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ON ALPHA DECAY OF SOME ISOMERIC STATES IN Po-Bi REGION \*

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## ABSTRACT

The relative and absolute  $\alpha$ -decay probabilities of the  $^{211m}$ Po,  $^{212m}$ Bi and <sup>212m</sup> Po isomers are calculated and various possibilities of their spin parity and configuration assignation are discussed.

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1. The study of the alpha decay of iscmers represents a useful and often a unique vay to obtain information about the structure of high spin isomers. Many authors  $\left( \frac{1}{n} \right)^{-1}$  have tried to describe the sluka decay of have tried to flpreribe the PlnVn decay of Po end Follitican ground and excited states of nuclei. In Pefs.1-3 the R-matrix theory or alpha decay was used to calculate the relative probabilities which were compared with the experiment. Such a comparison for absolute values of  $\alpha$ -decay probabilities  $(1)$ -3) meet difficulties the theoretical values depending strongly on the channel radius  $R_0$ . In certain cases, e.g. for  $212m$ Po, even the relative probabilities depend 3) on R. In this paper we use the non-K-matrix shell model approach to  $\alpha$ -decay theory  $\frac{5}{2}$ for the study of  $\frac{211m}{P}$  isomers with excitation energy  $E^* = 1.45$  MeV and of new isomers  $^{6)}$ ,7) of  $^{212}$ Bi and  $^{212}$ Po. Here, we apply the procedure used earlier  $\binom{1}{1}$  in studying the isomers of  $\frac{212}{10}$  (with  $E^* \approx 2.93$  MeV) and  $^{210m}$ Bi (E\* = 0.625 MeV), Thus, as the theory  $^{5)}$  does not have free parameters. we can use not only the relative values, but also the absolute probabilities for choosing between different possible configurations, spins and parities of isomeric states. The absolute theoretical values are compared with the experiment in terms of the enhancement coefficient K, defined in Refs.4 and  $r \in \mathbf{X}$  the endangleric coefficient coefficient  $r \in \mathbf{X}$ , defined in Refs. 5 as  $K = \frac{u}{-1+v} = \frac{f(x)}{a^2}$ , where  $\int_a^b Y'$  is the alpha decay width in the independent particle ~ L/C (i.p.) shell model **with** Woods-Saxon(W-S) potential (for more details see Refs.4, 5 and 8). According to the criterion of classification of absolute values  $\frac{h}{2}$ , the decays involved in this work belong to the unfavoured alpha decays (with  $K \le 10^2$ ) as coming from high spin states of nuclei and carrying large angular momenta, or to the semifavoured decays (with log  $K \approx 3$ ).

2. The alpha decay scheme of  $\frac{1 \text{ }\mu \text{ }}{1}$  is shown  $\frac{3}{2}$  in Fig.1. The spin, parity  $(\overline{I}_{\ell}^{\pi})$  and the wave function of the isomeric state ( $E^* = 1.45$  MeV) are unknown. The only limitation  $^{10)}$  of the I<sub>1</sub> value, I  $\frac{19}{2}$  comes from Wigner's estimation. The excited  $\frac{1}{2}$ ,  $\frac{2}{10}$  and  $\frac{12}{10}$  states can, with  $^{11})_{\text{biconvidored}}$  se enchalo state enough precision, beoonsidered as one-hole states In 2f, 3p and li neutron shells. The relative values  $\Gamma_H/\Gamma_A$ ,  $\Gamma_\sigma/\Gamma_A$  and  $\Gamma_\sigma/\Gamma_A$  were calculated by Zeh and Mang in the R-matrix theory of  $\alpha$  decay  $\overline{A}$ ising the harmonic oscillator (H.O.)shell.model. Two facts allow the comparison with Zeh and Mang's results. First, the relative values of  $^{211m}$ Po do not depend on the channel radius R,, Ref.l, and second, we found that the exchange of basis from H.O. to V-S the the same weakstable of changing 5) the does not in this case affect/relative values, in spite of changing 5) the absolute ones.

-2-

The results of our calculations are presented in Table I in comparison with Ref.1 and also with the experiment  $\frac{9}{2}$ . We presume, as in Ref.1, that we have state,  $\frac{1}{2}$  and  $\frac{1}{2}$  and  $\frac{1}{2}$  and  $\frac{1}{2}$ eric $l$ configurations with two unpaired protons $l$ as  $\frac{1}{\ln\alpha}$ or  $f(h_{n,m}, h_{n,m}) = 2g$ ,  $h_{n,m}$  as can be seen, our results are near to  $\frac{1}{2}$  $\frac{1}{2}$  and  $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{29}{2}$  configuration. In both cases (ours and  $\frac{1}{2}$  and  $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac$ Ref.l) the relative values are not reproduced when one uses simple configurations. The most noticeable difference between theory and experiment for the D/A ratio is always underestimated. This is merely the consequence of the shell model structure and does not depend on  $\alpha$ -decay theory. Namely, in the expression of  $\Gamma_+^{1,p}$ , Ref.5, the summation over the intermediate angular momenta at the given L takes place destructively for the D transition. the the states in the  $\frac{13}{6}$  and improvement of/D/A ratio from the admixture of other states in the 1i  $\frac{13}{6}$ wave function is limited by the small value of mixing coefficients  $11$ ). Another possibility is to take as additional terms in the isomeric states configurations which contribute only for the  $D$  transition<sup>-1</sup>. like configurations which contribute only for the D transition ', like and choosing the angular momenta  $\mathtt{j}_\mathtt{m}$  ,  $\mathtt{j}_\mathtt{m}$  $\begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix}$  and choosing the angular momenta  $\begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix}$  and  $\begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix}$ l i to give a maximum for the D value.

To impose the ratio B/A it is necessary to have additional terms with a constructive interference for the transition A and with a destructive one for the transition B. Unfortunately, we vere not able to find such a configuration mixing by using only two components. An adding term like  $\bar{8}^{-11}$ 11 /2 $^{\rm l}$ I<sup>+</sup> which fulfills the requested properties, has a small awidth and thus its contribution is not essential. (We remark that in Ref.l the ratio B/A was not discussed, as it was not yet experimentally determined.)

Three configurations from Table I are closer to the experiment for the relative values:  $I_1^{\pi_1} = \frac{25}{2}$ ,  $\frac{21}{2}$  and  $\frac{23}{2}$ . As only the relative values cannot permit to select between the proposed configurations, we must apply to the criterion of the absolute probabilities. We expect for the accounted unfavoured transition values of log K  $\zeta$  2, in analogy with the  $^{Z12m}$ Po isomer, Ref.5. The results of calculations for K are shown in the last column of Table I. The configurations with  $I_1^{\pi_1} = \frac{27^+}{2}$ ,  $\frac{29^-}{2}$ , having the coefficient K too large cannot be accepted, while the rejection of configurations with  $I_1^{\pi_1} = \frac{19^4}{2}$ ,  $\frac{21^2}{2}$  and  $\frac{19^2}{2}$  is due to their small values for K. Followi the same criterion, the configuration with  $I_1^T = \frac{25^+}{2}$  is improbable and those with  $I_{i}^{\pi_{i}} = \frac{23^{+}}{2}$  and  $\frac{25^{-}}{2}$  are less probable.

By cumulating both criteria, two candidates still remain, namely and  $\left[\frac{(\ln_{9/2} \ln_{13/2})_9} {2 \ln_{23} t} \right]_{23}$ . In the frame of the.i.p. shell model we cannot distinguish between the last<sup>6</sup> two configurations, nor to improve the relative a values. A more complicated mixing can reach this goal, but the most probable configurations discussed here must remain the main torm of the isomeric state wave function. Otherwise, the strong admixture of other configurations (such as that proposed here for the D transition) will drastically change the values of K.

drastically change the values of K.

3. Two new isomeric states were reported  $\frac{6}{10}$  and  $\frac{212}{10}$  which are genetical parents, Fig.2, of isomers  $(6)$ ,7) in  $^{212}$ Po. The isomers connected by B decay must have close spins. Thus, the assignation  $6$  of  $I^{\pi} = 15^{-}$  for the 9m isomer in <sup>212</sup>Bi agrees with I  $\approx 16^+$  of the 45s isomer of <sup>212</sup>Po. These assignations are sustained by a-decay calculations  $\mu$ ) which are in good agreement with experiment for the configuration  $\left[ (ig_{9/2})_8^2 (2g_{9/2})_8^2 \right]_{16}$ .  $212^{16}_{12}$ The calculations of the a-decay discusses of the 25m isomer of  $^{212}$ Po (semifavoured transition) are shown in Table I. The spin  $I = 10$  for the last isomer can be excluded by using the K criterion (K value too large). This is the same for configurations like  $|(1h_+, )^2 - (2g_+) - |$  with different  $r_{\rm A} = 2.5 \times 10^{14}$   $\sim 200$   $\frac{1000}{3}$  $\mathbb{J}_{\mathbb{P}_i}$  and  $\mathbb{J}_{\mathbb{N}_i}$  and this conclusion agrees with Ref. 7. In contradiction 2  $9/2$   $J_{\text{P}_1}$   $9/2$   $J_{\text{N}_1}$ with Ref.7 our calculations do not support configurations, such as  $\left. \begin{array}{ll} \left. \begin{array}{ll} 1_{6} & \text{or} \end{array} \right\vert \left. \begin{array}{ll} \left( 1\text{h}_{9/2} \right)_{0} & \left( 2\text{g}_{9/2} \right)_{0} \end{array} \right\vert_{\mathfrak{g}^{+}} \end{array} \right.$  neither their coherent mixing, as having the same value of K. The remaining possibility for I structure of  $^{c1cm}$ Po, namely  $\big| \left(1\text{h}_{\text{q/2}}\right)^\epsilon_\text{0} \left(2\text{g}_{\text{q/2}} \left|1\text{f}_{11/2}\right\rangle_\text{8}\big|_{\text{s+}}$  is not excluded but less probable as having the K value too large. For its parent isomer of 25m in  $^{212m}$ Bi, the value of log K calculated with  $^{6)}$  I<sup>\*</sup> = 9<sup>-</sup> is larger than 3, which is in disagreement with the results from Ref.<sup>4</sup> for the analogue 210<sub>B1</sub> isomer and does not reproduce the relative values. An improvement of the Bi Isomer and does not reproduce the relative values. An improvement of the K value implies the decrease of the spin to  $1 = 7$  for the 25m isomer, which makes possible the assignation of less values for the spin of the corresponding <sup>212</sup>Po isomer also (e.g.  $I^{\pi} = 6^{+}$ ). The values I < 4 can be excluded as giving too small .values for K.

A more precise estimation of spins can be obtained by looking for the a decay of the new isomer of  $^{212}$ Po on first 3<sup> $-$ </sup> and 5<sup> $-$ </sup> states of  $^{208}$ Pb, with  $E_r \approx 7.88$  and 7 MeV, respectively. The loss in energy in comparison with the decay to ground state of  $208$ Pb will be partially compensated by the

decrease of  $L = \Delta I$ , especially for the  $5^{\degree}$  state, where  $L_{\alpha} = 1$  if the isomer has the spin 6 . This effect was observed earlier <sup>4)</sup> in the case of the  $^{212m}$  p.  $-(E^* = 2.9 \text{ MeV})$  isomer. More detailed calculations are in process.

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The relative values of a-decay probabilities and the values of  $K = \frac{r^{\alpha}}{r_1^{\alpha} \cdot P}$  calculated for the  $\frac{211m}{P}$  isomer.



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Table II

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