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**AN INVESTIGATION
OF ASSOCIATIVE MULTIPLICITY
IN THE REACTION $\bar{p}p \rightarrow p$ (SLOW) + X
AT 22.4 GeV/c**

**Alma-Ata - Dubna - Helsinki - Kosice - Moscow -
Prague Collaboration**

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**B.V.Batyunya, I.V.Boguslavsky, I.M.Gramenitsky, R.Lednický,
S.V.Levonian, L.A.Tikhonova, T.P.Topuriya*, A.Valkarova,
V.Vrba, Z.Zlatanov**

Joint Institute for Nuclear Research, Dubna, USSR

A.A.Loktionov, V.V.Samojlov, M.A.Tashimov, T.Temiraliev
High Energy Physics Institute, Alma-Ata, USSR

J.Ervanne, S.Dumbrals-Ljung, R.Orava, P.Villanen
*Department of High Energy Physics, University of Helsinki,
Helsinki, Finland*

J.Patočka
UPJS University, Kosice, ČSSR

**R.K.Dementiev, V.E.Grechko, I.A.Korzhavina, E.M.Leikin,
V.I.Rud**
*Institute of Nuclear Physics, Moscow State University, Moscow,
USSR*

J.Cvach, I.Herynek, P.Reimer, V.Šimák
Institute of Physics, ČSSR Academy of Sciences, Prague, ČSSR

* Tbilisi State University, Tbilisi, USSR.

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Исследование ассоциативной множественности в реакции
 $\bar{p}p \rightarrow p(\text{медл.}) + X$ при 22,4 ГэВ/с

В работе исследуется поведение ассоциативной множественности как функции недостающей массы к идентифицированному протону в реакции $\bar{p}p \rightarrow p(\text{медл.}) + X$ при 22,4 ГэВ/с. Показан различный характер поведения ассоциативной множественности для дифракционных ($M_X^2/s \leq 0,1$) и недифракционных событий. В рамках двухкомпонентной модели качественно объяснено поведение отношения $\langle n(M_X^2) \rangle / D$ как функции M_X^2 .

При использовании масштабной переменной

$$z' = (n_{ch} - 1 - \alpha) / (\langle n(M_X^2) \rangle - \alpha), \quad \alpha = -1,04$$

для всех значений M_X^2 был получен аналог скейлинга KNO в системе X. Отмечается подобие реакций $\bar{p}p \rightarrow p(\text{медл.}) + X$ и $pp \rightarrow p(\text{медл.}) + X$.

Работа выполнена в Лаборатории высоких энергий ОИЯИ.

Препринт Объединенного института ядерных исследований. Дубна 1979

An Investigation of Associative Multiplicity in the
 Reaction $\bar{p}p \rightarrow p(\text{slow}) + X$ at 22.4 GeV/c

The associative multiplicity as a function of the missing mass squared to the identified proton in the reaction $\bar{p}p \rightarrow p(\text{slow}) + X$ at 22.4 GeV/c is studied. A different behaviour of the associative multiplicity for diffraction ($M_X^2/s \leq 0.1$) and nondiffraction events is observed. The M_X^2 dependence of the ratio $\langle n(M_X^2) \rangle / D$ is qualitatively explained on the basis of the two-component model.

An analogue of KNO scaling in the system X is obtained for all values of M_X^2 with the help of the scaling variable.

$$z' = (n_{ch} - 1 - \alpha) / (\langle n(M_X^2) \rangle - \alpha), \quad \alpha = -1.04.$$

A similar behaviour of the reactions $\bar{p}p \rightarrow p(\text{slow}) + X$ and $pp \rightarrow p(\text{slow}) + X$ is pointed out.

The investigation has been performed at the Laboratory of High Energies, JINR.

1. The associative characteristics of recoil system X to identified particle c in the reaction $aN \rightarrow c + X$ have been extensively studied for various particles a and c^{1/}.

In this paper we study the reaction



at 22.4 GeV/c. About 21 000 inelastic events were used in this analysis. Protons with a laboratory momentum of ≤ 1.5 GeV/c were identified by ionization thus yielding about 5 600 events of the type (1). The questions concerning the separation of elastic events, the corrections for losses of inelastic 2-prong events with slow recoil protons, etc., have been analyzed in ref.^{1/2/}.

2. The average charged multiplicity of system X is defined through the topological (inclusive) differential cross sections $d\sigma_n/dM_X^2(d\sigma/dM_X^2)$ of reaction (1),

$$\langle n(M_X^2) \rangle = \sum_n (n-1) d\sigma_n/dM_X^2 / d\sigma/dM_X^2, \quad (2)$$

as a function of the missing mass squared M_X^2 to the identified proton. In fig. 1 we compare the M_X^2/s dependence of $\langle n(M_X^2) \rangle$ both for the reaction (1) and the reaction $pp \rightarrow p(\text{slow}) + X$ at 19 GeV/c^{1/9/}. We have fitted our data points by the logarithmic expression

$$\langle n(M_X^2) \rangle = a + b \ln(M_X^2/M_0^2), \quad M_0 = 1 \text{ GeV}^2. \quad (3)$$

in an interval of $4 \leq M_X^2 \leq 22 \text{ GeV}^2$ and by the power law

$$\langle n(M_X^2) \rangle = a_1 + b_1 \sqrt{M_X^2} \quad (4)$$

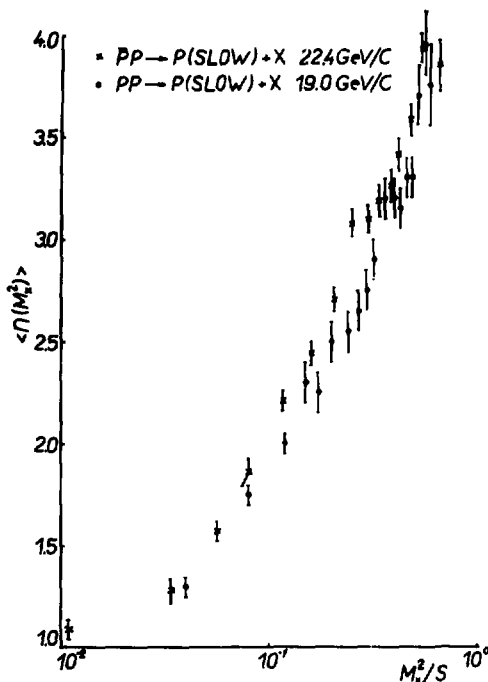


Fig. 1. The average charged multiplicity $\langle n(M_X^2) \rangle$ of system X as a function of M_X^2/s for the reactions $pp \rightarrow p(\text{slow}) + X$ (22.4 GeV/c) and $pp \rightarrow p(\text{slow}) + X$ (19 GeV/c)^{9/}.

in the diffraction region ($M_X^2 < 4 \text{ GeV}^2$), as suggested by multiperipheral models (see, e.g., ref.^{3/}) and by the fragmentation model "NOVA", incorporating cluster production^{4/}, respectively. The fitted parameters are shown in table 1 together with similar parameters for the reaction $pp \rightarrow p(\text{slow}) + X$.

3. In fig. 2 we show the M_X^2 -dependence of the ratio $\langle n(M_X^2) \rangle / D$, where

$$D = (\langle n^2(M_X^2) \rangle - \langle n(M_X^2) \rangle^2)^{1/2}. \quad (5)$$

A clear dip structure seen for $2 \leq M_X^2 \leq 4 \text{ GeV}^2$ can be explained, e.g., due to overlapping of two different mechanisms

Table 1

The parameters in eqs. (3), (4) and corresponding

$$X^2/ND \cdot pp(102-405)^{/8/}, \quad pp(36)^{/10/}.$$

Reaction momentum (GeV/c)	a	b	χ^2/ND	a_1	b_1	χ^2/ND
$\bar{p}p$ (22.4)	0.69 ± 0.11	0.94 ± 0.05	7.8/7	0.63 ± 0.09	0.61 ± 0.06	5/2
pp (36)	0.78 ± 0.45	0.85 ± 0.16	1.4/5	0.66 ± 0.18	0.55 ± 0.13	0.3/1
pp (102-405)	-0.55 ± 0.39	1.37 ± 0.09	-	0.71 ± 0.17	0.72 ± 0.07	-

in the diffraction region. In such a two-component model^{/5/} the dispersion can be written in the form

$$D = (\beta_1 D_1^2 + \beta_2 D_2^2 + \beta_1 \beta_2 (\langle n_1(M_X^2) \rangle - \langle n_2(M_X^2) \rangle)^2)^{1/2}, \quad (6)$$

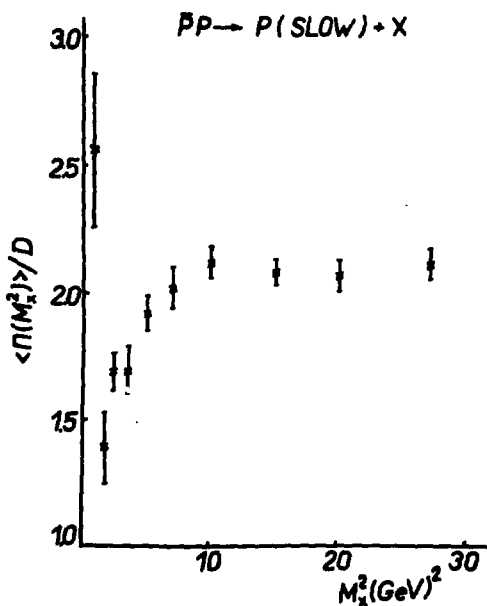


Fig. 2. The M_X^2 -dependence of the ratio $\langle n(M_X^2) \rangle / D$.

where the probabilities β_i of the two processes satisfy the normalization condition $\beta_1 + \beta_2 = 1$. The diffraction mechanism ($D=D_1$) dominates at $M_X^2 \sim 1 \text{ GeV}^2$ and the nondiffraction mechanism is responsible for $M_X^2 > 4 \text{ GeV}^2$ ($D=D_2$), while in the intermediate region the "interference" term in (6) increases the dispersion thus yielding the observed dip structure.

4. We analyse also the possibility of an analogue of KNO-scaling for the system X ^{/6/}. In table 2 we show the normalized moments $c_q = \langle n^q(M_X^2) \rangle / \langle n(M_X^2) \rangle^q$. It is seen that c_q values are different in the diffraction ($M_X^2/s \leq 0.09$) and nondiffraction regions. From this it follows that the usual KNO-scaling for the system X is not valid, i.e., the function

$$\Psi(z, M_X^2) = \frac{\langle n(M_X^2) \rangle d\sigma_N / dM_X^2}{d\sigma / dM_X^2} \quad (7)$$

Table 2

The normalized associative moments for various intervals of

$$M_X^2/s \cdot pp(205) ^{/6/}$$

M_X^2/s	c_2	c_3	c_4	Reaction momentum (GeV/c)
0. - 0.09	1.41 ± 0.02	2.71 ± 0.16	6.55 ± 0.85	$\bar{p}p$ (22.4)
	1.40 ± 0.04	2.58 ± 0.20	5.51 ± 0.82	pp (36)
	1.41 ± 0.03	2.54 ± 0.17	5.54 ± 0.69	pp (205)
0.09 - 0.18	1.26 ± 0.02	1.85 ± 0.09	3.18 ± 0.44	$\bar{p}p$ (22.4)
	1.25 ± 0.05	1.80 ± 0.19	2.90 ± 0.60	pp (36)
	1.22 ± 0.02	1.71 ± 0.06	2.66 ± 0.18	pp (205)
0.18 - 0.30	1.23 ± 0.02	1.72 ± 0.08	2.71 ± 0.18	$\bar{p}p$ (22.4)
	1.23 ± 0.04	1.71 ± 0.15	2.63 ± 0.43	pp (36)
	1.23 ± 0.02	1.77 ± 0.07	2.87 ± 0.20	pp (205)
0.30 - 0.39	1.23 ± 0.02	1.75 ± 0.04	2.76 ± 0.12	$\bar{p}p$ (22.4)
	1.27 ± 0.05	1.86 ± 0.17	3.02 ± 0.56	pp (36)
	1.23 ± 0.02	1.73 ± 0.06	2.70 ± 0.18	pp (205)
0.39 - 0.50	1.23 ± 0.02	1.74 ± 0.04	2.74 ± 0.13	$\bar{p}p$ (22.4)
0.50	1.24 ± 0.04	1.76 ± 0.15	2.73 ± 0.47	pp (36)

essentially depends on M_X^2 . To get rid of the M_X^2 dependence, we introduce the scaling variable ^{7/}

$$z' = (n_{ch} - 1 - a) / (\langle n(M_X^2) \rangle - a). \quad (8)$$

The parameter $a = -1.04$ in (8) is determined from the condition

$$[(\langle n(M_X^2) \rangle - a) / D]_d = [(\langle n(M_X^2) \rangle - a) / D]_{nd}. \quad (9)$$

where the l.h.s. (r.h.s.) have been calculated for $0 < M_X^2 < 4 \text{ GeV}^2$ ($4 < M_X^2 < 22 \text{ GeV}^2$). The corresponding normalized distribution $\Psi(z')$ is shown in *fig. 3* for $0 < M_X^2 < 22 \text{ GeV}^2$: The solid curve is the result of the fit:

$$\Psi(z') = (0.05 \pm 0.01) \exp[(7.78 \pm 0.59)z' - (4.17 \pm 0.58)z'^2 + (0.13 \pm 0.18)z'^3] \quad (10)$$

with $\chi^2 / ND = 26/20$.

5. CONCLUSIONS

The following results have been obtained in a study of the associative multiplicities in the reaction (1).

(i) We observe striking similarity between the reactions $\bar{p}p \rightarrow p(\text{slow}) + X$ and $pp \rightarrow p(\text{slow}) + X$ for comparable energies in an interval of $0 < M_X^2/s < 0.5$. This fact is illustrated by the $\langle n(M_X^2) \rangle$ distribution in *fig. 1* and the corresponding parameters

in *table 1*. Besides, in the diffraction region $M_X^2/s \leq 0.09$ the $\langle n(M_X^2) \rangle$ distribution is clearly independent of incident momentum (see the parameters a_1, b_1 in *table 1*).

(ii) The M_X^2 dependence of the ratio $\langle n(M_X^2) \rangle / D$ is qualitatively explained on the basis of the two-component model.

(iii) An analogue of KNO-scaling in the system X is obtained for all values of M_X^2 with the help of the scaling variable

$$z' = (n_{ch} - 1 - a) / (\langle n(M_X^2) \rangle - a), \quad a = -1.04.$$

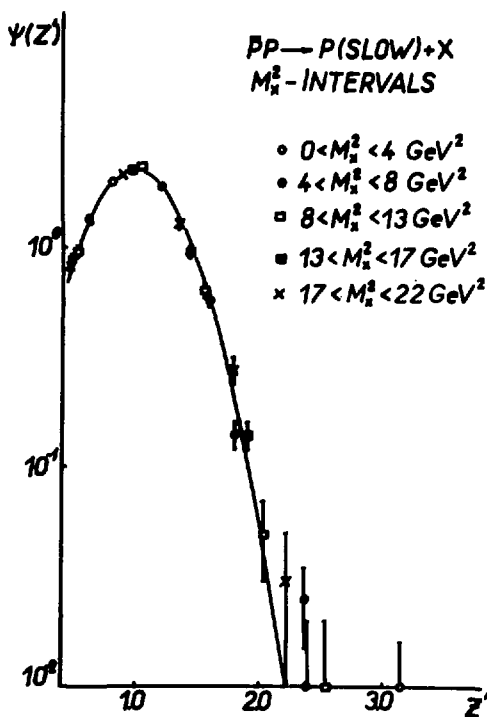


Fig. 3. The distribution $\Psi(z') = \frac{(\langle n(M_X^2) \rangle - a) d\sigma_n / dM_X^2}{d\sigma / dM_X^2}$,

$$z' = (n_{ch} - 1 - a) / (\langle n(M_X^2) \rangle - a), \quad a = -1.04$$

in an interval of $0 < M_X^2 < 22 \text{ GeV}^2$. The solid curve is defined in eq. (10).

REFERENCES

1. Blobel V. et al. *Nucl. Phys.*, 1977, B122, p.429.
Zhuravleva L.I. et al. *JINR*, P1-10643, Dubna, 1977.
2. Boos E.G. et al. *Nucl. Phys.*, 1977, B121, p.381.
3. Chan C.F. *Phys. Rev.*, 1973, D8, p.179.
4. Berger E.L., Jacov M., Slansky R. *Phys. Rev.*, 1972, D6, p.2580.
5. Van Hove L. *Phys. Lett.*, 1973, 43B, p.65.

6. Barshay S. et al. *Phys. Rev.Lett.*, 1974, v.32, p.1390.
7. Clifford T.S.et al. *Phys. Rev.Lett.*, 1974, v.33, p.1239.
8. Whitmore J. *Phys. Rep.*, 1974, 10C, p.274.
9. Boggild H. et al. *Nucl.Phys.*, 1974, B72, p.221.
10. Boguslavsky I.V. et al. *JINR*, 1-11828, Dubna, 1978.

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