

## HYDRO-ELASTIC STUDY OF INSTABILITY OF THE COOLING CIRCUIT OF SUPERPHENIX

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Summary : To deal with problems of hydro-elastic vibrations encountered during the start up of SUPERPHENIX, the L.N.H. has designed an approach which combines a physical scale model and in parallel a hydro-elastic analytical study.

Very low frequency vibrations whose intensity exceeded that forecast were detected during the initial sodium tests of the SUPERPHENIX reactor, the appearance of these phenomena was linked to loading the water of the cooling circuit of the main vessel.

The studies started by the L.N.H. had a twofold aim : on the one hand, to confirm the origin of the phenomena observed on the reactor and find ways to eliminate the vibrations and on the other hand, to understand the phenomenon and determine the threshold values of the parameters which trigger instability, two courses were followed simultaneously for this purpose :

- the construction of a physical model, scale : 1/4 (E.P.O.C) and,
- analytical study of the hydro-elastic coupling, putting the phenomenon into equation form and then solving them numerically.

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EDF.  
L.N.H.

### CONTENTS:

- Introduction
- Scale model E.P.O.C. (video)
- Analytical study
- Conclusions .

## SIMILITUDES:

### HYDRAULICS

- Reynolds number (turbulent flow)
- Froude number (gravity waves)

$$\Rightarrow \begin{aligned} &\rightarrow \text{geometrical scale } \hat{L} = \frac{1}{4} \quad (\text{for long. dimension}) \\ &\rightarrow F_r = \frac{V}{\sqrt{gL}} \quad \rightarrow \hat{V} = \hat{L}^{1/2} \\ &\rightarrow \hat{Q} = \frac{1}{32} \quad \hat{t} = \frac{1}{2} \end{aligned}$$

- The discharging crest is made of tin without distortion in thickness (for hydraulics reasons)

$$\frac{\hat{E}}{\hat{P}_e \hat{L}} = 1,01$$

- The shell is made of aluminium with a slight distortion of its thickness to respect a simplified similitude

$$\frac{\hat{E}}{\hat{P}_e \hat{L}^4} = 1 \quad (\text{membrane phenomena are negligible})$$

$\hat{h}$

$h = \text{thickness of the shell}$

### HYDRO-ELASTICS

$$\rightarrow \frac{E}{P_e V^2} \quad E = \text{Young Elasticity number}$$

$$\rho V^2 = \text{kinetic energy of the flow}$$

$$\rightarrow \frac{f_s}{P_e}$$

- $$\Rightarrow \begin{aligned} &\rightarrow \text{find a material with an Young elasticity number around } 4000 \text{ kg/mm}^2 \\ &\rightarrow \text{Tin is quite adequate but not for all of the shell.} \\ &\rightarrow \text{The shell is therefore built in two part.} \end{aligned}$$

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## SUPERPHENIX

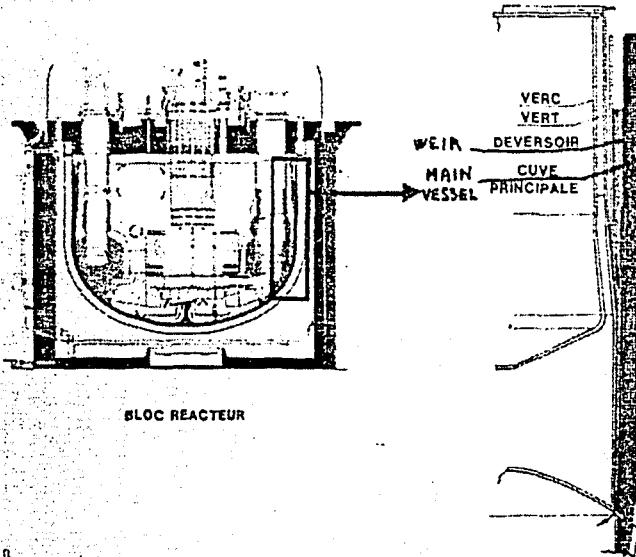
Detection of Hydro-Elastic vibrations

Physical scale-model  
E.P.O.C.  $\frac{1}{4}$

- confirm the origin
- find ways to deal with fluctuations
- understand the phenomena
- study the parameters

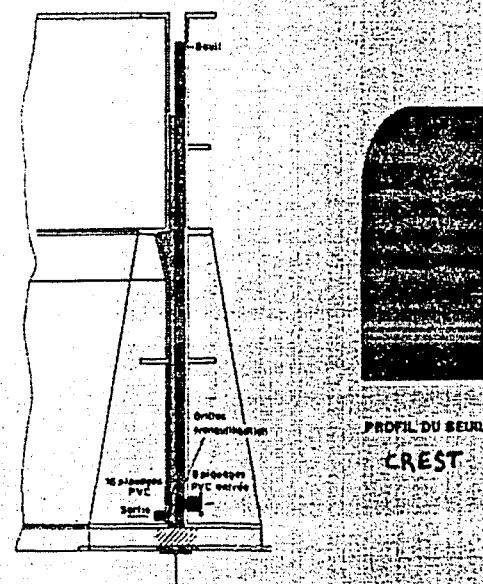
### E.D.F. STUDIES ON THE COOLING

#### CIRCUIT OF SUPERPHENIX



**REACTEUR SUPERPHENIX**

SITUATION DU CIRCUIT DE REFROIDISSEMENT  
DE LA CUVE PRINCIPALE



**MODELE E.P.O.C.**

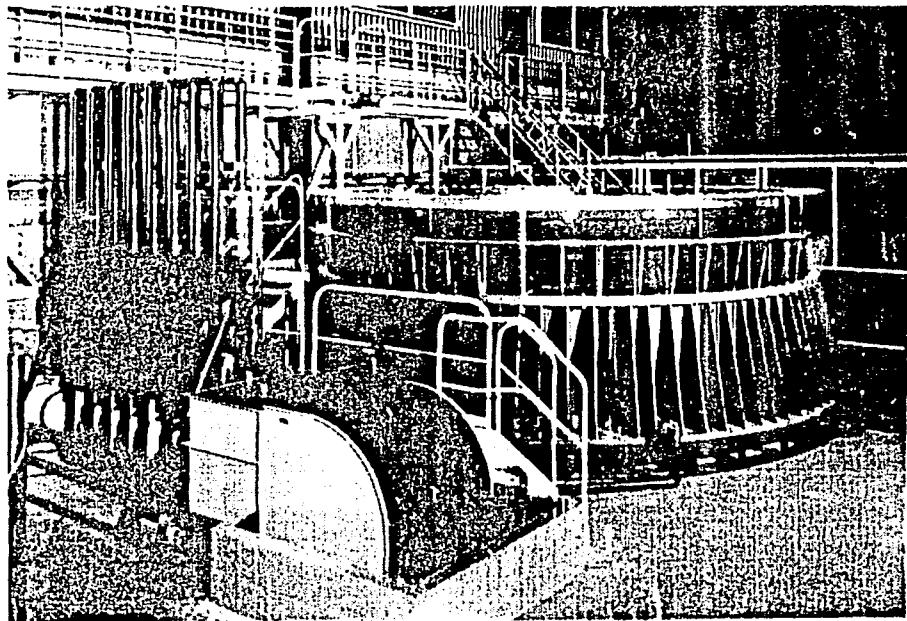
E.P.O.C. MODEL

SCALE  $\frac{1}{4}$

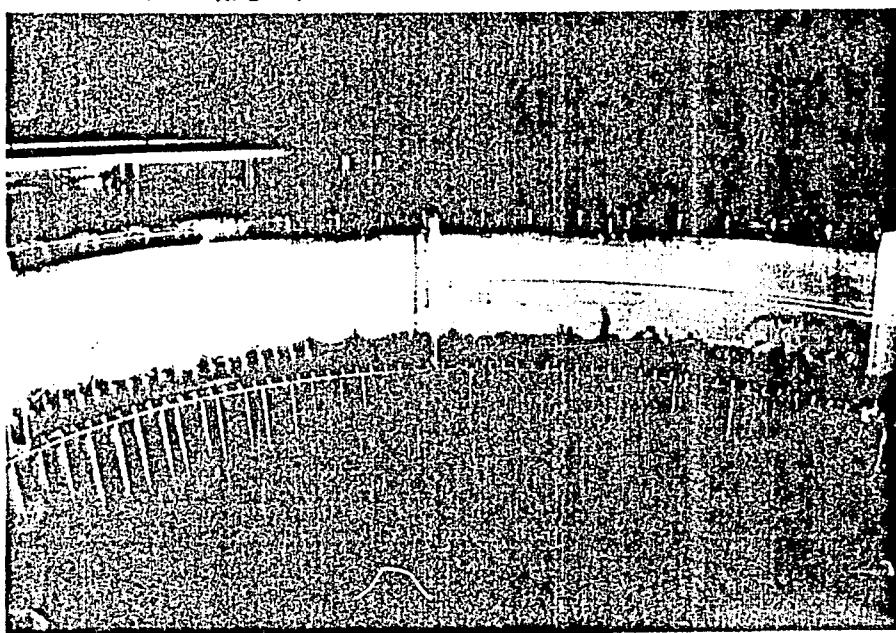
**ETUDE DES PHENOMENES ONDULATOIRES DANS LES COLLECTEURS DE SUPERPHENIX**  
(**MODELE E.P.O.C.**)

MODELLING THE GEOMETRY OF THE REACTOR FOR THE EPOC MODEL



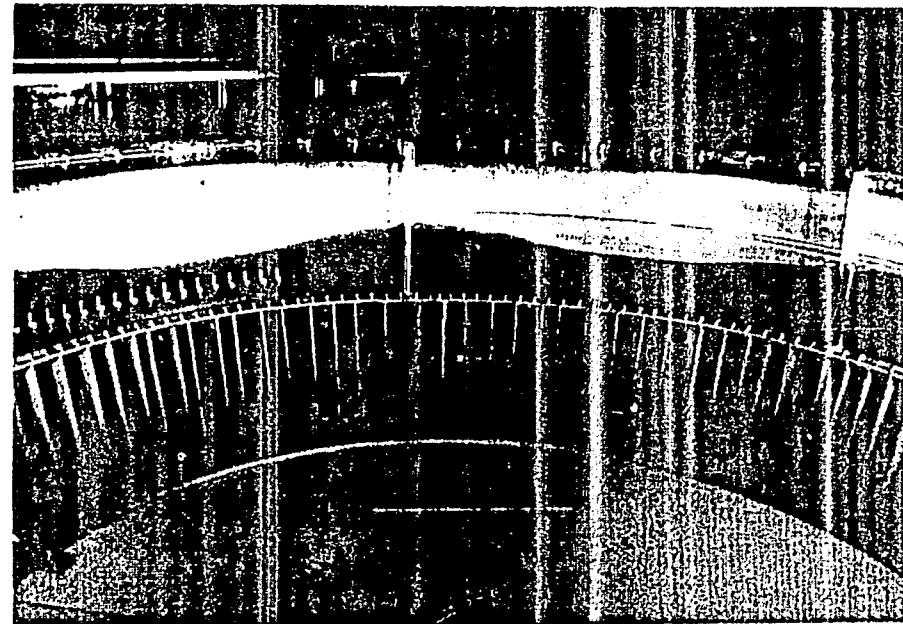


GENERAL VIEW OF THE EPOC SCALE MODEL

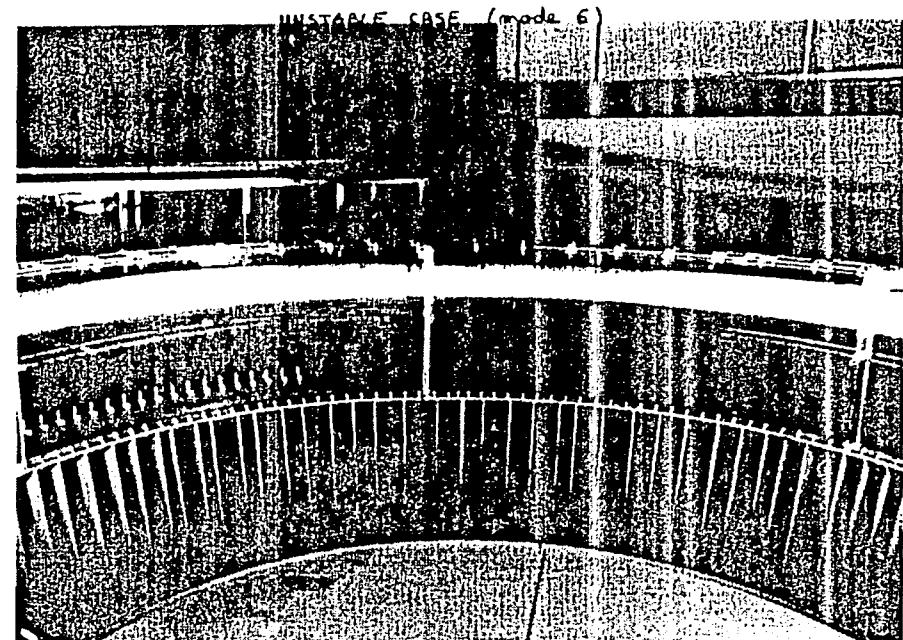


UNSTABLE CASE (fast mode)

DER  
EPOC



Cas instable 20 l/s, 45 cm de hauteur de chute



STABLE CASE  
Cas stable 30 l/s, 15 cm de hauteur de chute

VISUALISATION DES SURFACES LIBRES MODELE EPOC (2ème phase d'essais)

DISPLAY OF FREE SURFACES EPOC SCALE MODEL

DER  
M 1  
EPOC

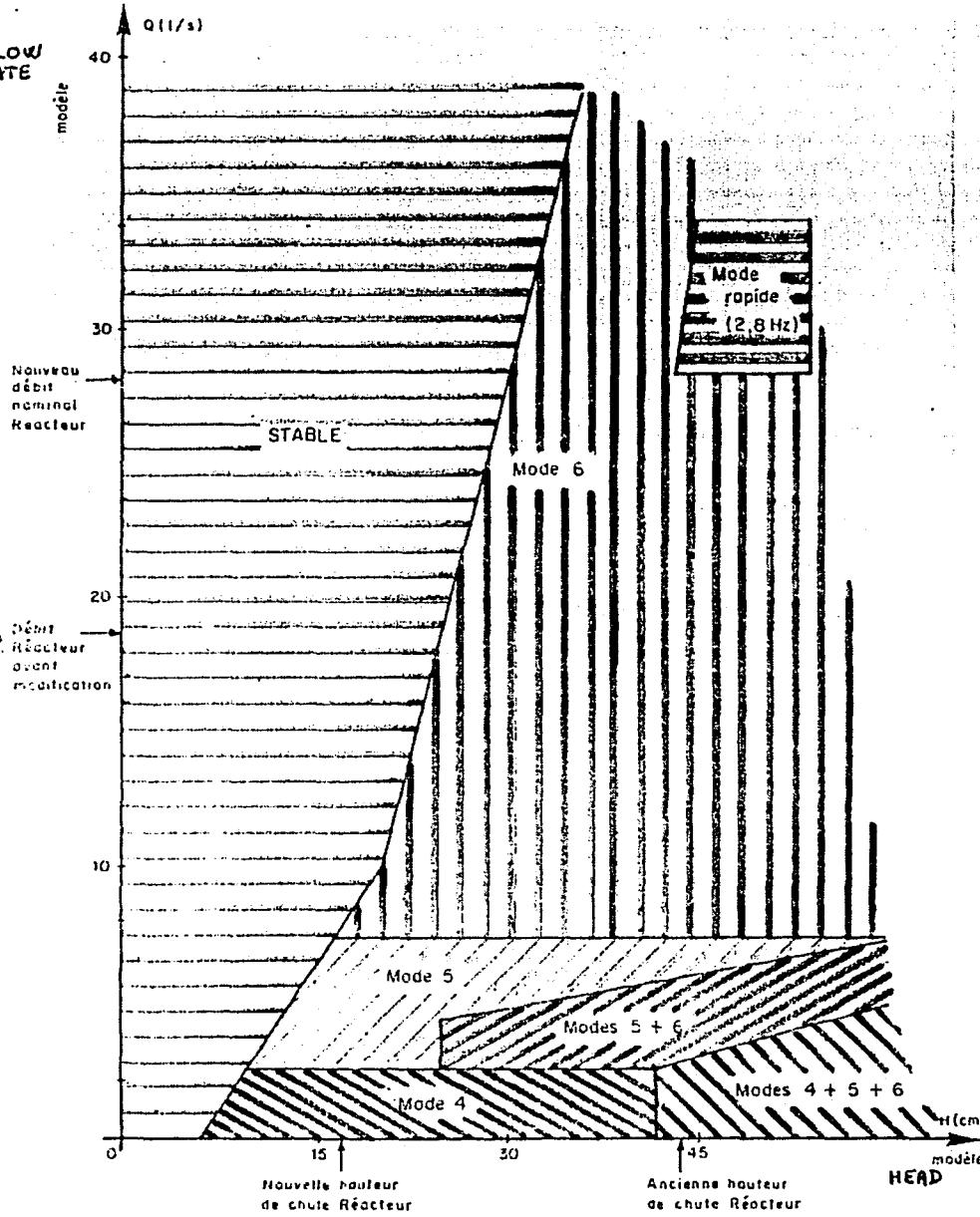


Figure 9 : Zones de stabilité et d'accrochage des différents modes (2ème phase d'essais)

STABILITY AND ESTABLISHMENT ZONES OF THE  
DIFFERENT MODES



$$\frac{d^2 \tilde{E}_{in}}{dt^2} \cdot e_1 = \frac{d\tilde{E}_{in}}{dt} \left( \frac{1}{2} g \frac{1}{2} h_1 U_1^2 + e_1 \tilde{U}_1 \right)$$

$$= \frac{\tilde{U}_1^2}{2} h_1^2 U_1^2 + \frac{1}{2} h_1^2 U_1^2 + e_1 \tilde{U}_1$$

$$= \frac{1}{2} h_1^2 U_1^2 + e_1 \tilde{U}_1$$

avec  $h_1 = 20 \text{ (cm)}$

UPSTREAM LEVEL

$$\frac{d^2 \tilde{E}_{in}}{dt^2} e_2 = \frac{d\tilde{E}_{in}}{dt} (e_2 \tilde{U}_2)$$

$$= \tilde{E}_{in} (e_2 \tilde{U}_2)$$

$$= \frac{d^2 \tilde{E}_{in}}{dt^2} h_1 = \frac{d^2 \tilde{E}_{in}}{dt^2} \frac{1}{2} h_2$$

$$= \frac{d\tilde{E}_{in}}{dt} (h_1 \frac{h_2}{h_1} \tilde{U}_2)$$

$$= \frac{d\tilde{E}_{in}}{dt} \left( \frac{1}{2} g \frac{1}{2} h_1 U_1^2 \right)$$

$$= \tilde{E}_{in} \frac{1}{2} \frac{h_2}{h_1} g \frac{1}{2} h_1 U_1^2 \frac{1}{2} h_1 \tilde{U}_1$$

avec  $h_2 = 20 \text{ (cm)}$

DOWNSTREAM LEVEL

(22)

(23)

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$$\frac{d^2}{dt^2} \left( \frac{r_1^2}{r_2^2} \right) = \frac{1}{r_1^2} \left( \frac{r_1^2}{r_2^2} - \frac{1}{r_2^2} + \frac{r_1^2}{r_2^2} \right) -$$

$$- \frac{d^2}{dt^2} \left( r_1 \frac{r_1^2}{r_2^2} + \frac{r_1^2}{r_2^2} \right) = \sqrt{\frac{r_1}{r_2}} \quad (\text{perturbation})$$

$$- \frac{d^2}{dt^2} \left( r_1 \frac{r_1^2}{r_2^2} + \frac{r_1^2}{r_2^2} \right) \rightarrow \left( \text{perturbation déphasée} \right)$$

$$- \frac{d^2}{dt^2} \left( r_1 \frac{r_1^2}{r_2^2} + \frac{r_1^2}{r_2^2} \right) \rightarrow \left( \text{perturbation} \right)$$

$$- \frac{d^2}{dt^2} \left( r_1 \frac{r_1^2}{r_2^2} + \frac{r_1^2}{r_2^2} \right) \rightarrow \left( \text{rigidité} \right)$$

$$- \epsilon_{10} \frac{1}{r_1^2} r_1 + \frac{1}{2} r_1 \frac{1}{r_2^2} r_1^{1/2} \frac{r_1}{r_2}$$

$$- \epsilon_{10} \frac{1}{r_1^2} r_1 + \frac{1}{2} r_1 \frac{1}{r_2^2} r_1^{1/2} \frac{r_1}{r_2}$$

$$- \frac{d\epsilon_{10}}{dt^2} \frac{1}{r_1^2} r_1$$

$$+ \epsilon_{10} \frac{1}{r_1^2} r_1$$

$$\text{avec } r_1 = \frac{\sin(\frac{t}{T} \pi)}{\sin(\frac{T}{2} \pi) \cdot \sin(\frac{t}{T} \pi)}$$

$$\text{et } r_2 = \frac{\sin(\frac{t}{T} \pi) - 1}{\sin(\frac{T}{2} \pi) \cdot \sin(\frac{t}{T} \pi)}$$

Equation of the shell movement.

27.

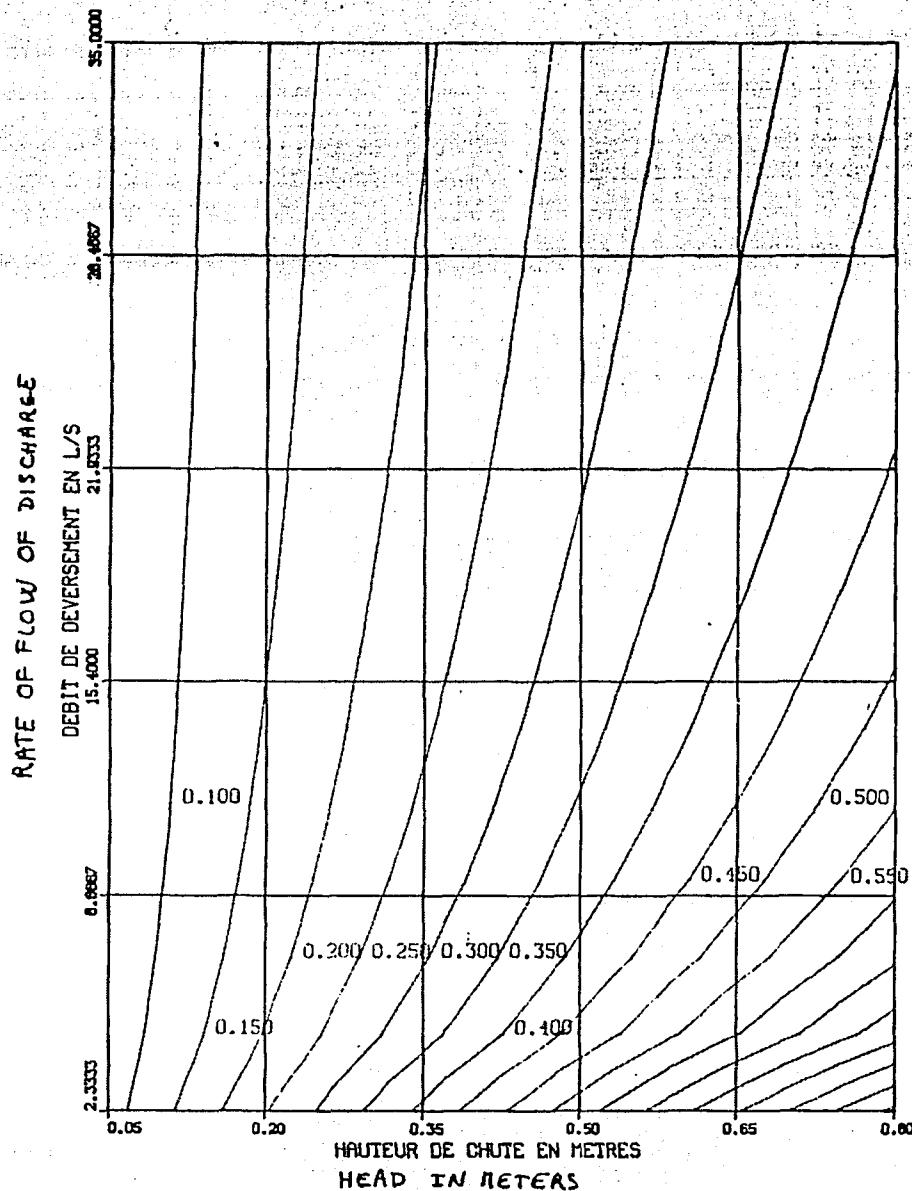


Fig:14

CALCUL ANALYTIQUE DU MODELE EPOC  
ISO-TEMPS DE CHUTE EN SECONDES  
ANALYTICAL COMPUTATION OF THE EPOC MODEL  
ISO-FALL TIME IN SECONDS

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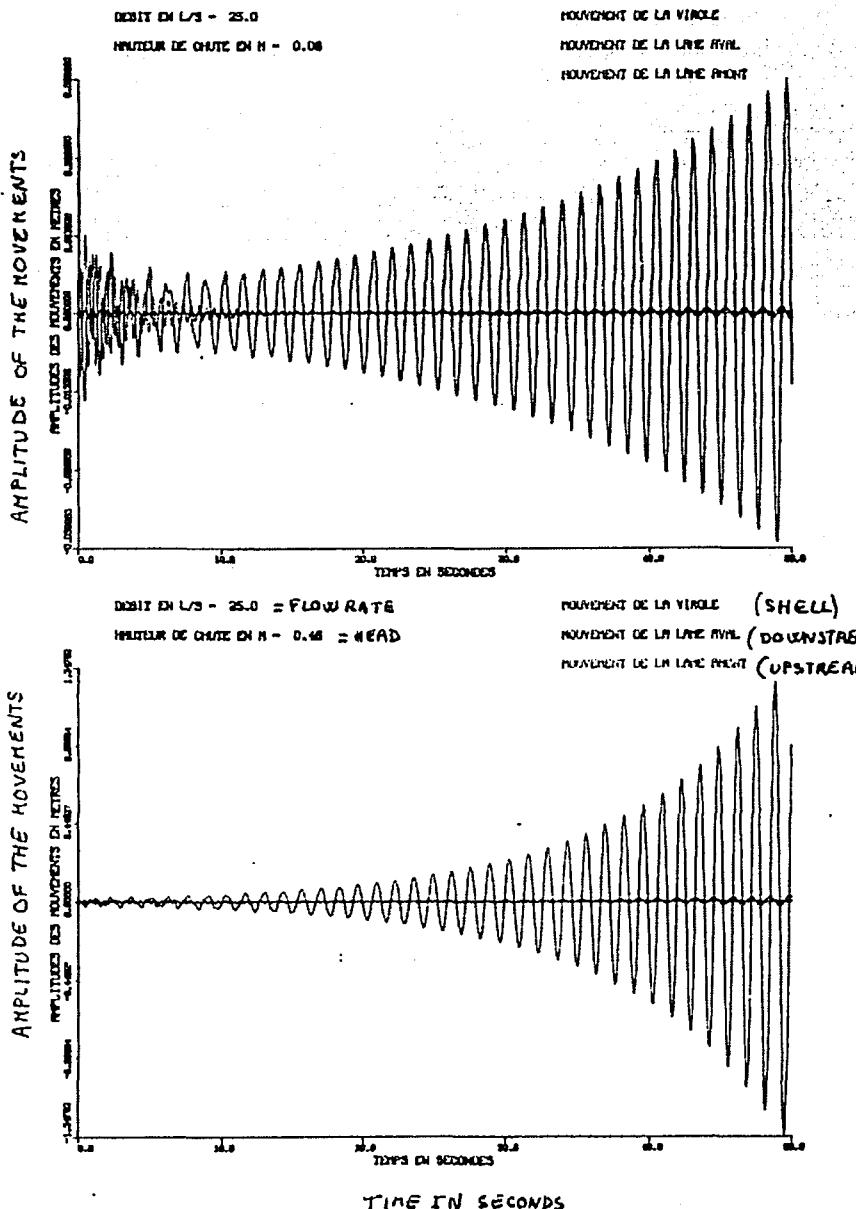


Fig :15 AMPLITUDES DES MOUVEMENTS  
CALCUL SEMI-ANALYTIQUE SANS AMORTISSEMENT

AMPLITUDE OF MOVEMENTS  
SEMI-ANALYTICAL COMPUTATION WITHOUT ABSORPTION

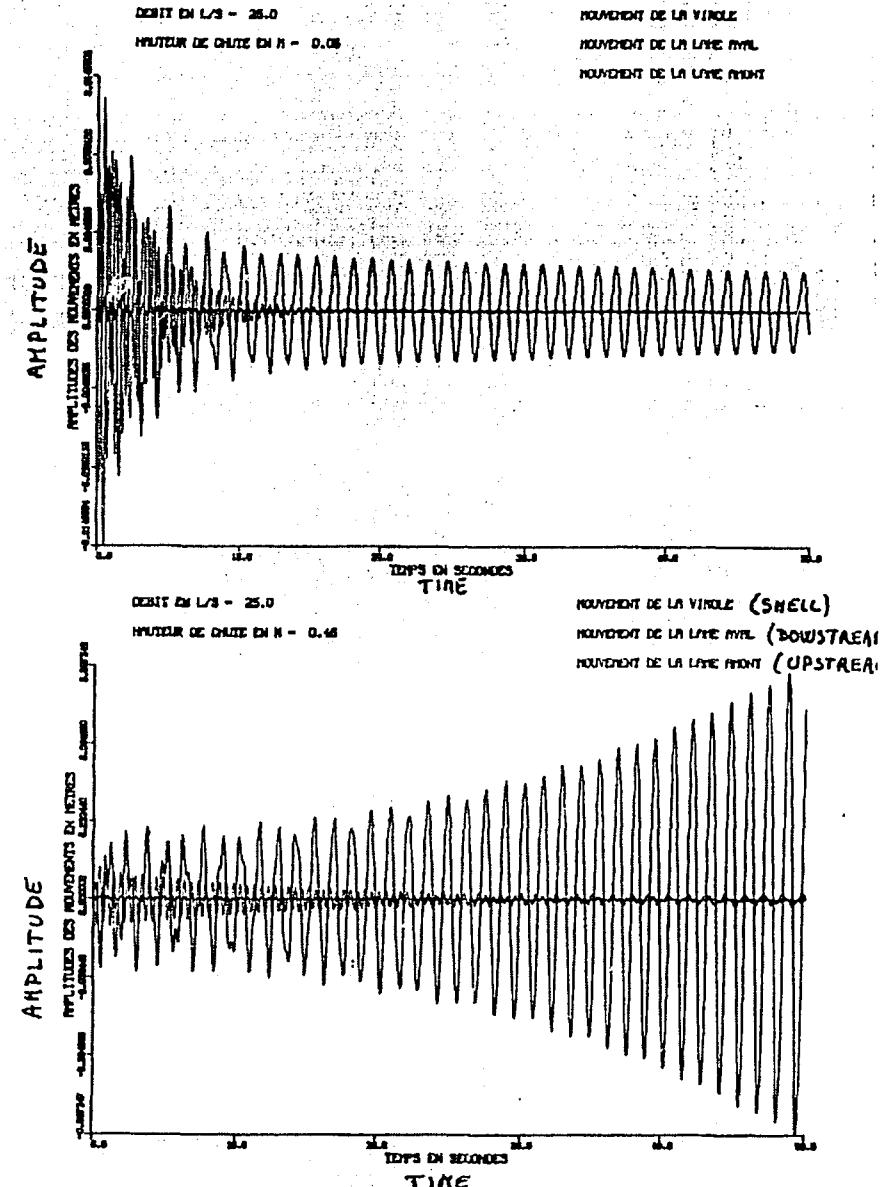


Fig :16 AMPLITUDES DES MOUVEMENTS  
CALCUL SEMI-ANALYTIQUE AVEC AMORTISSEMENT  
AMPLITUDE OF MOVEMENTS  
SEMI-ANALYTICAL COMPUTATION WITH ABSORPTION

CONCLUSIONS:

THE EPOC PHYSICAL SCALE MODEL IN HYDRO-ELASTIC SIMILITUDE  
WITH THE RELEVANT ZONE OF SUPERPHENIX HAS UNCOVERED  
A PHENOMENON OF CLOSE COUPLING BETWEEN FLUID AND  
STRUCTURE, AND HAS ENABLED THE MAIN HYDRO-ELASTIC  
CHARACTERISTICS OF THE PROBLEM TO BE GRASPED.

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Simplified SEMI-ANALYTICAL MODEL IS USED AS A  
THEORETICAL APPROACH OF THE PROBLEM. THE MODEL  
CLEARLY PROVES THE EXISTENCE OF HYDRO-ELASTIC INSTABILITY,  
AND DETERMINES THE THRESHOLD VALUES OF THE  
PARAMETERS WHICH TRIGGER INSTABILITY.