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ON THE POSSIBILITY OF UNIVERSAL DESCRIPTION OF ANGULAR DISTRIBUTION N INTERACTIONS OF HADRONS WITH NUCLEI

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ON THE POSSIBILITY OF UNIVERSAL DESCRIPTION OF ANGULAR DISTRIBUTION IN INTERACTIONS OF HADRONS WITH NUCLEI

PRÓBA JEDNOLITEGO OPISU ROZKŁADÓW KĄTOWYCH W ODDZIAŁYWANIACH HADRONÓW Z JĄDRAMI

О ВОЗМОЖНОСТИ УНИВЕРСАЛЬНОГО ОПИСАНИЯ УТЛОВЫХ РАСПРЕДЕЛЕНИЙ ВО ВЗАИМОДЕЙСТВИЯХ АДРОНОВ С ЯДРАМИ

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Summary

The validity of the hypothesis that the angular distribution of shower parsiples produced in hadron - nucleus interactions can be parametrized by the number of slow particles emitted from the struck modeus is tested. Relation between the mean number of slow particles and the mass number A of the target auclous or the corresponding average number of collisions inside the target nucleus is found.

<u>Streszczenie</u>

Zbedano możliwość parametryzacji, przy pomocy liczby cząstek powolnych amitowanych z jądra targetu, rozkładu kątowego cząstek produkowanych w oddziaływaniach hadronów z jądrami. Znalesiono zależacść pomiędzy średnią liczbą śladów powolnych, a liczbą masową A jądra targetu oraz średnią liczbą zderzeń wownątrz jądra targetu.

Pesidme

Проверяется гипотеза что угловые распределения ливневых частиц генерированных во взаимодействиях адронов с ядрами можно описать про-той функцией числа медленных частиц эмитированных ядром милени. Найдена зависимость среднего числа медленных частиц от массового числа ядра милени или от соответствующего среднего числа соударений первичной частипь в ядре мишени. It was shown in papers [1] and [2] that the angular distribution of shower particles n_s ($\beta \ge .7$) produced in proton-emulsion interactions at 67 GeV,200GeV and of the order of few thousands GeV can be parametrized using the number of heavy ionizing particles N_h ($\beta \le .7$) emitted from the struck nucleus. Our parametrization of inclusive distribution turned out to be:

$$\frac{1}{N}\frac{dms}{d\eta} = \alpha(\eta, E) + b(\eta, E) Nn \qquad (1)$$

where E stands for energy of the incoming proton and $m = -Im IOm \frac{\Theta_L}{2}$. It also turns out that pion-emulsion interactions at 60 GeV and 200 GeV obey the same linear parametrization but with different coefficients. Thus generally the angular distribution of shower particles produced in hadron-emulsion interactions can be parametrized by the following formula:

$$\frac{1}{N} \frac{\partial I_{n}}{\partial I_{n}} = O_{I}(\eta, E) + b_{I}(\eta, E) N_{h} \qquad (1)$$

where I denotes the incoming particle.

In Table I there are listed the numerical values of the coefficients s_{I} and b_{I} of formula (2) for interactions of protons and pions at the energy of 200 GeV. From formula (2) it follows immediately the well known relation between the average multiplicity \hat{n}_{e} and the number of \mathbf{R}_{h} particles:

⁴ Linear fits (eq.2)) were done for $\mathbb{R}_h \leq 20$.

$$\overline{m}_{s} = A_{r}(E) + B_{r}(E) N_{h}$$
(3)

where

$$A_{I}(E) = \int a_{I}(\gamma, E) d\gamma \quad B_{I}(E) = \int b_{I}(\gamma, E) d\gamma$$

Using the parametrization given by eq. (2) one can reproduce the angular distribution of $n_{\rm B}$ particles for a given $N_{\rm B}$ value. Pig.1 shows as an example the angular distributions of $n_{\rm B}$ particles produced in proton-emulsion interactions at 67 GeV and 200 GeV for arbitrarily chosen $N_{\rm B}$ values. From Fig.1 one can draw the following conclusions:

- 1. For a given primary proton energy there exists an angular interval $\mathcal{M} > \mathcal{M}_E$ in which , to a good approximation, the angular distribution does not depends on \mathbb{N}_h . More precisely the number of n_g tracks somewhat decreases with the increasing number of \mathbb{N}_h tracks.
- 2. With increasing primary proton energy, η_e moves towards higher values of η as the rapidity of the incident particle $(\Delta \eta_e = Im \frac{E_1}{E_2} = Im \frac{200}{67} = 1.4).$
- 3. For $\eta \leq \eta_{\rm S}$ the number of $n_{\rm S}$ tracks increases with increasing number of $N_{\rm h}$ tracks and the maximum of the angular distribution moves towards the smaller values of η .
- 4. For $\mathcal{N} \leq 1.5$ the angular distribution of n_{g} tracks does not depend on primary proton energy and is described by the number of M_{h} tracks.

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The main aim of this work is to test the validity of the hypothesis that the angular distribution of shower particles produced in hadron-nucleus interaction can be parametrized by formula (2) and that the coefficients a_I and b_I do not depend on the mass number A of the target nucleus and are the same as those found in emulsion.

Since formula (2) is linear in n_g and \overline{n}_h , it remains valid when $\overline{N_h}$ denotes the average number of slow particles emitted from the struck nucleus. Thus we shall test the validity of the formula:

$$\frac{1}{N}\frac{dns}{d\eta} = a_{r}(\eta_{i}E) + b_{I}(\eta_{i}E)\overline{N}_{h} \qquad (4)$$

In order to test our hypothesis we shall make use of the counter experiment data obtained by W.Busza et al. [3]. They analyzed the angular distribution of fast particles produced in hadron interactions with different target nuclei. Among many targets they used also nuclear emulsion. This allows a direct comparison between their and our data. In Pig.2 we present angular distributions of particles produced by 200 GeV protons and pions in interactions with nuclear emulsion as a target - one distribution is result of measurements performed in nuclear emulsion, the other obtained in the counter experiment. Except of the both ends of the \mathcal{N} distribution the agreement is very good (see Table II). Therefore in our

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analysis we shall restrict ourselves to the η interval .58< η < 5.28 .

We have adopted the following procedure of testing the validity of formula (4). Let us denote by $n(\eta_i)$ the mean number of particles in $\Delta \eta_i$ interval produced in interactions of protons or pions with a given target nucleus (experimental data obtained by W.Busza et al. [3]) and by $m_S(\eta_i)$ the number of particles given by formula (4) in the same $\Delta \eta_i$ interval. By minimizing the η^2 function with \overline{N}_h as a free parameter:

$$\chi^{2} = \sum_{\substack{0.58 < m_{1} < 5.28}} \frac{\sum m(m_{i}) - m_{s}(m_{i})]^{2}}{\sigma^{2}(m_{i}) + \sigma^{2}_{s}(m_{i})}$$
(5)

where $\mathfrak{S}(\eta_i)$ and $\mathfrak{S}_{\mathfrak{S}}(\eta_i)$ denote the errors of $\mathfrak{n}(\eta_i)$ and $\mathfrak{m}_{\mathfrak{S}}(\eta_i)$ respectively, we have found the mean values of $\overline{N_n}$ for 12 targets exposed to 200 GeV protons and pions by W.Busza et al. [3]. The reliability of our procedure is illustrated in Fig.3 where the angular distributions of 200 GeV proton and pion interactions with H_2 , C, Ag, and Pb nuclei are compared with the distributions calculated from eq. (4). The corresponding distributions coincide with each other very well (see χ^2 values in Table III). It is very striking that the same parametrization (with the coefficients s_1 and b_1 extracted from emulsion measurements) is working for nuclei as different as hydrogen and lead.

The average values of $\overline{N_h}$ as a function of the mass number A of the target nucleus obtained from the above procedure are presented in Fig.4 and Table III. In Fig.4 we have also plotted the known experimental values of the average $\overline{N_h}$ for interactions of protons with Cr.W [4], CNO and AgBr [5] and for interactions of protons and pions with nuclear emulsion [6]. The agreement between the directly measured $\overline{N_h}$ values and those found by the above procedure supports strongly our hypothesis.

The dependence \overline{N}_h on $\overline{V_A}$ for interactions of protons and pions, which follows from the already found \overline{N}_h vs A dependence, is presented in Pig.5. The mean number of collisions $\overline{V_A}$ of the incoming particle inside the target nucleus with the mass number A was calculated using the formula $V_A = \frac{A \cdot S_{12}}{S_A}$, where $\overline{S_P}$ and $\overline{S_A}$ denote the inelastic cross-sections on the proton and the nucleus with mass number A, respectively. One can see from Fig.5 that there is no unique relation between the mean number of $\overline{N_h}$ and the mean number of collisions. It depends on the nature of the projectile.

We would like to point out that the angular distribution of shower particles can be also parametrized using the number of black tracks \mathbb{N}_{b} or grey tracks \mathbb{N}_{g} emitted from the struck nucleus $(\mathbb{N}_{h} = \mathbb{N}_{b} + \mathbb{N}_{g})^{A'}$. The relations $\frac{A}{N} \frac{\partial (\mathcal{M}_{S})}{\partial (\mathcal{M})}$ vs \mathbb{N}_{b} and $\frac{A}{N} \frac{\partial (\mathcal{M}_{S})}{\partial (\mathcal{M})}$ vs \mathbb{N}_{g} are in a good approximation linear, similarly

^{4/} N_b - tracks having range in emulsion $R \leq 3600$ mµ, N_g - tracks with relative ionization > 1.4 and R > 3600 mµ.

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as it was found for N_{μ} as a parameter (formula (2)) .

By repeating again the same procedure (cf. eq. (5)) we have obtained the mean values of N_b and N_g for each target nucleus (see Table III). The relations we have got between the mean values of $\overline{N_b}$ or $\overline{N_g}$ and the mass number A of the target nucleus or the corresponding values of $\overline{N_A}$ are presented in Fig.6 and 7.

We conclude that the angular distribution of produced particles in proton-nucleus or pion-nucleus interactions can be parametrized as follows:

$$\frac{1}{N}\frac{dn_{s}}{d\eta} = a_{I}(\eta, E) + b_{I}(\eta, E) N_{slow}$$
(6)

where $N_{\rm slow}$ could be $N_{\rm h}$, $N_{\rm b}$ or $N_{\rm g}$. The coefficients $a_{\rm I}$ and $b_{\rm I}$ for a chosen $N_{\rm slow}$ parameter do not depend on the mass number A of the target nucleus. In other words the angular distribution of shower particles produced in interactions of a given primary particle at a given energy does not depend on the target nucleus provided the same number of slow particles $N_{\rm slow}$ has been emitted. Since formula (6) holds for any nucleus it is also valid for any mixture of nuclei (e.g. nuclear emulsion). The relation between $N_{\rm alow}$ and $\overline{V_{\rm t}}$ is not universal. It depends on the nature of primary particle.

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Table_I

Values of a I and b I per unit M interval

~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	200 GeV protons			200 GeV J -			
interval	ap	bp	χ ² NDF=3	£ ⁸	تت ^ن	X ² NDP=3	
-2<72-1	0.006 ±0.003	0.003 ±0.001	0.01	0.003 10.008	0.002 10.001	1.76	
-1<7<0	0.021 ±0.006	0.020 ±0.002	0.96	0.019 ±0.010	0.021 ±0.003	5.32	
0<7<1	0.322 ±0.025	0.112 ±0.006	6.74	0.192 ±0.029	0.106 ±0.007	7.82	
1<¶{2	1.097 ±0.050	0.222 ±0.009	0.22	0.681 ±0.057	0.210 ±0.013	11.03	
2<7<3	1.753 ±0.064	U.219 10.011	7.72	1.492 ±0.087	0.158 ±0.015	7.58	
3< ए ६४	° 066 ±∟.⊎63	0.122 ±0.009	7.31	1.815 ±0.094	0.109 ±0.014	6.06	
4 < n ≤ 5	1.928 ±0.047	0.033 ±0.006	6.82	1.918 ±0.073	0.023 ±0.010	2.78	
5 <n<6< td=""><td>0.928 ±0.027</td><td>-0.007 ±0.003</td><td>0,29</td><td>1.139 ±0.045</td><td>-0.022 ±0.006</td><td>0.89</td></n<6<>	0.928 ±0.027	-0.007 ±0.003	0,29	1.139 ±0.045	-0.022 ±0.006	0.89	
6 < m<7	0.309 ±0.015	-0.008 ±0.002	6.71	0.J25 ±0.025	-0.011 ±0.003	4.78	
7 < 9 58	0.062 ±0.008	-0.001 ±0.001	3.71	0.092 ±0.013	-0.004 ±0.001	5.92	

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<u>Table II</u>

Comparison of data on nuclear emulsion target obtained from our emulsion experiment and from counter experiment [3]

	200 GeV protons			200 GeV J		
7	$\frac{1}{N} \mathbf{n}_{g}(\gamma)$		χ2	<mark>1</mark> മ ₈ (γ)		٦²
interval	our data	Busza s data	NDP=1	our data	Busza s data	NDF=1
-0.67≤7<-0.38	0.05 ±0.01	0.14 ±0.03	8.84	0.05 ±0.01	0.11 ±0.03	4.05
-0.38 < 7 < 0.58	0.53 ±0.01	0.80 ±C.06	18.64	0.44 ±0.92	0.74 ±0.06	21.98
0.586720.92	0.57 ±0.02	0.54 ±0.04	0.63	0.43 ±0.02	0₊46 ±0₊04	0+33
0.92≤१<1.39	1.06 ±0.02	1.00 ±0.07	0.59	0.82 10.03	0.82 ±0.07	0 <b>.0</b> 04
1.39 6 7 < 1.99	1.76 ± 0.03	1.68 ±0.09	0.80	1.28 ±0.04	1.38 ±0.10	0,87
1.99 ≤ 1 < 2.25	0.85 ± 0.02	0.80 #0.05	0.89	0.62 ±0.02	0.67 ±0.06	0.70
2.25 & 7 < 2.76	1.69 ±0.03	1.56 #0.09	2.00	1.28	1.31 ±0.10	0,10
2.76 < 7<3.08	1.02 ±0.02	0.99 ±0.06	0,27	0.82 ±0.03	0.85 ±0.06	0.22
3.08 ≤ 7<3.38	0.92 ±0.02	0.90 #0.05	0.14	0.82 ±0.03	0.79 ±0.06	<b>0.</b> 17
3.38 ≼7<4.08	1.94 ± 0.03	1.90 #0.09	0.20	1.67 ±0.04	1.78 ±0.12	0.74
4.08 \$7< 5.28	2.20 ±0.03	2.08 40.12	1.01	2.24 ±0.05	2,42 ±0.28	0.39
5.28 < 7<7.	0.78 ±0.02	0.96	17.25	0.89 10.03	1.12	22.43

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## Table III

Values of  $\overline{M}_{h}$ ,  $\overline{M}_{b}$  and  $\overline{M}_{g}$  and the corresponding  $\chi^{2}$  values obtained for 12 nuclear targets by a procedure described

in the text.

target	200 GeV protons						
	Nh	L ² (NDF+9)	Nb	1 ² (NDF=9)	Ng	X²(N0F≥9j	
н ₂	-1.12 ±0.49	11.2	-1.33 ±0.36	16.8	-1.06 ± 9.21	18,4	
Be	0.97 ±0.40	5.8	0.24 ±0.30	11.0	-0.14 1 0.18	9.2	
C	1.65 ±0.39	4.2	0.74 10.30	8.4	0.14 ±0.17	5.7	
Al	3.93 ±0.50	2.6	2.40 ±0.37	4.9	1.10 ±0.21	1.5	
Ti	5.80 ±0.61	1.9	3.81 ±0.46	5*8	1.92 10.27	0.7	
Emulsion	6.68 ±0.61	2.6	4.46 ±0.47	2.5	2.30 ± 0.27	0.6	
Cu	6.92 ±0.64	2.6	4.64 ±0.48	2.4	2.41 ±0.28	0.7	
Мо	8.68 ±0.75	4.9	5.99 10.55	2.7	3.21 ±0.32	0.9	
Ag	9.28 ±0.78	6.4	6.44 ±0.57	3.2	3.47 ±0.33	1.3	
Ŵ	11.95 10.95	17.2	8.52 ±0.70	8.9	4.73 ±0.42	4.7	
РЪ	12.67 ±1.02	18.9	9.08 ±0.75	10.6	5.07 ±0.44	5.9	
U	13.40 11.08	22.2	9.68 ±0.80	12.9	5.44 ±0.48	7.6	

### Table III contd

Values of  $\overline{N}_h$ ,  $\overline{M}_b$  and  $\overline{M}_g$  and the corresponding  $\tilde{\lambda}^2$  values obtained for 12 nuclear targets by a procedure described

<u>in the</u>	text.						
target	200 Gev J						
	Ňn	$\chi^2(NDF=9)$	No	<u>)</u> ( (N0F≠9)	Ng	22(NDF=9	
B ₂	0.55 ±0.61	5.9	-0.69 ±0.55	13.1	-C.78 ±0.31	12.9	
Be	1.9) ±0.50	2.4	0.53 ±0.45	5.7	-0.12 ±0.25	6.1	
C	2.40 ±0.50	3.3	0.90 ±0.45	6.6	0.08 ±0.25	6.3	
VJ	4.47 ±0.65	0.6	2.55 ±0.57	0.7	0.99 ±0.30	1.2	
Ti	6,23 ±0,78	0,8	4.00 ± 0.67	0.5	1.78 ±0.35	1.2	
Emulsion	7.13 ±0.82	1.0	4.76 ±0.71	0.5	2.17 ±0.37	1.1	
Cu	7.29 ±0.85	1.1	4,89 20.74	0.5	2,25 ±0.38	1.2	
) Mico	9.05 ±0.97	1.9	6.40 ±0.84	1.0	3.07 ±0.43	1.9	
Ag	9.63 ±0.99	2.6	6.88 ±0.87	1.3	3.33 ±0.44	2.0	
Ħ	12.10 ±1.31	6.3	9.08 ±1.10	2.7	4.53 ±0.57	3.8	
ło	12.83 ±1.31	8.1	9.72 ±1.19	4.0	4+87 ±0+60	4.6	
U	13.57 11.42	9+3	10.30 ±1.27	4.3	5.24 ±0.65	5.7	



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Fig.1 Pseudorapidity distributions of particles produced in proton-emulsion interactions at 67 GeV - solid lines and 200 GeV - dashed lines. The distributions illustrate the parametrization of our data according to eq. (1) for  $N_{\rm h}$  = 0, 10, 20.

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Fig.2a Comparison of data on 200 GeV proton interactions obtained on nuclear emulsion as a target - from counter experiment[3] - dashed lines and from emulsion experiment [1] - dote.



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Fig.2b Comparison of data on 200 GeV I interactions obtained on nuclear emulsion as a target - from counter experiment [3] - dashed lines and from emulsion experiment [1] - dots.

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Fig.3a Pseudorapidity distributions of particles produced by 200 GeV protons on H₂, C, Ag and Pb targets. Solid lines - distributions obtained from our emulsion data by a procedure described in the text (cf.eq. (5)). Dashed lines - counter experiment data [3].

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Fig. 3b Pasudorapidity distributions of particles produced by 200 GeV negativ plons on H₂, C, Ag and Pb targets. Solid lines - distributions obtained from our emulsion data by a procedure described in the text (cf.eq. (5)). Dashed lines - counter experiment data [3].

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Fig.4  $\overline{M}_{h}$  vs A dependence obtained from the minimum  $\chi^2$  procedure described in the text (cf.eq. (5)).

- © 200 GeV proton interactions
- × 200 GeV J interactions

 experimental data for Cr, W nuclei, CNO, AgEr groups and nuclear emulsion

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Pig.5  $\overline{N}_h$  vs  $\overline{V}_h$  dependence obtained from the minimum  $\chi^2$  procedure (cf.eq. (5)).

- 200 GeV proton interactions
- × 200 GeV  $\widehat{J}$  interactions

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Fig.6  $\overline{M}_{b}$  vs A and  $\overline{M}_{g}$  vs A dependence obtained from the minimum  $\lambda^{2}$  procedure described in the text.

- 200 GeV proton interactions
- × 200 GeV J interactions

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