bar{3} \\ \text{of SU (3)} \end{array}$$

Estimates of their masses, using  $\psi$  mass to determine  $P'$  mass, have been performed by various authors, and give values around 2 GeV.

Together with the pseudoscalar octet, pseudoscalar charmed mesons are naturally assigned to the regular (15-dimensional) representation of  $SU(4)^{(8)}$ . Spin  $1/2^+$  charmed baryons ( $C = 1$  and 2) are assigned, together with the baryon octet, to a 20-dimensional  $SU(4)$  representation  $^{(2)}$ . We shall restrict to  $C = 1$  states which can be classified in  $SU(3)$  according to:

$$\begin{array}{l}
 C = +1 \left\{ \begin{array}{l}
 \left. \begin{array}{l}
 B^+ (P' P^n)_A \\
 B^0 (P' \lambda n)_A \\
 B^+ (P' \lambda P)_A
 \end{array} \right\} \begin{array}{l}
 S = 0, \quad I = 0 \\
 S = -1, \quad I = 1/2
 \end{array} \right\} \begin{array}{l}
 \text{representation} \\
 \bar{3} \text{ of } SU(3)
 \end{array} \\
 \\
 \left. \begin{array}{l}
 B^0 (P' n m)_S \\
 B^+ (P' P m)_S \\
 B^{++} (P' P P)_S
 \end{array} \right\} \begin{array}{l}
 S = 0, \quad I = 1 \\
 \\
 \\
 \end{array} \right\} \begin{array}{l}
 \text{representation} \\
 6 \text{ of } SU(3)
 \end{array} \\
 \\
 \left. \begin{array}{l}
 B^0 (P' \lambda m)_S \\
 B^+ (P' \lambda P)_S
 \end{array} \right\} \begin{array}{l}
 S = -1, \quad I = 1/2
 \end{array}
 \end{array}
 \end{array}$$

The subscript A(S) denotes antisymmetry (symmetry) of the wave function under exchange of the uncharged quarks. We shall assume in the following that the  $\bar{3}$  baryons are stable except for weak decays. This results from the analysis of ref. (9) for the case of quadratic mass formulae, and also from ref. (10). The sextet baryons should be able to decay into the others by pionic and/or e.m. transitions.

Masses of  $\bar{3}$  baryons are estimated to be of order of  $2.9 \div 3$  GeV in ref. (9) and  $2.2 \div 2.4$  GeV in ref. (10). Spin  $3/2^+$  baryons, assigned to another 20-dimensional SU(4) representation <sup>(2)</sup> together with the  $3/2^+$  decuplet, are presumably unstable against strong decays.

2. - Fundamental weak interactions

The four quark scheme allows for a very elegant and consistent description of weak interactions<sup>(2)</sup>.

Quarks couple to charged (W) and neutral (Z) intermediate bosons according to :

$$\mathcal{L}_W = g (J_\mu W^\mu + h.c.) - g_0 J_\mu^{(0)} Z^\mu \quad (1)$$

The neutral current,  $J_\mu^{(0)}$ , has  $\Delta S = \Delta C = 0$  and does not play any significant role in weak production and decay of charmed particles. The charged current  $J_\mu$  is given by :

$$J_\mu = \sum_{\text{colors}} \left[ \bar{p} \gamma_\mu (1 - \gamma_5) (\cos \theta n + \sin \theta \lambda) + \bar{p}' \gamma_\mu (1 - \gamma_5) (-\sin \theta n + \cos \theta \lambda) \right] \quad (2)$$

where  $\theta$  is the Cabibbo angle. As implied by the sum over colors  $J_\mu$  is a color singlet.  $J_\mu$  has a  $\Delta C = 0$  part which coincides with the familiar Cabibbo current, and an additional  $\Delta C \neq 0$  term which describes the coupling of  $p'$  to  $n$  and  $\lambda$  quarks. Note that  $p$  and  $p'$  couple to two orthogonal combinations of  $n$  and  $\lambda$ . This property assures the suppression of unobserved  $\Delta C = 0, \Delta S \neq 0$  neutral transition (e. g.  $K_L \rightarrow \mu^+ \mu^-$ ).

The  $\Delta C \neq 0$  term implies the following selection rules for semi leptonic transitions :

- large ( $\cos \theta$ ) component :  $\Delta S = \Delta C \neq 0, \Delta I = 0; \Delta Q = \Delta C \quad (3)$



- small ( $\sin \theta$ ) component :  $\Delta S = 0$ ,  $\Delta I = 1/2$  ;  $\Delta Q = \Delta C$  (4)

Weak non leptonic processes arise from emission and reabsorption of a virtual W and/or Z (Fig. 1). Again, to describe charm-changing processes, only charged currents need to be considered, and the resulting current x current hamiltonian has the structure:

$$\begin{aligned}
 H_{\text{eff}}^{\Delta C \neq 0} &\sim T(J J^+)_{\Delta C \neq 0} \sim \cos^2 \theta (\bar{P}' \lambda)(\bar{n} P) - \\
 &- \sin \theta \cos \theta [(\bar{P}' n)(\bar{n} P) - (\bar{P}' \lambda)(\bar{\lambda} P)] - \\
 &- \sin^2 \theta (\bar{P}' n)(\bar{\lambda} P) + \text{h.c.}
 \end{aligned}
 \tag{5}$$

We have used the abbreviated notation :

$$(\bar{P}' \lambda) \equiv \sum_{\text{colors}} \bar{P}'_{\mu} (1-\gamma_5) \lambda \quad \text{etc.}$$

summation over the Lorentz indices of currents is understood.

It follows from eq. (5) that the dominant transitions (i.e. those proportional to  $\cos^2 \theta$ ) obey the selection rules<sup>(11)</sup>:

$$\Delta C = \Delta S$$

$$\Delta I = 1$$

$$SU(3) = \bar{6} \oplus 15 + \text{h.c.}$$

we shall consider here only dominant transitions, leaving for the future the study of rare ( $\sim \sin \theta$  in amplitude) and super-rare

(  $\sim \sin^2 \theta$  ) non leptonic decay modes of charmed particles. In Sect.4 we shall discuss a further selection rule (sextet dominance) which arises in these processes as counterpart of the well known octet dominance in non leptonic strange particle decays.

3. - Neutrino and antineutrino production of charmed particles.

Charmed particles can be singly produced by the  $\Delta C \neq 0$  term of the current, eq. (2), in the processes :

$$\begin{aligned} \nu &+ (\text{Matter}) \rightarrow \mu^- + \text{anything} \\ \bar{\nu} &+ (\text{Matter}) \rightarrow \mu^+ + \text{anything} \end{aligned} \quad (7)$$

Charmed particle production by neutrinos has been studied in ref. (12) and (13).

We shall consider these processes in the deep inelastic region,  $E_\nu$  large with fixed  $x$  and  $y$  :

$$x = -q^2 / 2M \nu$$

$$y = \nu / E_\nu$$

$E_\nu$  = neutrino or antineutrino lab-energy,  $\nu = (q \cdot p)$ ,  $M$  = nucleon mass,  $P$ , and  $q$  being defined in Fig. 2. If we call  $W$  the invariant mass of the produced hadronic system, then:

$$W^2 - M^2 = 2 M E_\nu y(1-x) \quad (8)$$

At fixed values of  $E_\nu$ , charmed particles can be produced for  $W$  larger than a fixed, threshold value ( $W_{th}$ ), i.e. in region II of Fig. 3. Across the line  $W = W_{th}$  there will be an increase of the cross-section, producing a "charm ridge". As  $E_\nu$  increases the line

$W = W_{th}$  moves into region I, and region II increases.

A quantitative analysis of these non scaling effects can be done in the parton model assuming that scaling holds both in region I and II (i.e. assuming a sharp ridge) the difference in cross-sections arising from the possibility of charm changing reactions in region II.

To obtain cross sections in region I and II we recall that in the quark-parton model <sup>(14)</sup>, the cross-section is a sum of cross-sections for elementary processes where a parton quark (or antiquark) "a" absorbs a  $W^+$  or  $W^-$  and transforms into a quark (or antiquark) "b".

We denote by  $a(x)$  the average number of type "a" partons inside a proton, with a fraction  $x$  of proton momentum, and by  $g_{ab}$  the coupling of  $a\bar{b}$  to the weak boson  $W$ . The  $V - A$  structure of the interaction implies then the following contributions to the cross-section for  $\nu$  or  $\bar{\nu}$  scattering off protons:

$$i) \quad \nu + a \rightarrow \mu^- + b : \left( \frac{d\sigma}{dx dy} \right)_{a \rightarrow b}^{\nu, P} = \frac{G^2 M E_\nu}{\pi} g_{ab}^2 x a(x) \cdot \begin{cases} 1 & \text{(a and b are quarks)} \\ (1-y)^2 & \text{(a and b are antiquarks)} \end{cases}$$

$$ii) \quad \bar{\nu} + a \rightarrow \mu^+ + b : \left( \frac{d\sigma}{dx dy} \right)_{a \rightarrow b}^{\bar{\nu}, P} = \frac{G^2 M E_\nu}{\pi} g_{ab}^2 x a(x) \cdot \begin{cases} (1-y)^2 & \text{(a and b are quarks)} \\ 1 & \text{(a and b are antiquarks)} \end{cases}$$

To obtain cross-section off neutrons, simply exchange  $n \leftrightarrow p$ ,  $\bar{n} \leftrightarrow \bar{p}$  leaving all other terms unchanged; the cross-sections per nucleon off  $I = 0$  matter are then obtained by averaging proton and neutron cross - sections. Table 2 illustrates the elementary transitions for  $\nu$  and  $\bar{\nu}$  reactions below charm threshold with the corresponding values of  $g_{ab}^2$ . The resulting cross-sections per nucleon in region I, are therefore :

$$\left(\frac{d\sigma}{dx dy}\right)_I^\nu = \frac{G^2 M E_\nu}{\pi} \chi \cdot \left\{ [n(x) + p(x)] \cos^2 \theta + 2 \lambda(x) \sin^2 \theta + (1-\gamma)^2 [\bar{p}(x) + \bar{n}(x)] \right\} \quad (9)$$

$$\left(\frac{d\sigma}{dx dy}\right)_I^{\bar{\nu}} = \frac{G^2 M E_\nu}{\pi} \chi \cdot \left\{ [\bar{n}(x) + \bar{p}(x)] \cos^2 \theta + 2 \bar{\lambda}(x) \sin^2 \theta + (1-\gamma)^2 [n(x) + p(x)] \right\} \quad (10)$$

Charm changing reactions which contribute in region II are displayed in Table 3. The resulting increase in cross-sections is :

$$\Delta \left(\frac{d\sigma}{dx dy}\right)_I^\nu = \frac{G^2 M E_\nu}{\pi} \chi \cdot \left\{ [n(x) + p(x)] \sin^2 \theta + 2 \lambda(x) \cos^2 \theta + (1-\gamma)^2 2 \bar{p}'(x) \right\} \quad (11)$$

$$\Delta \left( \frac{d\sigma}{dx dy} \right)^{\bar{\nu}} = \frac{G^2 M E_\nu}{\pi} x \cdot \left\{ [\bar{n}(x) + \bar{p}(x)] s \cdot \cos^2 \theta + 2 \bar{\lambda}(x) \cos^2 \theta + (1-y)^2 2 p'(x) \right\} \quad (12)$$

Electroproduction data, as well as low energy neutrino data from Gargamelle and FNAL seem to support the following qualitative features of distribution functions<sup>(15)</sup>:

- i)  $n(x)$  and  $p(x)$  are large, rather well determined and extend to large values of  $x$ ; they receive contributions from leading (valence) quarks;
- ii)  $\bar{n}, \bar{p}, \lambda, \bar{\lambda}$  and  $p', \bar{p}'$ , seem to be concentrated at small  $x$ ; they are much less known, theoretical arguments suggesting  $\bar{n}(x) = \bar{p}(x)$ ,  $\lambda(x) = \bar{\lambda}(x)$ ,  $\bar{p}(x) = p'(x)$ , and perhaps  $\lambda(x) = \bar{n}(x)$  (SU(3) limit). Such distributions are thought to arise from a sea of neutral  $q\bar{q}$  pairs.

We may now discuss the cross-sections for charmed particle production, eq.s (11) and (12).

In neutrino reactions, eq. (11), we have two different components.

The term proportional to  $n(x) + p(x)$  has the following features:



The antineutrino cross-section, eq. (12), receives only sea contributions, with features identical to the second component of the neutrino cross-section.

In all cases, the  $C \neq 0$  final state could undergo a semileptonic decay, with emission of a  $\mu\nu$  or  $e\nu$  pair.

Dimuon events are thus expected <sup>(16)</sup>. The  $\Delta C = \Delta Q$  rule in semileptonic transitions, eq. (3), implies only the following charge combinations to be present :

$$\begin{array}{ll} \mu^- \text{ leading, } \mu^+ & (\nu^- \text{ reactions}) \\ \mu^+ \text{ leading, } \mu^- & (\bar{\nu}^- \text{ reactions}) \end{array}$$

the most energetic (leading) muon originating from the primary interaction.

The ratio of dimuon events versus single muon events is related to the total charm-changing cross-section and to the semileptonic branching ratio according to :

$$\frac{D}{S} = \frac{(\text{dimuon rate})}{(\text{single muon rate})} = \frac{\Delta\sigma}{\sigma} \cdot B_{\mu} \quad (13)$$

$$B_{\mu} = \frac{\Gamma(C \rightarrow \mu + \nu + \dots)}{\Gamma(C \rightarrow \text{anything})} \quad (14)$$

Using eqs (9) to (12) and neglecting non leading with respect to leading quark contributions we find :



$$\frac{\Delta\sigma^v}{\sigma^v} \approx \sin^2\theta + 2 \frac{\langle\lambda\rangle + \frac{1}{3}\langle\bar{P}'\rangle}{\langle n+P\rangle} \quad (15)$$

$$\frac{\Delta\sigma^{\bar{v}}}{\sigma^{\bar{v}}} \approx 6 \frac{\langle\bar{\lambda}\rangle + \frac{1}{3}\langle P'\rangle}{\langle n+P\rangle} \approx 3 \left( \frac{\Delta\sigma^v}{\sigma^v} - \sin^2\theta \right) \quad (16)$$

where we have set :  $\langle a \rangle = \int dx \ x a(x)$  = average momentum carried by parton "a".

Using an explicit parton model of nucleons, fitted to SLAC and Gargamelle data, the authors of ref (13) have estimated (17):

$$\frac{\Delta\sigma^v}{\sigma^v} \sim 15\% \quad ; \quad \frac{\Delta\sigma^{\bar{v}}}{\sigma^{\bar{v}}} \sim 30\%$$

Anticipating a branching ratio  $B_{\mu} \sim 5\%$  (see next section) one obtains :

$$\frac{D}{S} \sim 1\%$$

which is of the order of the ratio observed by the Harvard - Pennsylvania - Wisconsin group at FNAL, and presented at this Conference.

#### 4. Weak decays of charmed particles

As discussed in Sect 1, lowest lying charmed particles decay weakly into normal hadrons, with or without emission of a lepton pair. We shall discuss here two points : i) ratio of semileptonic to non leptonic decay rates ( $B_{\mu}$  as defined in eq. (14)); ii) the structure of non leptonic amplitude.

To this aim, we shall use the results on the structure of non leptonic amplitudes recently obtained in ref (18) and (19). The picture which emerges can be summarized as follows;

- i) non leptonic amplitudes arise from virtual W-exchange, Fig. 1;
- ii) the leading part of the amplitude depends upon the behaviour of the product  $J_{\mu}(x) J_{\nu}^{\dagger}(0)$  at short space time distance <sup>(20)</sup>, ( $x^2 \sim \frac{1}{M_W^2}$ , much smaller than typical hadronic length scale)
- iii) if strong interactions are asymptotically free, the short distance behaviour of  $J_{\mu}(x) J_{\nu}^{\dagger}(0)$  can be computed, and the result, in the SU (4)  $\times$  SU (3) color model, is that a term in the product is enhanced, corresponding to the component over a 20-dimensional SU(4) representation;
- iv) the enhanced term is a superposition of a  $\Delta C = 0$ , pure octet

(leading to octet dominance in strange particle decays) and a  $|\Delta C| = 1$  term transforming under SU(3) as a  $6 \oplus \bar{6}$  representation. Thus we expect charmed particle non leptonic decays to exhibit the same enhancement as  $\Delta I = 1/2$  strange particle non leptonic decays.

This leads to the estimate (21,7):

$$\frac{B}{\mu} = \frac{\Gamma(C \rightarrow \mu + \nu + \dots)}{\Gamma(C \rightarrow \text{anything})} \sim 1 \div 10 \% \quad (15)$$

Moreover if the effective hamiltonian transforms as a component of an SU(3) sextet, we can replace eq. (6) with the more restrictive selection rules (21) (to order  $\cos^2 \theta$ ):

$$\begin{aligned} \Delta C &= \Delta S \\ \Delta I &= 1 \\ \Delta V &= 0 \\ \text{SU}(3) &= 6 \oplus \bar{6} \end{aligned} \quad (16)$$

where the V-spin is the SU(3) (and SU(4)) subgroup which mixes  $\lambda$  and  $p$  quarks, leaving unchanged all the others.

Eq. (16) leads to selection and intensity rules, which I will briefly summarize.

#### Meson decays

From  $\Delta V = 0$ , we get the equalities (valid up to SU(3) breaking in phase space)

$$\begin{aligned} \sum \Gamma(D^0 \rightarrow 2PS) &= \sum \Gamma(S^+ \rightarrow 2PS) \\ \sum \Gamma(D^0 \rightarrow 3PS) &= \sum \Gamma(S^+ \rightarrow 3PS) \\ \sum \Gamma(D^0 \rightarrow V+PS) &= \sum \Gamma(S^+ \rightarrow V+PS) \\ &\text{etc.} \end{aligned}$$

$$\Gamma_{\text{total}}(D^0) = \Gamma_{\text{total}}(S^+)$$

ps and V indicate C = 0 pseudoscalar and vector mesons, and sums run over all allowed channels of the given kind.

Sextet dominance implies also :

$$D^+ \rightarrow \bar{K}^0 \pi^+$$

which is the counterpart of the rule  $K^+ \rightarrow \pi^+ \pi^0$  implied by  $\Delta I = 1/2$  enhancement. Further relations among two body and three body decay amplitudes of  $D^{+,0}$  and  $S^+$  have been given in ref. (21).

#### Baryon decays

As anticipated in Sect. 1 we assume the  $\bar{3}$  spin  $1/2^+$  baryons to be stable. As a consequence of  $\Delta V = 0$ , again we find equalities among partial and total widths of the  $V_3 = \pm 1/2$  baryons :

$$\begin{aligned} \sum \Gamma [B^0(p' \lambda m)_A \rightarrow B + ps] &= \sum \Gamma [B^+(p' \lambda m)_A \rightarrow B + ps] \\ \Gamma_{\text{total}} [B^0(p' \lambda m)_A] &= \Gamma_{\text{total}} [B^+(p' \lambda m)_A] \quad \text{etc.} \end{aligned}$$

where B indicates a C = 0,  $1/2^+$  octet baryon. Relations for two body decay amplitudes have been studied in ref. (22).

SU(4) limit

One may investigate consequences of exact SU(4) symmetry for non leptonic decays with the aim of obtaining estimates of charmed particle lifetimes.

For the decays :  $B' (C=1) \rightarrow B (C=0) + ps$ , one can determine all relevant amplitudes from hyperon decay amplitudes<sup>(22)</sup>, and obtain estimates for  $\sum \Gamma(B' \rightarrow B + ps)$  of the order of  $10^{13} \text{ sec}^{-1}$ . It is amusing that SU(4) symmetry implies a relation among hyperon decay S-wave amplitudes<sup>(22)</sup> which reads :

$$S(\Lambda_-^0) = -\frac{1}{\sqrt{3}} S(\Sigma_0^+)$$

and is not too badly violated (l.h.s. = 1.50, r.h.s. = 0.84).

5. - Conclusion

The introduction of charm makes it possible to formulate a theory of weak interactions of great elegance and simplicity.

This theory leads to very precise predictions about weak production and weak decays of charmed particles.

The new phenomena observed in  $e^+e^-$  and neutrino collisions encourage us to think that this theory may have indeed some elements of truth. It remains now as a challenge to our colleagues experimentalists to put the idea of charm to its decisive test, by confirming or disproving the existence of charmed particles.

	Q	$I_3$	S	C
$P'$	$2/3$	0	0	1
P	$2/3$	+ $1/2$	0	0
n	$-1/3$	- $1/2$	0	0
$\lambda$	$-1/3$	0	-1	0

TABLE I

Quantum numbers of the four quarks.

	$a \rightarrow b$	$g_{ab}$
$\bar{\nu}$	$n \rightarrow p$	$\cos^2 \theta$
	$\lambda \rightarrow$	$\sin^2 \theta$
	$\bar{p} \rightarrow \bar{n}$	$\cos^2 \theta$
	$\bar{p} \rightarrow \bar{\lambda}$	$\sin^2 \theta$
$\nu$	$\bar{n} \rightarrow \bar{p}$	$\cos^2 \theta$
	$\bar{\lambda} \rightarrow \bar{p}$	$\sin^2 \theta$
	$p \rightarrow n$	$\cos^2 \theta$
	$p \rightarrow \lambda$	$\sin^2 \theta$

TABLE 2

Elementary transitions contributing to  $\bar{\nu}$  and  $\nu$  cross-section below charm threshold.

	$a \rightarrow b$	$g_{ab}^2$
$\nu$	$n \rightarrow p'$	$\sin^2 \theta$
	$\lambda \rightarrow p'$	$\cos^2 \theta$
	$\bar{p}' \rightarrow \bar{n}$	$\sin^2 \theta$
	$\bar{p}' \rightarrow \bar{\lambda}$	$\cos^2 \theta$
$\bar{\nu}$	$\bar{n} \rightarrow \bar{p}'$	$\sin^2 \theta$
	$\bar{\lambda} \rightarrow \bar{p}'$	$\cos^2 \theta$
	$p' \rightarrow n$	$\sin^2 \theta$
	$p' \rightarrow \lambda$	$\cos^2 \theta$

TABLE 3

Elementary transitions contributing to  $\nu$  and  $\bar{\nu}$  production of charmed states.



References and Footnotes

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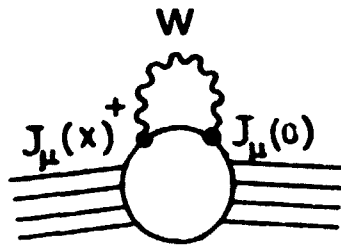


Fig.1

Virtual  $W$  exchange leading to non leptonic weak amplitudes.

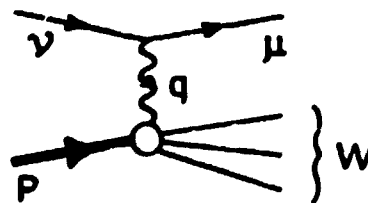


Fig.2

Inelastic scattering of neutrinos off nucleons.  $W$  is the invariant mass of the hadronic final state.

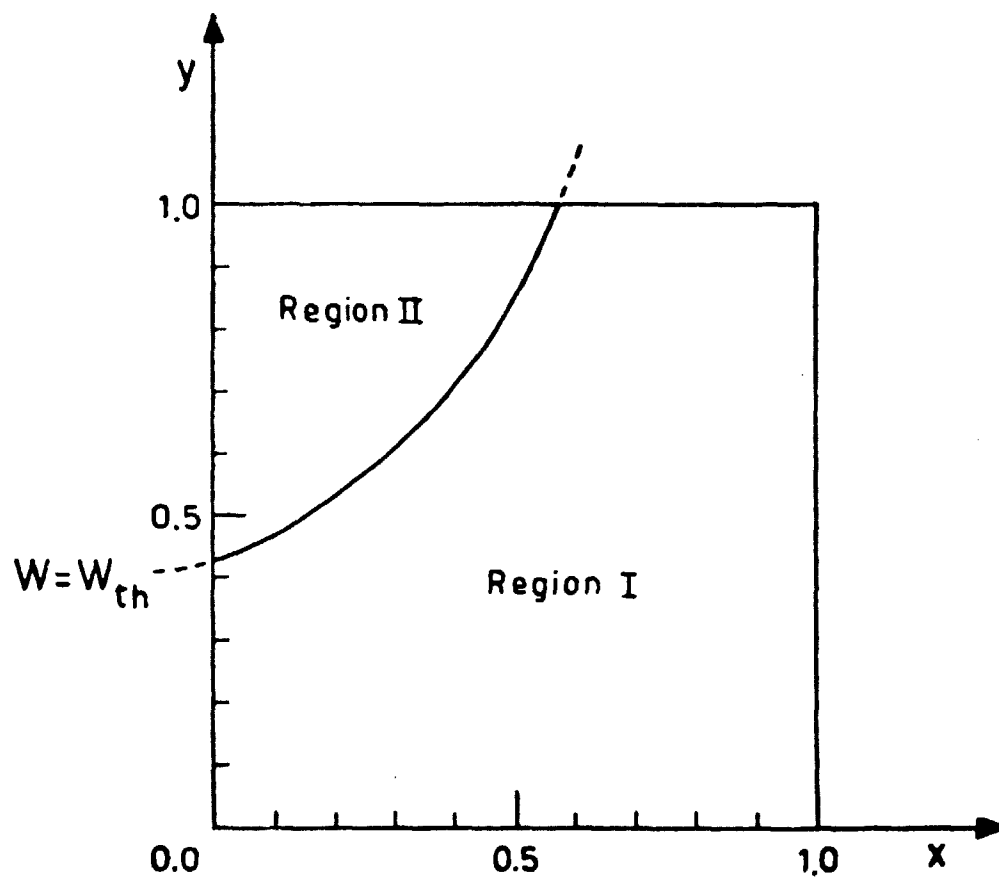


Fig. 3

Kinematical regions below (I) and above (II) charm threshold,  $W_{th}$ , in  $x, y$  variables. The curve here reported is computed for  $E = 30$  GeV, and  $W_{th} = 5$  GeV.

Riassunto - Interazioni deboli delle particelle con "charm".

Si passano in rassegna le predizioni teoriche sulla produzione da neutrini e sui decadimenti deboli delle particelle con "charm". L'analisi è fatta nell'ambito del modello basato su SU(4).

Abstract - Weak Interactions of Charmed Particles.

Theoretical predictions for weak neutrino production and weak decays of charmed particles in the SU(4) scheme are reviewed.



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