FERMILAB-Pub-81/74-THY October, 1981

Two Photon Physics*

W. A. BARDEEN Fermi National Accelerator Laboratory P.O.Box 500, Batavia, Illinois 60510

*Invited Talk Presented at the 1981 International Symposium on Lepton-Photon Interactions at High Energies, Germany, August 24-29, 1981.



I. INTRODUCTION

A new experimental frontier has recently been opened to the study of two photon processes. The first results of many aspects of these reactions are being presented at this conference. In contrast, the theoretical development of research into two photon processes has a much longer history. In this talk, I will review the many different theoretical ideas which provide a detailed framework for our understanding of two photon processes.

This field began with papers by Low on resonance production and by Calagero and Zemach² on meson pair production, both published in the same volume of the Physical Review in 1960. After a dormant period, interest in two photon processes was renewed in 1970 by a number of groups 3,4,5. The classic papers by Brodsky, Kinoshita, and Terazawa³ emphasize the intrinsic physical interest of two photon processes in addition to their role as a background to the annihilation reactions in ete collisions. these papers was followed by a burst of advent of theoretical activity which is largely summarized in reviews Terazawa and Budnev et al . After a diversion provided by the discovery of charm, interest in two photon processes was renewed with emphasis on structure functions, jets and QCD. The progress of the field, both theoretically and experimentally, is emphasized by the creation of specialized annual workshops held at Lake Tahoe in 1979, Amiens in 1980, and in Paris in 1981. We can look forward to continuing interest as more data becomes available to challenge a variety of theoretical speculations.

After a brief discussion of the equivalent photon approximations I will review the theoretical foundation of various aspects of two photon physics. These aspects include resonance production, exclusive particle production, structure functions, and jet production.

II. EQUIVALENT PHOTON APPROXIMATION

We are primarily interested in the physics associated with the two photon reaction, $\gamma^*+\gamma^*+x$. This reaction is not observed directly but must be inferred from e^+e^- reactions, $e^++e^-+e^++e^-+x$. Severe technical problems are associated with the precision determination of $\gamma^*\gamma^*$ cross-sections from e^+e^- data.

At high energy, the initial e⁺ and e⁻ beams may be approximately treated as an equivalent spectrum of collinear photons. The classical determination of this spectrum involves the equivalent photon approximation (EPA) developed by Weizacker and Williams and by Landau and Lifshitz in 1934. Brodsky et al¹ make use of a version of the EPA in their analysis of a number of interesting physical processes. Budnev et al⁷ criticize the use of this version of EPA when precision results in needed certain kinematic regions.

Attempts to improve the EPA have been a continuing interest. To obtain a model independent analysis of two photon processes, a complete study of their kinematic structure was made⁸. The group at College de France⁹ has made an extensive study of methods for extracting two photon cross-sections in a variety of situations including various tagging possibilities. The role of standard radiative corrections has also been studied¹⁰ and found to be small in most cases.

An alternative approach to the analysis of two photon processes involves the use of Monte Carlo studies of particular physical processes 11. This approach requires a detailed modelling of the physical processes, such as provided by the lowest order Feynman diagrams, and then uses a Monte Carlo program to compute the observable cross-sections. This procedure is clearly more sensitive to the experimental configurations but is dependent on the validity of the physical models employed.

The effective luminosity available for various two photon processes was also critically reviewed by J. Field 12 for various machine and tagging possibilities.

These different methods of analysis are important if two photon processes are eventually to provide precision tests of QCD or other dynamical theories. With this somewhat technical introduction, I now turn to the physics of two photon processes.

III. RESONANCE PRODUCTION

In 1960, Low¹ suggested that the π^{O} lifetime could be determined by observing its production in e⁺e⁻ collisions via the two photon process. He derived an expression which relates the production cross-section to the partial decay width into two photons. This expression, generalized to arbitrary spin, is given by

$$\sigma(e^+e^- + e^+e^-R) = (2\alpha \ln s/4M_e^2)^2 \cdot f(M_R^2/S) \cdot (2J+1) \cdot \Gamma(R+\gamma\gamma)/M_R^3$$
 where

$$f(\tau) = (1/2) \cdot (2+\tau)^2 \ln(1/\tau) - (1-\tau) (3+\tau)$$

and s the total energy squared.

In addition to the π^{O} , even charge conjugation resonances can be produced through the two photon process which are not observable through annihilation. Among these possible resonances are π^{O} , η , η' , f, f', A_{2} , quarkonia $(\eta_{C}, \chi_{C}, \eta_{b}, \chi_{b})$, gluonia, Higg's bosons, technibosons, etc. Of course these resonances are not produced with equal efficiency. A comprehensive review by Gilman¹³ uses various theoretical and experimental estimates of the partial widths to predict production cross-sections. We present his estimates for an electron beam energy of 15GeV; tables for other energies can be computed directly or found in Gilman's review.

Table I

Resonance	Γ(R+2γ) KeV	$(2\alpha \ln (S/4M_e^2))^2 f\tau)$	σ(ee÷eeR) nb.
π ^O η η' Α2 f' η α ΧΟ	7.95x10 ⁻³ 0.324 5.9 1.8 5.0 0.4 6.4 1 4/15	1.68 1.17 0.97 0.86 0.87 0.81 0.57 0.53	2.1 0.9 2.6 1.3 4.2 0.18 5x10-3 5x10-3 1x10-5
χ ₂ η _b	0.4	0.21	4x10

The theoretical framework for estimating $\Gamma(R \rightarrow \gamma \gamma)$ is described by Budnev et al⁷ and reviewed by Gilman¹³. I will briefly present the various theoretical arguments that have been used for these predictions for the different types of resonances.

A. π^0 , η , η' : The rate for pseudoscalar meson production is enhanced by the triangle anomaly and can be computed using a low energy theorem following from current algebra and chiral symmetry. The rate is given by

where the constant S=tr($\lambda^R Q^2$) includes the quark color factor and f_π is the pion decay constant. Recent measurements may be compared with the predictions in Table II.

Table II

	meory	Experiment
$\Gamma(\pi^0 + \gamma \gamma)$	7.6 eV	7.95 eV
$\Gamma(\eta+\gamma\gamma)$	395 eV	324 eV
$\Gamma(n' + \gamma \gamma)$	6.0 KeV	5.9 KeV

This dramatic agreement seems hard to justify as the use of current algebra for such heavy states as η and η' is suspect, especially when complicated by the "U(1) problem".

B. f,f,A₂,E,...: Predictions for the other light quark states are less firmly based and a variety of theoretical models have been used. Early models involved either vector-tensor dominance¹⁴ or FESR and duality¹⁵. The nonrelativistic quark model has been developed for these states and applied to these reactions¹⁶. An alternative model based on S-matrix unitarization¹⁷ has also been submitted to this conference.

Krasemann and Vermaseren¹⁶ make an extensive analysis of resonance production observed via the $\pi^+\pi^-$ final state based on the quark model. They obtain a 2γ width of $2^{1/4}$ KeV and a helicity two dominance in the production. They also find a helicity one component due to virtual photons. Their results are in rough agreement with earlier quark model results and with the FESR predictions which obtain somewhat larger widths. The observation of the $\pi^+\pi^-$ angular distributions and the Q^2 dependence in virtual production provide an important test of these models.

C. n_c , χ_c , n_b , χ_b , ...: The production of heavy quark states should be well described through the use of the nonrelativistic Schrodinger bound state picture¹³. The two photon widths may be simply calculated in terms of the properties of the wave functions near the origin which can be determined from other reactions. For example, the two photon width of the pseudoscalar state is simply related to the leptonic width of the vector meson through the relation,

$$\Gamma(\eta_q^{+2\gamma}) = \Gamma(V_q^{+e^+e^-}) \cdot (e_q/e)^2$$

where (e_q/e) is the ratio of the heavy quark charge to that of the electron. In a similar manner, the two photon widths of the χ states are related to their hadronic widths by

$$\Gamma(\chi + \gamma \gamma) = \Gamma(\chi + GG) \cdot (\alpha/\alpha_s)^2 \cdot (9e_q^4/2)$$

The model also makes definite predictions for the helicity structure of the decays. However, it is possible that some of these predictions receive large QCD corrections in higher order.

D. Exotic Particles: Two photon production of the Higgs boson¹⁸ is expected to be quite small due to the small couplings to known fermions and the extremely small induced couplings. It may be possible to see light charged Higgs bosons but they are much more easily seen in annihilation. Similar conclusions must be reached for the production of

possible technicolor bosons¹⁹. Goldberg²⁰ suggests substantial production of glueball states despite their suppressed two photon couplings.

E. The large cross section observed in $\gamma\gamma+\rho^{O}\rho^{O}$, has motivated a number of speculations on resonant structures. These speculations must be consistant with the lack of similar signal in $\pi^{+}\pi^{-}$, etc., final states. Suggestions for resonance explanations range from standard $\bar{q}q$ resonances to glueballs²¹. Nonresonant threshold enhancements are also possible explanations²². The quark composite structure of the ρ^{O} is one such mechanism that has been advocated by Biswal and Misra²³. Further clarification of this interesting effect is clearly needed both experimentally and theoretically.

IV. EXCLUSIVE PRODUCTION

In their pioneering paper, Calogero and Zemach² studied the exclusive production of muon pairs and pion pairs in two photon reactions. Brodsky et al³ made extensive numerical studies of these processes and provided the initial framework for understanding details of exclusive production. A vast amount of early research on exclusive reactions is summarized in the reviews of Terazawa⁶ and Budnev et al⁷. I

will briefly review some aspects of exclusive production by two photons.

- A. QED processes: Lepton pair production provides a test not only of QED but also the EPA and other aspects of two photon production²⁴.
- B. Meson production at low energy: Low energy theorems which follow from chiral symmetry and current algebra provide a systematic procedure for analysing the production of soft pions. The normal parity production is determined from the born terms and current algebra while the abnormal parity production is enhanced by contributions from the anomaly²⁵. While results clean Adler these are theoretically, they have limited applicability due to the importance of resonance structure. A recent attempt to incorporate resonance structure through a proper unitarization procedure is discussed by Mennessier 17. The anomalously large $\rho^{O}\rho^{O}$ production discussed in the previous section may be due to resonance structure or, more likely, due to subtle threshold enhancements.
- C. Charm production: The photon production of open charm states is quite interesting but is expected to be highly

suppressed at current accelerator energies due to the large mass thresholds in the production. Some detailed quark model estimates of the production of $D\overline{D}$, $\overline{D}D^*$, \overline{D}^*D^* have been made by Suaya et al²⁶.

high energy: The exclusive Meson production at production of mesons at high transverse momentum provides a Brodsky and Lepage²⁷ have recently unique test of QCD. argued that these reactions may be factorized into a contribution coming from the hard scattering of the two photons which is calculable in QCD and a contribution which depends on the meson wavefunction in a minimal $Q\overline{Q}$ Fock state. Simplifications occur from the suppression of vector meson dominance effects because of dimensional counting Sudakov effects.

Similar techniques can also be applied the formfactors, Y^*+Y^*M . The transition meson-photon factorization properties can again be applied to give the matrix elements in terms of a perturbatively calculable component and a minimal wavefunction component. These effects are related to the results of meson production in the massive quark model mentioned previously 16.

V. STRUCTURE FUNCTIONS

Two photon processes in the deep inelastic configuration provide a unique probe of the structure of the photon and a sensitive test of QCD. Because of the direct coupling of the photon to quarks, the photon is expected to have a pointlike component in addition to the hadronic component usually described using vector meson dominance (VMD).

The general structure of a hard scattering reaction normally described by a factor representing the hard scattering off the pointlike constituents of the target and a factor representing the distribution of these constituents in the target. In contrast to the hadronic situation, participate directly in the hard target photon can scattering process and must, in some sense, be considered its own constituent. If quarks and gluons are considered as possible pointlike constituents, then the general hard scattering cross-section may be represented by a convolution of the constituent cross-sections with the appropriate constituent distribution functions. For a photon target, we have

 $\sigma_{\gamma} = \tilde{\sigma}_{Q} \otimes Q + \tilde{\sigma}_{G} \otimes G + \tilde{\sigma}_{\gamma}$

where the VMD (or hadronic) components contribute only to Q and G and the pointlike component generating \mathfrak{F}_{γ} as well as possible additional contributions to Q and G.

In the parton model the pointlike component in deep inelastic scattering off a photon target has been identified with the 'box' diagram where a quark, or parton, is exchanged between the real and virtual photons²⁸. The box diagram gives the contribution

$$F_2^{\text{Box}}(x,Q^2) = \sum_{Q} e_Q^4 \cdot P(x) \cdot \ln(Q^2/m^2)$$

and the full structure function has the form

$$F_2(x,Q^2) = F_2^{Box}(x,Q^2) + F_2^{VMD}(x)$$
.

The noted features of box contribution are its sensitivity to the fourth power of the quark charge, the stiff x distribution, P(x), and the dominance of the pointlike component at sufficiently high Q^2 over the scaling VMD component.

In QCD, the quarks and gluons are not free constituents but also have pointlike interactions with each other. The first consistant treatment of the photon structure—function was made by Witten²⁹ using the operator product formalism. In this procedure, the asymptotic freedom of QCD permits the calculation of the hard scattering cross-sections as an expansion in the running coupling constant, $\alpha_{\rm S}$, and the calculation of the Q² evolution of the constituent distributions. This calculation implies the existance of a dominant pointlike component in addition to the normal hadronic terms which reflects the behavior of the box diagram contribution modified by the QCD interactions.

The predictions for the theory are most simply stated in terms of moments of the structure functions,

$$M_n(Q^2) \equiv \int_0^1 dx \ x^{n-2} \ F_2(x,Q^2)$$
 $+a_n/a_s(Q^2)+b_n$ (pointlike) $+\sum_i (a_s(Q^2)d_{ni}(1+\cdots)C_{ni}(hadronic))$
where a_n and b_n are calculable coefficients and the exponents, $d_{ni}=\gamma_{ni}^{0}\geq 0$ are the logarithmic anomalous dimensions of the relevant hadronic operators. The pointlike terms dominate at high Q^2 as the asymptotic freedom implies a vanishing of the running coupling constant,

 $\alpha_{\rm S}(Q^2)$ + $16\pi^2/\beta_{\rm O} \ln{(Q^2/\Lambda^2)}$ + 0 as $Q^2+\infty$. The asymptotic behavior of the moments becomes

$$M_n(Q^2) \rightarrow A_N \cdot \ln(Q^2/\Lambda^2) + B_N + O(1/\ln Q^2)$$
 or for the structure function

 $F_2(x,Q^2) \rightarrow A_2(x) \cdot \ln(Q^2/\Lambda^2) + B_2(x) + O(1/\ln Q^2)$ The asymptotic structure function has the same Q^2 behavior as the lowest order box diagram, but the shape of the x distribution has been modified to reflect the pointlike dynamics of the quarks and gluons (See Figure 1). Similar leading order (in $\alpha_s(Q^2)$) results have been obtained using many different procedures 30 .

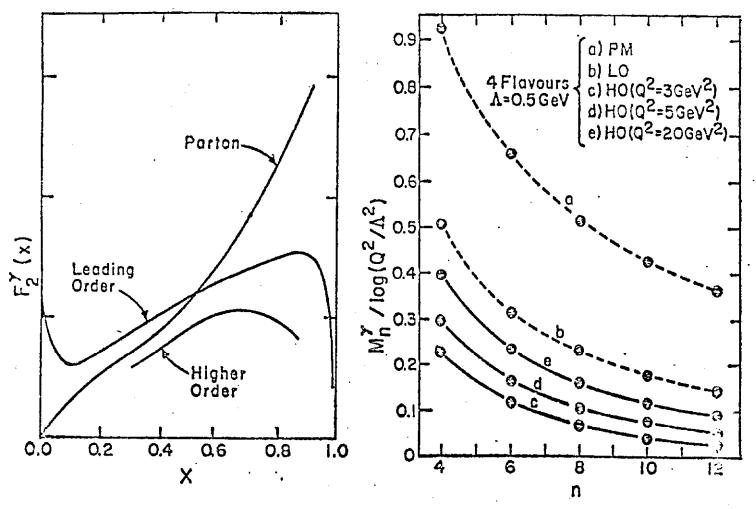


Figure 1. The photon structure function.

Figure 2. Higher order moments.

corrections order pointlike higher to the contribution have also been calculated 31. These corrections involve both the modification of the evolution of $\alpha_{_{\mathbf{S}}}(\mathtt{Q}^2)$ and the computation of the coefficient, b_n. These calculations are necessary if the scale parameter Λ^2 in the definition of to have significance. is These contributions hadronic continue dominate the contributions to asymptotically since all the hadronic anomalous dimensions are positive except for the singlet operators where d_{n-}^{+} o as n+2. The effect of these pointlike corrections on the

structure functions is shown in Figure 1 and, in more detail, for the moments in Figure 2. The prediction is seen to be perturbative for moderate x. An additional suppression of the structure function at large x beyond that found in leading order is evident.

Duke and Owens³¹ emphasize the existance of a strong negative component at small x which forces the structure function negative for sufficiently small values of x. To examine this pathology, they separate the structure function into its valence and sea components,

$$F^{\gamma}(x,Q^2) = \langle e^4 \rangle \cdot F_{\gamma}^{\gamma} + \langle e^2 \rangle^2 \cdot F_{s}^{\gamma}$$
(Valence)

In the valence component, both photons interact with the same quark while the sea component contains all the quark-gluon mixing. The small x singularity occurs only in the sea distribution. This pointlike component mixes strongly with hadronic sea distribution because the anomalous dimensions, d_{n-} , vanishes as n+2, (x+0). Duke and Owens include a standard vector dominance estimate for the hadronic component which leaves the small x behavior singular as seen in Figure 4.

I conclude that the simple higher order analysis should be valid at moderate x, .4 < x < .9, where the perturbative approach seems to converge well. However, the perturbative treatment seems to break down for both small x and large x. A realistic analysis at moderate energies will also require

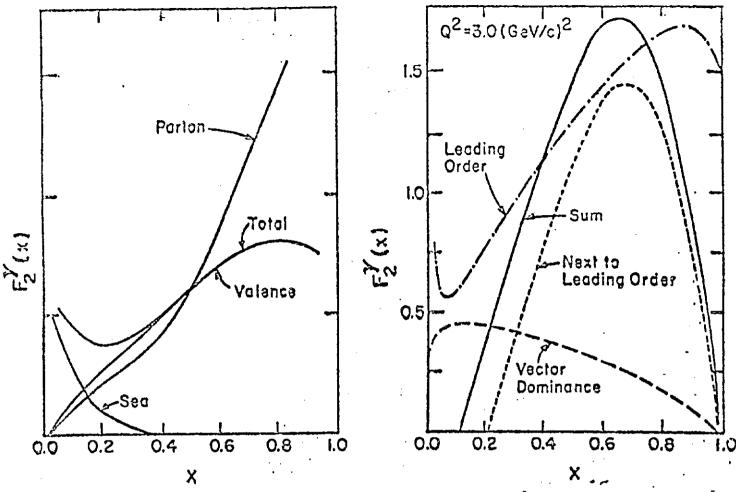


Figure 3. Leading order valencesea distributions.

Figure 4. Higher order structure function.

the proper treatment of mass effects for the heavy quarks such as charm³².

A possible resolution of the x+0 behavior is suggested by the work of Uematsu and Walsh 3 . They study the structure of a virtual photon target. The structure functions are now completely calculable as QCD can be used to evaluate the previously unknown hadronic component. The principal effect they find is the suppression of the QCD corrections particularly those associated with the hadronic operators related to d_n . The negative pointlike contribution of Duke and Owens can be traced to a singular term contained in b_n ,

$$b_n \rightarrow -1/d_{n-} + ---$$

This singularity is compensated by a similar singularity in the hadronic component,

$$c_{n-} + (\alpha_S(P^2))^{-d_{n-}}/d_{n-}$$

Together the contribution to the moment is given by

$$M_{n}(Q^{2}) \sim -\frac{1}{d_{n_{-}}} + \frac{1}{d_{n_{-}}} (\alpha_{s}(Q^{2})/\alpha_{s}(P^{2}))^{d_{n_{-}}}$$

where P² is the mass of the virtual photon target. combination is nonsingular even when $d_{n-}^{\rightarrow 0}$ which occurs as n+2. Hence the asymptotic behavior as $Q^2+\infty$ is not uniform in near n=2 or equivalently, small x. While this cancellation explicit for a virtual photon target, cancellation must occur for a real photon target where $\alpha_{\rm c}({\rm P}^2)$ is replaced by an effective scale which can depend on n but whose precise value is not relevant when d_{n-} is small. Since the entire sea contribution is small except for singularity, once we have determined that the singularity is cancelled by the hadronic sea contribution we should expect remaining sea contribution will be quite small. calculable, nonsingular valence contribution will dominate the higher order corrections for small x as well as for moderate values of x.

The higher order calculations also gives large corrections as x+1. Brodsky and Lepage³⁺ interpret this behavior as a kinematic effect due to the use of improper phase space limits for the K integration in leading order. This interpretation is certainly valid in leading order but there are discrepancies³⁵ in the next order which need clarification. Fortunately these effects are well treated by the higher order perturbative calculation except for x very close to 1.

I have only discussed problems associated with the F_2 structure function. Deep inelastic scattering off a photon target involves four structure functions. The QCD corrections to the longitudinal structure function, F_L , were also computed by Witten²⁹. He found that this structure function scales but is modified slightly from the parton model result.

The polarized structure function F_3 and F_4 have been studied by many groups 3 6 . The F_3 structure function was found to be given correctly by the parton model result. The F_4 structure function behaves in a manner similar to the F_2 structure function with a nonscaling, leading pointlike component. I note that the F_4 structure function involves a "new" set of leading twist hadronic operators which have no proton matrix elements because of the large intrinsic spin required.

Another approach to two photon structure functions outside the context of QCD is that of a massive quark model developed by Preparata³⁷.

Kripfganz and Schiller³⁸ argue that many of the problems associated with determining the photon structure functions in e^+e^- reactions could be avoided by directly measuring the electron structure function. They argue that the electron structure function is "calculable" in a manner similar to the photon structure function. However Caldwell and DeGrand³⁹ argue that the electron structure function is not measurable in the physically interesting region, x_e^+0 .

VI. JETS

Quark and gluon jets are produced by the hard scattering subprocesses. The pointlike component of the photon provides a unique mechanism for jet production. The special features of jets produced in two photon processes were emphasized by Brodsky et al⁴⁰ and were discussed by Kajantie and Raitio⁴¹ from the context of leading log QCD.

An example of these predictions is the expected production of two quark jets via the box diagram in the reaction $e^+e^-+e^+e^-+q\bar{q}$. The jets can be produced cleanly as shown in Figure 5 in contrast to hadronic production where

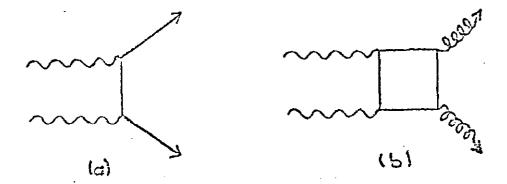


Figure 5. a) two quark jet and b) two gluon jet production.

beam fragmentation plays an essential role. The pointlike contribution is expected to dominate the VMD component and provides a good test of QCD⁺². This process is sensitive to the propagator of the exchanged quark and to the quark charges. The two jet cross-section may be directly compared to the equivalent muon pair cross-section through the ratio,

$$R_{\gamma\gamma} = d\sigma (\gamma\gamma + q\bar{q})/d\sigma (\gamma\gamma + \mu\bar{\mu}) = \Sigma Q_q^4 = 34/27$$

for u, d, s, c quarks. Two clean gluon jets can also be produced through the virtual box diagrams and represent a nontrivial contribution to the two jet cross-section at current energies.

Three and four jet reactions are also interesting as they are produced by more complex QCD mechanisms. Gluonic corrections, VMD contributions, and higher twist effects all play important roles as indicated by Figures 6 and 7. The pointlike terms dominate and the differential cross-section is expected to scale,

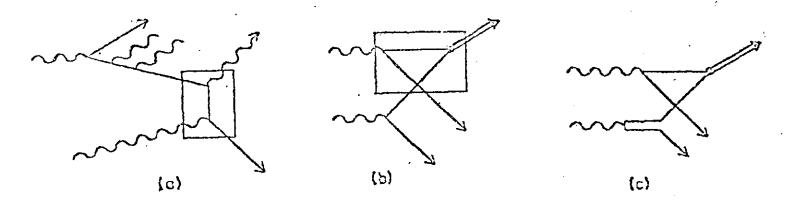


Figure 6. Three jet processes: a) contributions to QCD modification of the structure function b) and c) higher twist contributions.

$$E \frac{d\sigma^{JET}}{d^3P} \sim (P_{\perp})^{-4}F (X_J,Q_J)$$

The dependence on the running coupling constant, α_s , cancels as the explicit factor of α_s in the hard scattering amplitude is cancelled by the $(\alpha_s)^{-1}$ factor in the structure function. These reactions are more sensitive to details such as the spin structure, etc., which can enhance the QCD effects⁴³.

An alternative analysis 4 suggests the use of energy flow, or antenna patterns, to study the implications of QCD for inclusive reactions in two photon processes.

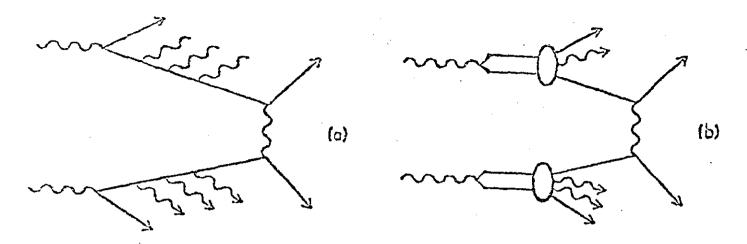


Figure 7. Four jet processes: a) pointlike and b) VMD contributions to quark-quark scattering.

VII. CONCLUSIONS

I have briefly reviewed the many facets of theory which relate to the physics of two photon processes. These range from the variety of mechanisms for resonance production to the detailed QCD calculations for structure functions and jet cross-sections. The experiments are now beginning to provide the precision tests needed to confront these theoretical speculations and to lead to possible new directions in two photon physics.

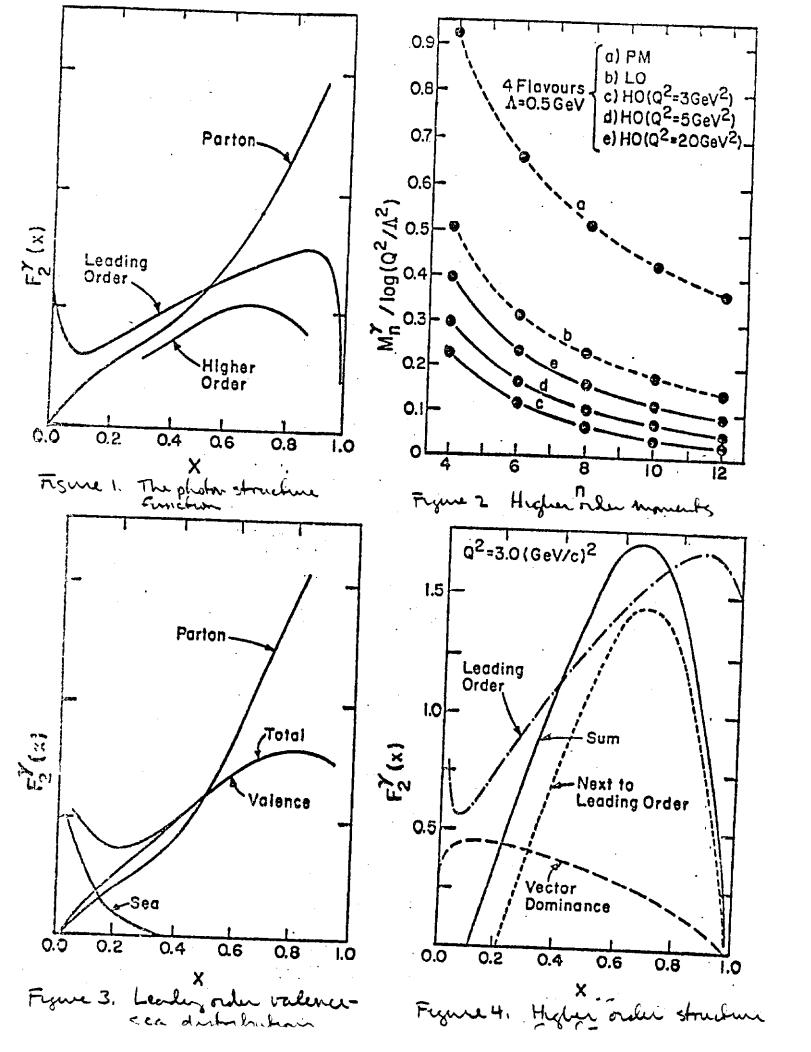
REFERENCES

- 1. F.E. Low; Phys. Rev. 120 (1960) 582.
- 2. F. Calogero and C. Zemach, Phys. Rev. 120 (1960) 1860.
- 3. S.J. Brodsky, T. Kinoshita, H. Terazawa, Phys. Rev. Lett. <u>25</u> (1970) 972; Phys.Rev. <u>D4</u>, (1971) 1532.
- 4. V.E. Balakin, V.M. Budnev, I.F. Ginzburg, JETP Lett. 11 (1970) 388.
- 5. N. Arteaga-Romero, A. Jaccarini, P. Kessler, Phys. Rev. D3 (1971) 1569.
- 6. H. Terazawa, Rev. Mod. Phys. 45 (1973) 615.
- V.M. Budnev, I.F. Ginsburg, G.V. Meledin, V.G. Seibo,
 Phys. Rep. 15 C (1975) 182.
- C.E. Carlson and Wu-Ki Tung, Phys. Rev. <u>D4</u> (1971) 2873;
 R.W. Brown and I.J. Muzinich, Phys. Rev. <u>D4</u> (1971) 1496.
- 9. C. Carimalo, P. Kessler, J. Parisi, Phys. Rev. <u>D20</u> (1979) 1057; Phys. Rev. <u>D20</u> (1979) 2170; Phys. Rev. <u>D21</u> (1980) 669; Proc. Amiens Conf. G. Cochard and P. Kessler, ed. (Berlin, 1980),pg.181; etc.
- 10. G. Cochard, S. Ong; Proc. Amiens Conf. ibid., pq. 202.
- 11. J. Smith, Paris Workshop 1981; J.A.M. Vermaseren, Proc. Amiens Conf. <u>ibid.</u>, pg. 35; J.A.M. Vermaseren <u>et al.</u>, Phys. Rev. <u>D19</u> (1979) 137; etc.

- J.H. Field, Nucl. Phys. <u>B168</u> (1980) 477; see also Proc
 Amiens Conf. <u>ibid.</u>, pg. 248.
- F. Gilman, Proc. Lake Tahoe Conf. (U.C.Davis, 1979),
 pg. 215.
- 14. B. Renner, Phys. Lett. <u>33B</u> (1970) 599 and Cottingham and Dunbar, J. Phys. <u>G5</u> (1979) <u>L155</u>.
- 15. B. Schrempp-Otto, F. Schrempp and T.F. Walsh, Phys. Lett. 36 (1971) 463; P. Grassberger and R. Kogerler, Nucl. Phys. B106 (1976) 457.
- 16. J. Babcock and J.L. Rosner, Phys. Rev. <u>D14</u> (1976) 1786;
 H. Krasemann and J.A.M. Vermaseren, Nucl. Phys. <u>B184</u>
 (1981) 269.
- 17. G. Mennessier, Bonn Conf. 42 (1981).
- 18. G. Kane, Proc. Lake Tahoe Conf. (U.C.Davis, 1979);
 J.A. Grifols and R. Pascual, Z. Phys. C6 (1980) 353.
- J.A. Grifols, Barcelona Preprint (1981).
- 20. H. Goldberg, Phys. Rev. D22 (1980) 2286.
- 21. Goldberg and Weiler, Phys. Lett. 102B (1981) 63; Godbole and Sarma, Bonn Conf. (1981) 63; Layssac and Renard, Montpelier Preprint (1980).
- 22. C. Ayala, A. Bramon, F. Cornet, Bonn Conf. (1981) 115.
- 23. Biswal and Misra, Bonn Conf. (1981) 12.
- 24. J. Smith, Proc. Amiens Conf. (1980) 298.
- 25. Terentjev, Usp-Fiz Nauk. <u>112</u> (1974) 37; Terentjev, JETP Lett. <u>14</u> (1971) 94; S.L. Adler, Phys. Phys. <u>D4</u> (1971) 3497.

- 26. C.E. Carlson and R. Suaya, SLAC Pub.-2483 (1980);
 R. Suaya, Proc. Lake Tahoe Conf. (U.C., Davis, 1979)
 pg.244.
- 27. S.J. Brodsky and G.P. Lepage, SLAC Pub. -2733 (1981).
- 28. T.F. Walsh, Phys. Lett. <u>36B</u> (1971) 121; S.J. Brodsky, T. Kinoshita, and H. Terazawa, Phys. Rev. Lett. <u>27</u> (1971) 280.
- 29. E. Witten, Nucl. Phys. B120 (1977) 189.
- 30. C.H. Llewellyn-Smith, Phys. Lett <u>79B</u> (1978) 83;
 C.T. Hill and G.G. Ross, Nucl. Phys. <u>B148</u> (1979) 373;
 R.J. DeWitt, L.M. Jones, J.D. Sullivan, D.E. Willen, and H.W. Wyld, Phys. Rev. <u>D19</u> (1979) 2046; W.R. Fraser and J.F. Gunion, Phys. Rev. D20 (1979) 147; etc.
- 31. W.A. Bardeen and A.J. Buras, Phys. Rev. <u>D20</u> (1979) 166;
 D.W. Duke and J.F. Owens, Phys. Rev. <u>D22</u> (1980) 2280.
- 32. C.T. Hill and G.G. Ross, Nucl. Phys. B148 (1979) 373.
- 33. Uematsu and Walsh, PL <u>101B</u> (1981) 263; Fermilab Pub.-81/55; see also W.R. Fraser and J.F. Gunion, Phys. Rev. Lett. <u>45</u> (1980) 1138.
- 34. S.J. Brodsky and G.P. Lepage SLAC-PUB-2447 (1979); see also D. Amati et al., Nucl. Phys. <u>B173</u> (1980) 429.
- 35. M.K. Chase, Oxford Preprint 97/80 (1980); W.R. Fraser, San Diego Preprint UCSD-222 (1980).
- M.A. Ahmed and G.G. Ross, Phys. Lett. <u>59B</u> (1975)369;
 K. Sasaki, Phys. Rev. <u>D22</u> (1980) 2143; F. Delduc et al.
 Nucl. Phys. <u>B174</u> (1980) 147, 157; W. Fraser and
 G. Rossi, Phys. Rev. <u>D21</u> (1980) 2710; C. Peterson et al.

- Nucl. Phys. <u>B174</u> (1980) 424; A. Vourdas, J. Phys. <u>G6</u> (1980) 789.
- 37. P. Castorina, G. Nardulli, G. Preparata, Bari Preprint BA-GT-80/1 (1980).
- 38. J. Kripganz and A. Schiller, Karl Marx Preprint, KMU-HEP-80-14 (1980).
- 39. D.O. Caldwell and T.A. DeGrand, Santa Barbara Preprint UCSB-EXP-81-1.
- 40. S.J. Brodsky, T.A. DeGrand, J.F. Gunion, and J.H. Weis, Phys. Rev. Lett. 41 (1978) 672.
- 41. K. Kajantie and R. Raitio, Nucl. Phys. B159 (1979) 528.
- 42. Y.L. Dokshitser, D.I. D'Yakonov, S.I. Troyan, SLAC-Trans-183; J.F. Gunion, Proc. Amiens Conf. (1980) pg.321; F.A. Berends, Z. Kunst, R. Gastmans, Phys. Lett 92B (1980) 186; M.K. Chase, Nucl. Phys. B174 (1980) 109; T.A. DeGrand, Proc. Vanderbilt Conf. (1980); S. Iwao, Lett. Nuovo Cim. 25 (1979) 449, 453 and 26 (1979) 461.
- 43. J.H. Field, Nucl. Phys. <u>B171</u> (1980) 377; J. Kodaira, A. Higuchi, S. Matsuda SLAC-PUB-2695 (1981); J.A. Hassant, D.J. Pilling, Manchester Preprint M/C TH 80/23 (1980).
- 44. M. Abud, M. Dacorogna, R. Gatto, C.A. Savoy, Phys. Lett. <u>84B</u> (1979) 229; M. Abud, R. Gatto, C.A. Savoy, Phys. Rev. D20 (1979) 2224.



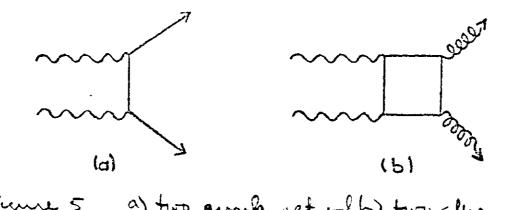


Figure 5. a) two quark jet who) two gluen jet production.

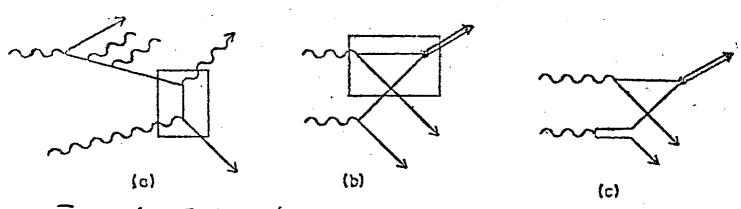


Figure 6. Three jet processes! a) contributions to acs modification of the structure funding, b) and c) higher twist contributions.

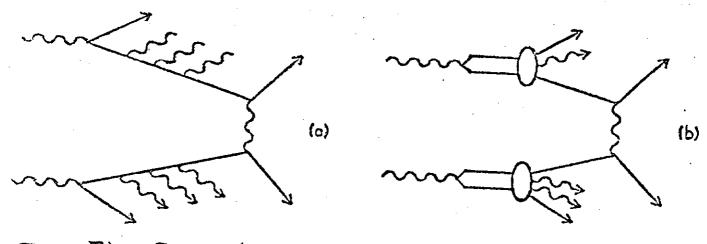


Figure 7) Four jet processes; a) point whe and b) VMO contributions to quark-quark scatterers

