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by

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FORWARD GLORY EFFECTS IN THE ELASTIC SCATTERING OF ¹²C •¹²C

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ABSTRACT

It is shown that the elastic scattering of ¹²C + ¹² **in the center-of-mass energy range 6< E < 31 MeV exhibits forward glory enhancement. Semiclassical analysis of the quantity** $i \tau_{12} = \sigma_R - \frac{1}{2} \left| \frac{-Ruth}{d\Omega} - \frac{eL}{d\Omega} \right| d\Omega$ indicates that the **best car** \rightarrow ate for a 12 C + 12 C interaction potential is a **small-r *.JÍ , deep Hoods-Saxon potential, in qualitative agreemerr- i ith the results obtained from recent analyses of ?£' tone at higher energies.**

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Recently several analyses of elastic and inelastic scattering data of light-heavy ion systems at intermediate energies have been reported . The main conclusion reached has been the removal of some of the major ambiguities attached to the ion-ion optical potential usually extracted from data taken at lower energies. This is accomplished at intermediate energies because of the incipient dominance of the farside amplitude over the nearside one²⁾, thus leading to a greater degree of sensi**tivity to the details of the ion-ion interaction at shorter separation distances.**

In a parallel theoretical development³⁾, the **observation has been made that the extraction and analysis of the forward glory contribution to tne elastic scattering, would also furnish further constraints on the interaction potential. It has been suggested in Ref. 3 that a careful study of the quantity**

$$
\Delta \sigma_{\mathbf{R}} = \sigma_{\mathbf{R}} - \int d\Omega \left[\frac{d\sigma_{\mathbf{R}}}{d\Omega} + \frac{d\sigma}{d\Omega} \right]
$$
 (1)

where σ_p is the total reaction cross section, $\frac{10}{40}$ the elastic **differential cross section and —^ t h > , the differential Rutherford cross section, can supply the above mentioned constraint. This comes about as a consequence of the optical** theorem which relates $\Delta \sigma_R$ to the imaginary part of the forward **"nuclear" scattering amplitude viz**

$$
\Delta \sigma_{\mathbf{R}} = \frac{4 \pi}{k} \operatorname{Im} [f_{\epsilon 0} - f_{\mathbf{R} u t h}(\epsilon)] \tag{2}
$$

where f and f_{Ruth} are the total and Rutherford scattering **amplitudes, respectively and k is the asymptotic wave number**

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of relative motion. The occurence of forward glory, a refractive effect, leads to a major enhancement in $\Delta \sigma_p$.

In this letter, we present evidence for the forward glory enhancement in $\log_{\rm R}$ for the scattering of ¹²C on ¹²C in the energy range $6 < E_{cm} < 31$ MeV.

We have determined the quantity $\Delta\sigma_p$ from existing experimental data on the total reaction cross section, σ_p , and **published values of the sum-of-differences cross section, r** rdo_m do 7 da

 $\sigma_{\text{SOD}} = \int d\Omega \left[\frac{d\Omega}{d\Omega} - \frac{d\Omega}{d\Omega} \right]$ where $\frac{d\Omega}{d\Omega}$ is the Mott cross section. The total reaction cross section $\sigma_{\mathbf{p}}$ is obtained from

the sunned contribution of the complete fusion cross section, o_ , and the total, angle-integrated, cross section of direct processes $\sigma_{\mathbf{n}}$. **Recently Kolata et al.**⁵⁾ measured the total α yield

in the 12 C + 12 C fusion. The contribution to σ_p arising **from the 3a evaporation, not taken into account in previous fusion measurements, was determined. An anomalous a yield,** which seems to be a direct process, was included in $\sigma_{\mathbf{n}}$. We used σ_R from Kolata's work⁵⁾, and calculated the σ_R from other fusion measurements^{6,7,8} summing to them the 3α evaporation, and considered $\sigma_{\mathbf{n}}$ as composed of the total **5 9) angle-integrated inelastic cross section ' and the anomalous a yield⁵*.**

The quantity σ_{SOD} was constructed by Treu et al.¹⁰⁾ **and more recently by Ledoux et al. from the measured elastic scattering angular distributions. The quantity of interest in** this letter, $\Delta \sigma_{\text{b}}$, was then evaluated, as indicated in Eq. (1), $name{1y}$ $A\sigma_R = \sigma_R - \sigma_{SOD}$.

Owing to the dispersion inherent in both σ_p and $^{\circ}$ **s**OD , we present our $^{\circ}$ $^{\circ}$ $^{\circ}$ as a band,whose width is much **smaller than its mean value. This band of points representing**

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Ao_ , is plotted in Fig. 1 vs. the center of mass energy. One sees clearly the beginning of the oscillatory behaviour expected from the theoretical study of Ref. 3). To ascertain the refractive nature of $\Delta\sigma_p$ **, we show in the figure** $\Delta\sigma_p$ **calculated** \sim 121 and \sim 121 **12)**

$$
\Delta \sigma_{\mathbf{R}}^{S.C.} = \frac{2\pi}{k^2} \sum_{\ell=0}^{\ell_c} (2\ell + 1) \cos 2\sigma_{\ell} \tag{3}
$$

where σ_p is the ℓ -Coulomb phase-shift and ℓ_c is the sharp **cut-off angular momentum that specifies the value of the total reaction cross section through** $\sigma_p = \pi/k^2 (l_a+1)^2$ **.**

We consider as a criterion for the refractive enhancement in $\Delta \sigma_{p}$ due to forward glory scattering, the **enhancement in Aa_ due to forward glory scattering, the**

$$
\frac{\Delta \sigma_{\rm R}}{\Delta \sigma_{\rm R}^{3.0}} > 1 \tag{4}
$$

which is clearly satisfied by the $C + C + C$ $C - AC$ _p data shown **in Pig. 1 .**

It has been pointed out in Ref. 3) that different optical potentials that give similar reasonable fits to the ratio to Rutherford scattering at small angles, may give quite different Ao's . Thus through the confrontation of the calculated $\Delta\sigma_p$ with the experimental one, a less ambiguous optical potential may be deduced¹³⁾. We have tested this idea **12 12 on our C+ C case. We have considered two optical potentials that both generate forward glory scattering namely the corresponding classical deflection function 8(1) passes through zero at a finite value of** l , $l_{\alpha l}$.

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The first optical potential we considered in our analysis is the one suggested by the Yale group¹⁴⁾. This Saxon-**Woods potential, whose parameters are,** $V = 14$ **MeV,** $a_{-} = 0.35$ **fm,** r_v = 1.35 fm, W = 0.4+0.1 E_{CM} (MeV), a_w =0.35 fm, r_w = 1.40 fm, **reproduces reasonably well the elastic scattering angular distributions of ¹² C *¹ *C and accounts for the structure seen in the excitation function at 90[°]. We calculated** $\Delta \sigma_{\bf p}$ using the Ford-Wheeler¹⁵⁾, stationary-phase approximation, which **gives**

$$
\Delta \sigma_R = \frac{4 \pi}{k^2} (l_{g_1} + l_2) \left[\frac{2 \pi}{\frac{d\theta}{d\ell}} \right]^{l_2} |S^n_{g_{g_1}}| \sin \left[z (r_{g_2} + r_{g_2}^n) - \frac{\pi}{4} \right]^{(5)}
$$

where $\delta_{\mathbf{q}\ell}$ is the nuclear phase shift evaluated at the forward glory angular momentum, $\ell_{g\ell}$, , and $s_{\ell_{g\ell}}^{n}$ is the reflection coefficient at $\ell_{\alpha\ell}$. We have found that the reflection coefficient $\begin{bmatrix} \mathbf{S}^{\mu}_{\ell} & \mathbf{f} \end{bmatrix}$ for the Yale potential very close to unity
in the energy range of interest. Further, the effect of absorption on $\ell_{\alpha\beta}$ was found to be small too. This convinced us that the use of a classical deflection function is more than **us that the use of a classical deflection function is more than adequate. The nuclear phase shift 5ⁿ is a rapidly varying function of I in the forward glory region. However its value at** α of α , α has shown us.

has shown us. potential, using a classically generated θ and $\ell_{q\ell}$ and ignoring $|S_{\ell}^{n}|$ and $\delta_{g\ell}^{n}$, is shown in Pig. 1 as the dotted curve. We see clearly that the magnitude of $\Delta\sigma_{\mathbf{p}}$ comes out right, however there is a major discrepancy in the phase. We have also calculated $\Delta \sigma_p$ for a potential tailored according **to that obtained from the analysis of the intermediate-energy data; a rather small-radius deep Saxon-Wood interaction. He have taken V = 250 MeV , ry = 0.66 fm and** *ay* **= 0.63 fm 1a) . The result is presented in Fig. 1 as the full curve. The agreement with the general trend of the data is striking. This agreement with the behavior of the data is made meaningful by the fact** that the elastic scattering angular distribution with this real potential and with $W = 0.4 + 0.3E$ (MeV), $r_w = 0.93$ fm, $a_w = 0.35$ fm, is coming out as reasonable **as the one obtained witn the Yale Potential, as clearly seen in Fig. 2 .**

The fact that $\Delta \sigma_p$ is acting as a filter to the **appropriate optical potential that best represents the interacting system would be understood easily by the fact that** *•tt* **(9) probes a certain combination of the optical potential** parameters, whereas $\Delta \sigma_p$ tests a different combination. This **situation becomes quite clear at higher energies where the** forward glory impact parameter, $b_{q\ell} = \ell_{q\ell}/k$, becomes independent of energy¹⁶⁾

$$
b_{3l} = R_v \Big[1 + \frac{a_v}{2R_v - 3a_v} \Big(3 \ln R_v + \ln \Big(\frac{2a_v}{\pi} \Big(\frac{v}{2, \overline{2} \epsilon^2} \Big)^2 \Big) \Big] \qquad (6)
$$

and the slope of $\frac{d\sigma}{d\Omega}$ (θ) in the drop-off region (the region of the quarter-point angle) is determined basically by^{2,17)}

$$
l_{o} = 2 k a \left[\pi - \text{Arctan} \frac{W}{V} \right]
$$
 (7)

if an equal-geometry for W(r) and V(r) is assumed. Therefore the two equations above furnish two invariants for $\frac{d\sigma}{d\theta}$ (θ) and **AoR , supplying, thus, important constraints on the parameters of the ion-ion interaction, as our calculation clearly indicate**

(see Figs. 1 and 2). Though not quite applicable at the low energies we are considering, Eqs. (6) and (7) do supply two reasonable qualitative constraints.

In connection with the deep potential that gave the best account of $A\sigma_{\bf p}$, it is important to stress that exactly **this type of potential is seen to emerge froa the analysis of intermediate energy data. At these higher energies a remnant of a nuclear rainbow scattering (scattering to negative angles) is seen to occur. At the low energies considered in this letter, our deep potential generates strong orbiting situation,** which would persists up to a critical energy given a proximately bv^{17}

$$
E_{cr} = \frac{V_e(\mathbf{r}_v)}{2} + \frac{V}{8 a R_v} \left[\left(R_v - 2 a_v \right)^2 + 2 a_v^2 \right]
$$
 (8)

where V_{α} (R) is the Coulomb interaction at the nuclear potential **radius R. Using the parameters of our potential, V =250 MeV,** $r_{\text{v}} = 0.66$ fm, $a_{\text{v}} = 0.63$ fm, we obtain $E_{\text{c}} = 72$ MeV, well above the **energy at which our collected data point enu. It would be quite interesting to extend the present study to energies higher** than $E_{\alpha r}$, where both nuclear rainbow and forward glory would be acting.

In conclusion, we have presented in this letter, strong evidence for the forward glory scattering phenomenon in the 12 C + 12 C system, as exemplified by the enhancement and oscillation in $\Delta \sigma_p$. To our knowledge, this is the first time that such a phenomenon has been "seen" in nuclear heavy ion scattering¹⁸⁾. We have clearly shown that a joint analysis of both $\frac{d\sigma}{d\Omega}$ and $\omega \sigma_R$ reveals a less ambiguous interaction potential. The 12 C + 12 C potential we obtained from our

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analysis is quite deep and resembles closely the interaction potential deduced from analysis done on the elastic scattering of $12c + 12c$ at intermediate energies (E - $\frac{15 \text{ MeV}}{N}$) and that **19) calculated from the double folding model**

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$$
\Delta \sigma_{R}^{S.C} \cong \frac{2 \sigma_{R}}{1 - \eta^{2}} \left[\cos \left[-2 C \eta + 2 \eta \ln \left(l_{c} + \frac{1}{2} \right) \right] + \eta \sin \left[-2 C \eta + 2 \eta \ln \left(l_{c} + \frac{1}{2} \right) \right] \right]
$$

where C » 0.5772156649 (Euler's constant) and n is the Sommerfeld parameter. The above expression gives the magnitude of Aa»*⁰' quite accurately and tends to the correct limiting value $2\sigma_p$ at very high energies $(n + 0)$.

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- **FIG.** 1 The quantity $\Delta \sigma_{\mathbf{R}}$ for the $\frac{12}{c}$ + $\frac{12}{c}$ system, with the Yale potential $V = 14$ MeV, $r_y = 1.35$ fm, **av = 0.35 fm (dotted curve), the small-radius, deep interaction, V = 250 MeV**, $r_{\text{w}} = 0.66$ fm, $a_{\text{w}} = 0.63$ fm **(full curve) and the sharp cut-off limit, Eq. (3) (dashed curve). The data points were extracted from Refs. 5) (open triangles), 6) (open circles), 7) (full** circles) and 8) (full triangles), using σ_{conn} from **ref. 10) and 11).**
- **FIG. 2 The elastic scattering angular distribution for** $12C + 12C$ at three center of mass energies¹¹. The theoretical curves were obtained with the Yale potential (see caption to fig.1) with $W = 0.4 + 0.1$ E_{cm} (MeV), $r_{\text{cs}} = 1.40$ fm, $a_{\text{cs}} = 0.35$ fm (dashed curve), and with the small radius, deep potential of fig. 1 with $W = 0.4 + 0.3 E_{CM}$ (MeV), $r_{cs} = 0.93$ fm and $a_{cs} = 0.35$ fm w - 0.35
V - 0.31 Fm and a state of the detail and a state of the where you went to you you with the latter potential is slightly smaller than the experimental value. The values of $|S_{\ell_{\alpha\beta}}|$ in both eases come out close to unity.

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 $Fig. 2$

 $Fig. 1$

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