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SCALING IN THE MEAN AND ASSOCIATIVE MULTIPLICITIES FOR THE INCLUSIVE REACTIONS $\ddot{p} + p \cdot K_s^0 + x$ AND $\ddot{p} + p \cdot \Lambda + X$ AT 22.4 GeV/c

Dubna - Alma-Ata - Helsinki - Moscow - Prague - Tbilisi Collaboration

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батюня Б.В. и др.

Исследование скейлинга в среднем и ассоциативной множественности в инклюзивных реакциях образования K_s° - и Λ -частиц в $\bar{p}p$ -взаимодействиях при 22,4 ГэВ/с

В работе представлены результаты экспериментального исследования скейлинга в среднем и ассоциативной множественности в реакциях образования K_s° – и Λ -частиц в \bar{p} р-взаимо-действиях при 22,4 ГэВ/с. Показано, что скейлинг в среднем выполняется для K_s° -мезонов и нарушается для Λ -гиперонов. Проверяется теоретическое предсказание о связи скейлинга в среднем с другими скейлинговыми законами.

Для Λ -частиц получена линейная зависимость ассоциативной множественности от логарифма квадрата недостающей массы с параметром наклона, близким по величине аналогичным параметрам, найденным в других экспериментах. Проверено выполнение ассоциативного КNO-скейлинга для реакций образования Λ -гиперонов.

Работа выполнена в Лаборатории высоких энергий ОИЯИ.

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Scaling in the Mean and Associative Multiplicities for the Inclusive Reactions $\bar{p}+p \to K^o_g + X$ and $\bar{p}+p \to \Lambda + X$ at 22.4 GeV/c

Scaling in the mean and associative multiplicities are studied for K_s° and Λ production in pp-interactions at 22.4 GeV/c. It is found that the scaling in the mean is valid for K_s° -mesons and not for Λ -hyperons. The connection of the scaling in the mean with other scaling laws is discussed. For Λ particles the associative multiplicities depend linearly on the logarithmic missing mass squared with a slope parameter comparable to those found in other experiments. The validity of the associative KNO-scaling has been tested for events with Λ -production.

The investigation has been performed at the Laboratory of High Energies, JINR.

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1. SCALING IN THE MEAN

The hypothesis of scaling in the mean was introduced in paper $^{'1}$ '. From it a scaling equation follows for semi-inclusive one-dimensional distributions of particle c

$$\frac{\langle \mathbf{p}_i \rangle_n}{\sigma_n^c} = \frac{d\sigma_n^c}{d\mathbf{p}_i} = \phi_i \left(\frac{\mathbf{p}_i}{\langle \mathbf{p}_i \rangle_n} \right) \tag{1}$$

Here i=T,L for transverse (p_T) and c.m. longitudinal (p_L^*) momenta of particle c, $(p_i)_n$ are the mean values of these momenta, and (σ_n^c) is the inclusive cross section of particle c produced in association with n charged particles. The functions (ϕ_i) depend only on the scaling variable (p_i) $(p_i)_n$, but neither on primary energy nor on charged multiplicity. It has been also assumed that the functions (ϕ_i) are independent of the initial state.

Equation (1) has been tested for π^{σ} -meson production in different reactions '1.2a' and for neutral strange particle production in pp-interactions at 19 GeV/c '2b' and 300 GeV/c '2c' It has been found that scaling in the mean is valid for mesons, but for Λ -particles only the variable p $_{\Upsilon}$, p $_{\Upsilon}$, p $_{\Upsilon}$, scales.

In this paper the semi-inclusive processes

$$\bar{p} + p \rightarrow K_s^{\circ} + n + \text{neutrals}$$
 (2)

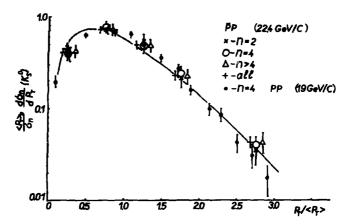
$$\vec{p} + p \rightarrow \Lambda + n + neutrals$$
 (3)

(n is the number of charged particles) are studied using equation (1).

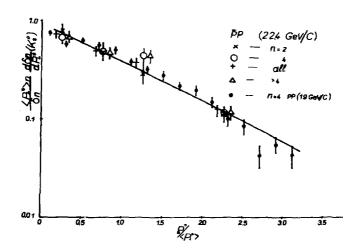
The experimental data have been obtained in exposures of the hydrogen bubble chamber Ludmila to a RF separated beam of 22.4 GeV/c antiprotons at the Serpukhov accelerator. The amount of interactions is 1123 with $\rm K_s^o$ -mesons and 454 with Λ -hyperons. The scanning, measuring and fitting procedures of the interactions with neutral strange particles have been described elsewhere $^{/3/}$.

The transverse and longitudinal distributions (equation(1)) are presented for K_s^o -mesons in Figs.1 and 2 and for Λ -hyperons in Figs.3 and 4* The data with $n \ge 6$ have been combined in

^{*}For clarity our data with n > 6 and for all events have been shifted along the abscissa axis from the real positions (data at n=2,4). The data for all events include zero-prong interactions as well.



<u>Fig.1.</u> Plot of $(\langle p_T \rangle_n/\sigma_n) \cdot (d\sigma_n/dp_T)$ versus $p_T/\langle p_T \rangle_n/\sigma_n$ versus $p_T/\langle p_T \rangle_n/\sigma_n$. We mesons. The solid line is the result of fitting the m-production in pp-interactions in an energy interval of 13-300 GeV/c.



 $\frac{\text{Fig.2.}}{\text{for }K^{\circ}_{\text{L}}-\text{mesons.}}$ The solid line is the result of fitting the π^- -production in pp-interactions in an energy interval of 13-300 GeV/c.

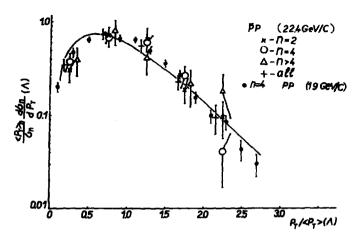
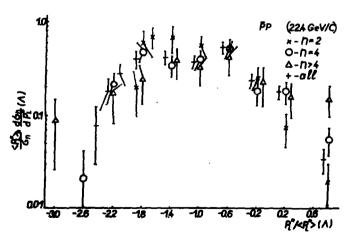


Fig. 3. Plot of $(\langle p_T \rangle_n / \sigma_n)(d\sigma_n / dp_T^*)$ versus $p_T / \langle p_T \rangle_n$ for Λ -particles. The solid line is the same as that in <u>fig.1</u>.



 $\frac{\rm Fig.4.~Plot~of~(< p_L^*>_n/\sigma_n~)\cdot (d\sigma_n/dp_L^*)~~versus~p_L^*/< p_L^*>_n}{\rm for~A~-particles.}$

 $\frac{Table}{} \mbox{'}$ Average values of p $_T$ and p $_L^{\star}$ (in the c.m.s.) for K $_s^{\circ}$ and A - particles.

Particle	Multiplicity	Number of events	∠P _T >n GeV/c	$\angle P_L >_n \text{ GeV/c}$
K°	2	265	0.42 ± 0.02	0.65 ± 0.04
	4	375	0.43 ± 0.01	0.57 ± 0.03
	≫ 6	435	0.43 ± 0.01	0.44 ± 0.02
	all	1123	0.423 <u>+</u> 0.008	0.56 ± 0.02
٨	2	166	0.47 ± 0.02	-1.58 ± 0.08
	4	185	0.49 <u>+</u> 0.02	-1.09 ± 0.07
	≫ 6	81	0.47 ± 0.03	-0.69 ± 0.08
	all	454	0.48 ± 0.01	-1.26 ± 0.05

order to improve statistics. The points from the pp-experiment at 19 GeV/c are given for comparison.

For K_8° -mesons the hypothesis of scaling in the mean is valid within errors for both transverse and longitudinal variables. For Λ -hyperons the scaling in the mean holds for the transverse variable, but for the longitudinal variable the shape of the distribution depends on multiplicity. For low multiplicities it is steeper. A similar effect has been also observed in the PP-experiment at 19 GeV/c.

The curves in Figs.1,2 and 3 describe the scaling in the mean for π -production in pp-interactions in an energy interval of 13-300 GeV/c $^{'1'}$. One can see that the data points follow these curves closely. A similar feature has been observed for π° -mesons in π° P-interactions at 5 GeV/c $^{'2a'}$. Thus, one can see that scaling in the mean distributions for both PT and Pt - variables are very similar for different types of mesons. In addition, for the PT-variable these distributions are very alike for mesons and Λ -hyperons.

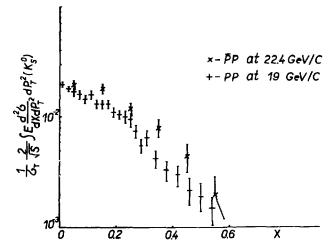
The mean values of the transverse and longitudinal momentum for K_s° and Λ are presented in the Table. As is seen, the absolute values of $< p_L^*>_n$ for Λ -hyperons decrease with increasing n , i.e., the leading behaviour * of Λ 's is more pronounced for small multiplicities. So the kinematical limits for the variables $p_L^*/< p_L^*>_n$ vary strongly for different n^{**} and scaling in the mean is violated at large negative values of $p_L^*/< p_L^*>_n$ (for $p_L^*/< p_L^*>_n <-1.8$ in Fig.4). Thus, the violation of the law of scaling in the mean for Λ 's in this kinematical region is connected with the leading effect.

It has been proposed $^{\prime 4\prime}$ that the scaling in the mean is a consequence of; a) Feynman scaling $^{\prime 5\prime}$, b) KNO-scaling $^{\prime 6\prime}$ and c) factorization of the cross section over longitudinal and transverce momenta

$$\frac{\mathrm{d}^2 \sigma_n}{\mathrm{d} p_L^* \, \mathrm{d} p_T} = f_1(p_L^*, \frac{n}{\langle n \rangle}) \cdot f_2(p_T), \tag{4}$$

^{*}The production of Λ 's mainly in the proton fragmentation region.

^{**}The $p_L^*/< p_L^*>_n$ kinematical limits are -1.94 for n=2, -2.74 for n=4, -4.22 for $n\geq 6$ and -2.43 for all events.

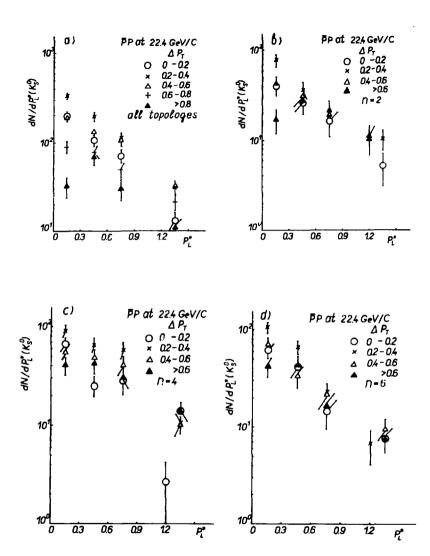


 $\frac{\text{Fig. 5. Distribution of the invariant function}}{\frac{1}{\sigma_{\text{tot}}}\frac{2}{\sqrt{s}}\int E^{*}\frac{d^{2}\sigma}{dx\ dp_{T}^{2}}dp^{2}_{T} \quad \text{versus x for K}_{s}^{\circ}\text{-mesons.}}$

where n/<n> is the KNO-variable $^{\prime 6}{}^{\prime}$. In other words, it has been supposed that the hypothesis of scaling in the mean contains no new information. In order to check this assumption, we have tested the conditions a) and c) for K_o^s inclusive production. Figure 5 shows the invariant normalized inclusive x-distributions (x is the Feynman variable) for K_o^s production in our experiment and in pp-interactions at 19 GeV/c $^{\prime 7}{}^{\prime}$. One can see that there is a significant difference between the presented distributions in the intermediate region of x, i.e., Feynman scaling does not hold for different initial states.

In <u>fig.6</u> (a,b,c,d) we show the p*-distributions of K*o in different intervals of p*_T for all events and separately for multiplicities 2, 4 and 6. It is seen that in all considered cases the shapes of the distributions change with p*_T , i.e., the factorization condition (4) is not fulfilled. The same result has been found for pp-interactions at 19 GeV/c $^{\prime 2b\prime}$.

Thus, the results presented in <u>figs.5</u> and <u>6</u> do not support the assumption that the scaling in the mean is only the consequence of the above laws a), b), c). Another picture of connection between the scaling laws is considered in papers $^{/8/}$,



 $\frac{\text{Fig.6}}{\text{vals}}.$ p_L^* -distribution of K_s° for different intervals of p_T^* .

where it has been obtained that at asymptotic energies the validity of KNO-scaling and scaling in the mean leads to the violation of Feynman scaling. This violation in the central region (at x=0) may correspond (with certain additional assumptions) to the rise of the cross section of meson production, which is also experimentally observed 9 in pp-interactions up to ISR energies.

2. MULTIPLICITIES ASSOCIATED WITH STRANGE PARTICLES IN $\vec{p}p \to K^\circ_0 + X$ AND $\vec{p}p \to \Lambda + X$ REACTIONS AT 22.4 GEV/C

Associative multiplicities in inclusive processes have been studied as a function of missing mass $\rm M_{\chi}$ for this and other experiments $^{\prime 10\prime}$. The following logarithmic dependence has been predicted $^{\prime 11\prime}.$

$$n(M_x^2) = A + B \ln(M_x^2)$$
 (5)

in the framework of the multiperipheral model for particle production in the fragmentation region. In eq.(5) B is the universal slope parameter. The prediction has been made assuming that a main contribution to these processes comes from the diagrams where system X is produced in the virtual interaction of some effective trajectory with one of the primary particles. The M_{χ}^2 value is analogous to the c.m.s. energy squared for real processes.

In Fig.7 the average charged multiplicities $n(M_x^2)$ are presented as a function of M_x (to logarithmic scale) for inclusive production of K_s° and Λ . The fit to expression (5) (solid line in Fig.7) yields for the slope parameter of Λ 's $B=1.26\pm0.14$ ($\chi^2/N_F=1.5/6$). For K_s° -mesons the fit is not satisfactory ($\chi^2/N_F=27/7$). For comparison with other results we have also made the same fit for Λ 's with $\cos\theta < < -0.5*$ ($\sim85\%$ of the sample) where θ is the polar angle in the c.m.s. We got $B=1.31\pm0.11$, which is almost the same as without the cut. Both values of the parameter B for Λ -particles agree rather well with the values obtained in other experiments $^{/10/}$.

Analogously to real processes, one can assume that for system X produced with Λ -particles the Wroblewski $^{/12/}$ and KNO relations have been applied in the following way:

$$D(M_{x}^{2}) = a + b < n(M_{x}^{2}) >$$
 (6)

In Fig.7 these new data are denoted by circles if they do not coincide with those observed for all Λ 's (crosses in Fig.7).

and
$$\frac{\langle n(M_x^2) \rangle}{\sigma(M_x^2)} \sigma_n(M_x^2) = \Psi(\frac{n(M_x^2)}{\langle n(M_x^2) \rangle}), \tag{7}$$

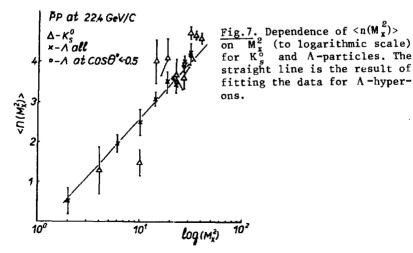
where $D\left(M_{x}^{2}\right)$ is the square root of the dispersion of the associative multiplicity distribution, $\sigma\left(M_{x}^{2}\right)$ and $\sigma_{n}\left(M_{x}^{2}\right)$ are the total and topological cross sections for definite values of M_{x}^{2} .

The experimental dependence of $D(M_x^2)$ on $\langle n(M_x^2) \rangle$ is shown in Fig.8 for different M_x^2 intervals. After fitting the experimental data by the function (6), we have obtained the parameters $a=0.28\pm0.3$ and $b=0.40\pm0.09$ (straight line in fig.8). In Fig.9 is shown the KNO dependence (7) for three intervals of M_x^2 . One can see that the KNO distributions for all M_x^2 intervals are similar.

An analytical expression for the associative KNO scaling has been obtained in the framework of renormalizable quantum field teeory using the renormalization group method $^{/15/}$. For system X with mass M, we get

$$\Psi\left(Z\left(M_{x}^{2}\right)\right) = C \frac{\alpha^{\alpha}}{\Gamma(\alpha)} Z^{\alpha-1}\left(M_{x}^{2}\right) e^{-\alpha Z\left(M_{x}^{2}\right)}, \tag{8}$$

where $Z(M_x^2) = n(M_x^2)/\langle n(M_x^2) \rangle$, C is a normalization para-



meter and $a=1/b^2$ (b is the same as in eq.(6)). The curve in Fig.9 is the result of fitting our data by expression (8) with the parameter $C=1.86\pm0.11$ ($\chi^2/N_F=4.2/10$). One can see that the data are quite well described by expression (8).

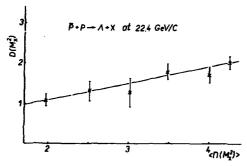


Fig. 8. Dependence of $\overline{D(M_x^2)}$ on $\langle n(M_x^2) \rangle$ for Λ' s for the intervals $\Delta M_x^2 = (4-8, 8-12, 12-16, 16-24, 24-30, 30-32) (GeV/c)^2$. The straight line is the fitting result.

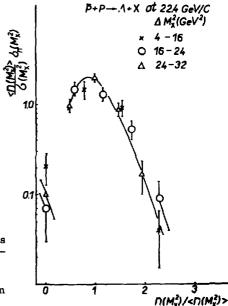


Fig. 9. Plot of $(\sigma_n(M_x^2) \times \times (n(M_x^2)))/\sigma(M_x^2)$ versus $n(M_x^2)/(n(M_x^2))$ for Λ -particles. The curve is the result of fitting by the theoretical expression (8).

3. CONCLUSIONS

- 1. The scaling in the mean is shown to be valid in the variables $p_T/\langle p_{T}\rangle_n$, $p_L^*/\langle p_L^*\rangle_n$ for inclusive K_s^o -production. The scaled distributions coinside with the data obtained in pp- and π^-p -interactions.
- 2. For Λ particles the scaling in the mean in the variable $p^*_L/< p^*_L>_n$ is violated which can be due to the leading particle behaviour.
- 3. The dependence of the mean associative multiplicities on $\ln(M_{\chi}^{2})$ for Λ -production is linear, the slope agreeing rather well with the values obtained in other experiments.
- 4. The associative KNO-scaling for Λ 's is observed in our experiment. The KNO distribution has the shape predicted by renormalizable quantum field theory.

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