

## Is Anomalous Transport "Diffusive"?

G. Rewoldt

PPPL--2650

Princeton Plasma Physics Laboratory, Princeton University,  
Princeton, New Jersey 08543

DE90 000849

### ABSTRACT

It has often been assumed that the anomalous transport in saturated plasma instabilities is "diffusive" in the sense that the particle flux,  $\Gamma$ , the electron energy flux,  $q_e$ , and the ion energy flux,  $q_i$ , can be written in forms that are *linear* in the density gradient,  $dn/dr$ , the electron temperature gradient,  $dT_e/dr$ , and the ion temperature gradient  $dT_i/dr$ . In the simplest form,  $\Gamma = -D_n^n (dn/dr)$ ,  $q_e = -D_e^n (dT_e/dr)$ , and  $q_i = -D_i^n (dT_i/dr)$ . A possible generalization of this is to include so-called "off-diagonal" terms, with  $\Gamma = nV_n - D_n^n (dn/dr) - D_n^n (n/T_e) (dT_e/dr) - D_n^n (n/T_i) (dT_i/dr)$ , with corresponding forms for the energy fluxes. Here, general results for the quasilinear particle and energy fluxes, resulting from tokamak linear microinstabilities, are evaluated to assess the relative importance of the diagonal and the off-diagonal terms. A further possible generalization is to include also contributions to the fluxes from higher powers of the gradients, specifically "quadratic" contributions proportional to  $(dn/dr)^2$ ,  $(dn/dr)(dT_e/dr)$ , and so on. A procedure is described for evaluating the corresponding coefficients, and results are presented for illustrative, realistic tokamak cases. Qualitatively, it is found that the off-diagonal diffusion coefficients can be as big as the diagonal ones, and that the quadratic terms can be larger than the linear ones. The results thus strongly suggest that the commonly used "diffusive" approximation with only diagonal terms,  $\Gamma = -D_n^n (dn/dr)$ , and correspondingly for the energy fluxes, is not adequate in practice.

## I. INTRODUCTION

Standard forms for transport equations and fluxes have been discussed recently by D. W. Ross.<sup>1</sup> Here, these equations will be extended in various ways and the coefficients will be evaluated explicitly for the quasilinear transport due to linear tokamak instabilities in realistic, illustrative cases. This will allow a test of the so-called "diffusive" approximation, where the quasilinear particle and energy fluxes of electrons and ions are linear in the density and temperature gradients. In this work, a pure hydrogenic plasma is considered so that the equilibrium densities satisfy  $n_e = n_i = n$ , and  $dn_e/dr = dn_i/dr = dn/dr$ , and the electron and ion quasilinear particle fluxes are equal on any chosen magnetic surface,  $\Gamma_e = \Gamma_i = \Gamma$ . Defining  $Q_j$  as the total energy flux for species  $j$ , the  $(5/2)\Gamma T_j$  convective part is subtracted out, giving  $q_j \equiv Q_j - (5/2)\Gamma T_j$ . Alternative forms of the convective part are compared in Ref. 1, and it is concluded there that  $(5/2)\Gamma T_j$  is the correct form. The simplest forms of the diffusion equations are

$$\begin{aligned}\Gamma &= -D_n^n \frac{dn}{dr}, \\ q_e &= -D_e^e n \frac{dT_e}{dr}, \\ q_i &= -D_i^i n \frac{dT_i}{dr}.\end{aligned}\tag{1}$$

Here, only the so-called "diagonal" terms are kept. The generalization to include the so-called "off-diagonal" diffusion coefficients, as well as corresponding anomalous convection (pinch) velocities,  $V_n$ ,  $V_e$ , and  $V_i$ , is

$$\begin{aligned}\Gamma &= nV_n - D_n^n \frac{dn}{dr} - D_e^e n \frac{dT_e}{T_e dr} - D_i^i n \frac{dT_i}{T_i dr}, \\ q_e &= nT_e V_e - D_e^e T_e \frac{dn}{dr} - D_e^e n \frac{dT_e}{dr} - D_i^i n \frac{dT_i}{dr}, \\ q_i &= nT_i V_i - D_i^i T_i \frac{dn}{dr} - D_i^e n \frac{dT_e}{dr} - D_i^i n \frac{dT_i}{dr}.\end{aligned}\tag{2}$$

Equations (2) can be conveniently written in matrix form as

$$\begin{pmatrix} \Gamma/n \\ \dot{q}_e/(nT_e) \\ \dot{q}_i/(nT_i) \end{pmatrix} = \begin{pmatrix} V_n \\ V_e \\ V_i \end{pmatrix} - \begin{pmatrix} D_n^n & D_n^e & D_n^i \\ D_e^n & D_e^e & D_e^i \\ D_i^n & D_i^e & D_i^i \end{pmatrix} \begin{pmatrix} (dn/dr)/n \\ (dT_e/dr)/T_e \\ (dT_i/dr)/T_i \end{pmatrix}. \quad (3)$$

Normalizing this way, one finds that all of the diagonal and off-diagonal  $D_j^k$  (where  $j$  and  $k = n, e,$  and  $i$ ) have the same units ( $m^2/\text{sec. say}$ ), and so are directly comparable. For notational convenience, write  $\hat{\Gamma} \equiv \Gamma/n$ ,  $\hat{q}_j \equiv q_j/(nT_j)$ ,  $\kappa_n \equiv -(1/n)(dn/dr)$ , and  $\kappa_j \equiv -(1/T_j)(dT_j/dr)$ , so that Eq. (3) becomes

$$\begin{pmatrix} \hat{\Gamma} \\ \hat{q}_e \\ \hat{q}_i \end{pmatrix} = \begin{pmatrix} V_n \\ V_e \\ V_i \end{pmatrix} + \begin{pmatrix} D_n^n & D_n^e & D_n^i \\ D_e^n & D_e^e & D_e^i \\ D_i^n & D_i^e & D_i^i \end{pmatrix} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix}. \quad (4)$$

Equation (4) can be regarded as a "Taylor series" for the fluxes,  $\hat{\Gamma}$ ,  $\hat{q}_e$ , and  $\hat{q}_i$ , in powers of the gradients,  $\kappa_n$ ,  $\kappa_e$ , and  $\kappa_i$ , truncated at first order. The extension of Eq. (4) to second powers in the gradients is

$$\begin{aligned} \begin{pmatrix} \hat{\Gamma} \\ \hat{q}_e \\ \hat{q}_i \end{pmatrix} &= \begin{pmatrix} V_n \\ V_e \\ V_i \end{pmatrix} + \begin{pmatrix} D_n^n & D_n^e & D_n^i \\ D_e^n & D_e^e & D_e^i \\ D_i^n & D_i^e & D_i^i \end{pmatrix} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\ &+ \begin{pmatrix} E_n^{nn} & E_n^{ee} & E_n^{ni} \\ E_e^{nn} & E_e^{ee} & E_e^{ni} \\ E_i^{nn} & E_i^{ee} & E_i^{ni} \end{pmatrix} \begin{pmatrix} \kappa_n^2 \\ \kappa_e^2 \\ \kappa_i^2 \end{pmatrix} + \begin{pmatrix} F_n^{ne} & F_n^{ni} & F_n^{ei} \\ F_e^{ne} & F_e^{ni} & F_e^{ei} \\ F_i^{ne} & F_i^{ni} & F_i^{ei} \end{pmatrix} \begin{pmatrix} \kappa_n \kappa_e \\ \kappa_n \kappa_i \\ \kappa_e \kappa_i \end{pmatrix}. \end{aligned} \quad (5)$$

Equation (4) is a good approximation to Eq. (5) if the quadratic  $E_j^{kk}$  and  $F_j^{kl}$  contributions to the fluxes are small compared to the linear  $D_j^k$  contributions, and Eq. (1) is a good approximation to Eq. (4) if the off-diagonal  $D_j^k$  are small compared to the diagonal  $D_j^j$  and the  $V_j$  are small compared to the  $D_j^k$  contributions. It is these conditions which will be investigated here for realistic tokamak instabilities.

A comprehensive electromagnetic kinetic eigenfrequency eigenfunction code<sup>2</sup> for high toroidal mode number tokamak instabilities such as the trapped-electron- $\eta$  mode and the MHD ballooning mode is employed here. This code also calculates the quasilinear fluxes of particles and energy for each plasma species using formulas which are direct generalizations

of those derived in Ref. 3. The eigenmode equations, the solution methods employed, and the quasilinear flux expressions are all presented in detail in Ref. 2, so this material will not be repeated here. However, this calculation can be described briefly as constituting a solution of the linearized gyrokinetic equation in toroidal geometry without any frequency expansions, using a model collision operator. It employs the ballooning formalism at lowest order in  $1/n$  (toroidal mode number), so the calculation is local to a single, chosen magnetic surface. Thus, the calculation includes transit frequency harmonics (Landau damping, etc.) for circulating particles of each species, bounce frequency harmonics for trapped particles of each species, magnetic drift frequency effects, and full finite Larmor radius effects. Input data, such as radial density and temperature profiles, for the calculation of the results presented here come either from experimental measurements or from transport code results. The MHD equilibrium used in the instability calculation is computed numerically from the corresponding pressure and safety factor profiles, or else an algebraic model MHD equilibrium is used.

The quasilinear fluxes, while being only bilinear in the fluctuation amplitudes, can in general be nonlinear in the density and temperature gradients. Given a set of gradients,  $\kappa_n$ ,  $\kappa_e$ , and  $\kappa_i$ , the code calculates the quasilinear particle and energy fluxes,  $\tilde{\Gamma}$ ,  $\tilde{q}_e$ , and  $\tilde{q}_i$ , proportional to the square of the unknown saturation level  $\phi_0$  for the perturbed electrostatic potential of the mode. The results to be presented here will allow us to assess the strength of this nonlinearity in the gradients.

The specific procedure for doing this is described in Sec. II. Numerical results for realistic tokamak cases are presented in Sec. III for the linear truncation in Eq. (4) and in Sec. IV for the quadratic truncation in Eq. (5). Discussion and conclusions are given in Sec. V.

## II. Gradient Variation

For practical computation, start with a base parameter set, denoted by a zero superscript, and compute  $\hat{\Gamma}^0$ ,  $\hat{q}_e^0$ , and  $\hat{q}_i^0$  for  $\kappa_n = \kappa_n^0$ ,  $\kappa_e = \kappa_e^0$ , and  $\kappa_i = \kappa_i^0$ . Here,  $\kappa_n^0$ ,  $\kappa_e^0$ , and  $\kappa_i^0$  will represent the actual experimental or transport code values on a chosen magnetic surface. Then, define a series of parameter sets in which  $\kappa_n$ ,  $\kappa_e$ , and  $\kappa_i$  are varied slightly up or down by amounts  $\Delta\kappa_n$ ,  $\Delta\kappa_e$ , and  $\Delta\kappa_i$ , respectively, in different combinations, from the base parameter set, with  $\hat{\Gamma}^m$ ,  $\hat{q}_e^m$ , and  $\hat{q}_i^m$  being recomputed for each of these sets of gradient values, where the superscript  $m$  identifies the parameter set. The  $\kappa_n$ ,  $\kappa_e$ , and  $\kappa_i$  values for the needed parameter sets are all listed in Table I.

Only results for parameter sets 0 to 3 are actually needed to evaluate all of the  $D_j^k$  in Eq. (4). Using standard formulas<sup>4</sup> for the numerical evaluation of derivatives, it is found that

$$\begin{aligned} D_n^n &= \frac{\hat{\Gamma}^1 - \hat{\Gamma}^0}{\Delta\kappa_n}, & D_n^e &= \frac{\hat{\Gamma}^2 - \hat{\Gamma}^0}{\Delta\kappa_e}, & D_n^i &= \frac{\hat{\Gamma}^3 - \hat{\Gamma}^0}{\Delta\kappa_i}, \\ D_e^n &= \frac{\hat{q}_e^1 - \hat{q}_e^0}{\Delta\kappa_n}, & D_e^e &= \frac{\hat{q}_e^2 - \hat{q}_e^0}{\Delta\kappa_e}, & D_e^i &= \frac{\hat{q}_e^3 - \hat{q}_e^0}{\Delta\kappa_i}, \\ D_i^n &= \frac{\hat{q}_i^1 - \hat{q}_i^0}{\Delta\kappa_n}, & D_i^e &= \frac{\hat{q}_i^2 - \hat{q}_i^0}{\Delta\kappa_e}, & D_i^i &= \frac{\hat{q}_i^3 - \hat{q}_i^0}{\Delta\kappa_i} \end{aligned} \quad (6)$$

to lowest order in the  $\Delta\kappa_j/\kappa_j^0$ . Once the  $D_j^k$  have been evaluated, then the anomalous convection velocities are given, from Eq. (4), as

$$\begin{aligned} V_n &= \hat{\Gamma}^0 - D_n^n \kappa_n^0 - D_n^e \kappa_e^0 - D_n^i \kappa_i^0, \\ V_e &= \hat{q}_e^0 - D_e^n \kappa_n^0 - D_e^e \kappa_e^0 - D_e^i \kappa_i^0, \\ V_i &= \hat{q}_i^0 - D_i^n \kappa_n^0 - D_i^e \kappa_e^0 - D_i^i \kappa_i^0. \end{aligned} \quad (7)$$

In evaluating the  $D_j^k$  in Eq. (5), results for parameter sets 0 to 6 can also be used, and the same results are necessary to evaluate the  $E_j^{kk}$ . Results for all of parameter sets 7 to

IS are needed to evaluate the  $F_j^{ki}$  in Eq. (5). Again using standard formulas<sup>4</sup> for numerical evaluation of derivatives, it is found that

$$\begin{aligned}
 D_n^n &= \frac{\hat{\Gamma}^1 - \hat{\Gamma}^4}{2\Delta\kappa_n}, & D_n^e &= \frac{\hat{\Gamma}^2 - \hat{\Gamma}^5}{2\Delta\kappa_e}, & D_n^i &= \frac{\hat{\Gamma}^3 - \hat{\Gamma}^6}{2\Delta\kappa_i}, \\
 D_e^n &= \frac{\hat{q}_e^1 - \hat{q}_e^4}{2\Delta\kappa_n}, & D_e^e &= \frac{\hat{q}_e^2 - \hat{q}_e^5}{2\Delta\kappa_e}, & D_e^i &= \frac{\hat{q}_e^3 - \hat{q}_e^6}{2\Delta\kappa_i}, \\
 D_i^n &= \frac{\hat{q}_i^1 - \hat{q}_i^4}{2\Delta\kappa_n}, & D_i^e &= \frac{\hat{q}_i^2 - \hat{q}_i^5}{2\Delta\kappa_e}, & D_i^i &= \frac{\hat{q}_i^3 - \hat{q}_i^6}{2\Delta\kappa_i}.
 \end{aligned} \tag{8}$$

and

$$\begin{aligned}
 E_n^{nn} &= \frac{\hat{\Gamma}^1 + \hat{\Gamma}^4 - 2\hat{\Gamma}^0}{2\Delta\kappa_n^2}, & E_n^{ee} &= \frac{\hat{\Gamma}^2 + \hat{\Gamma}^5 - 2\hat{\Gamma}^0}{2\Delta\kappa_e^2}, & E_n^{ii} &= \frac{\hat{\Gamma}^3 + \hat{\Gamma}^6 - 2\hat{\Gamma}^0}{2\Delta\kappa_i^2}, \\
 E_e^{nn} &= \frac{\hat{q}_e^1 + \hat{q}_e^4 - 2\hat{q}_e^0}{2\Delta\kappa_n^2}, & E_e^{ee} &= \frac{\hat{q}_e^2 + \hat{q}_e^5 - 2\hat{q}_e^0}{2\Delta\kappa_e^2}, & E_e^{ii} &= \frac{\hat{q}_e^3 + \hat{q}_e^6 - 2\hat{q}_e^0}{2\Delta\kappa_i^2}, \\
 E_i^{nn} &= \frac{\hat{q}_i^1 + \hat{q}_i^4 - 2\hat{q}_i^0}{2\Delta\kappa_n^2}, & E_i^{ee} &= \frac{\hat{q}_i^2 + \hat{q}_i^5 - 2\hat{q}_i^0}{2\Delta\kappa_e^2}, & E_i^{ii} &= \frac{\hat{q}_i^3 + \hat{q}_i^6 - 2\hat{q}_i^0}{2\Delta\kappa_i^2}.
 \end{aligned} \tag{9}$$

and

$$\begin{aligned}
 F_n^{ne} &= \frac{\hat{\Gamma}^7 - \hat{\Gamma}^8 - \hat{\Gamma}^9 + \hat{\Gamma}^{10}}{4\Delta\kappa_n\Delta\kappa_e}, & F_n^{ni} &= \frac{\hat{\Gamma}^{11} - \hat{\Gamma}^{12} - \hat{\Gamma}^{13} + \hat{\Gamma}^{14}}{4\Delta\kappa_n\Delta\kappa_i}, & F_n^{ei} &= \frac{\hat{\Gamma}^{15} - \hat{\Gamma}^{16} - \hat{\Gamma}^{17} - \hat{\Gamma}^{18}}{4\Delta\kappa_e\Delta\kappa_i}, \\
 F_e^{ne} &= \frac{\hat{q}_e^7 - \hat{q}_e^8 - \hat{q}_e^9 + \hat{q}_e^{10}}{4\Delta\kappa_n\Delta\kappa_e}, & F_e^{ni} &= \frac{\hat{q}_e^{11} - \hat{q}_e^{12} - \hat{q}_e^{13} + \hat{q}_e^{14}}{4\Delta\kappa_n\Delta\kappa_i}, & F_e^{ei} &= \frac{\hat{q}_e^{15} - \hat{q}_e^{16} - \hat{q}_e^{17} - \hat{q}_e^{18}}{4\Delta\kappa_e\Delta\kappa_i}, \\
 F_i^{ne} &= \frac{\hat{q}_i^7 - \hat{q}_i^8 - \hat{q}_i^9 + \hat{q}_i^{10}}{4\Delta\kappa_n\Delta\kappa_e}, & F_i^{ni} &= \frac{\hat{q}_i^{11} - \hat{q}_i^{12} - \hat{q}_i^{13} + \hat{q}_i^{14}}{4\Delta\kappa_n\Delta\kappa_i}, & F_i^{ei} &= \frac{\hat{q}_i^{15} - \hat{q}_i^{16} - \hat{q}_i^{17} - \hat{q}_i^{18}}{4\Delta\kappa_e\Delta\kappa_i}.
 \end{aligned} \tag{10}$$

to lowest order in the  $\Delta\kappa_j/\kappa_j^0$ . From Eq. (5), the anomalous convection velocities are then given as

$$\begin{aligned}
 V_n &= \hat{\Gamma}^0 - D_n^n \kappa_n^0 - D_n^e \kappa_e^0 - D_n^i \kappa_i^0 - E_n^{nn} (\kappa_n^0)^2 - E_n^{ee} (\kappa_e^0)^2 - E_n^{ii} (\kappa_i^0)^2 - F_n^{ne} \kappa_n^0 \kappa_e^0 - F_n^{ni} \kappa_n^0 \kappa_i^0 - F_n^{ei} \kappa_e^0 \kappa_i^0, \\
 V_e &= \hat{q}_e^0 - D_e^n \kappa_n^0 - D_e^e \kappa_e^0 - D_e^i \kappa_i^0 - E_e^{nn} (\kappa_n^0)^2 - E_e^{ee} (\kappa_e^0)^2 - E_e^{ii} (\kappa_i^0)^2 - F_e^{ne} \kappa_n^0 \kappa_e^0 - F_e^{ni} \kappa_n^0 \kappa_i^0 - F_e^{ei} \kappa_e^0 \kappa_i^0, \\
 V_i &= \hat{q}_i^0 - D_i^n \kappa_n^0 - D_i^e \kappa_e^0 - D_i^i \kappa_i^0 - E_i^{nn} (\kappa_n^0)^2 - E_i^{ee} (\kappa_e^0)^2 - E_i^{ii} (\kappa_i^0)^2 - F_i^{ne} \kappa_n^0 \kappa_e^0 - F_i^{ni} \kappa_n^0 \kappa_i^0 - F_i^{ei} \kappa_e^0 \kappa_i^0.
 \end{aligned} \tag{11}$$

However, there are some practical questions as to what to include in the variation process so as to pick up various indirect effects. Specifically, in the fully electromagnetic version of the computer code, as  $dn/dr$ ,  $dT_e/dr$ , and  $dT_i/dr$  are varied,  $n$ ,  $T_e$ ,  $T_i$ ,  $B_0$ ,  $\beta$ , and the toroidal mode number are held fixed. Also, the changed converged values of the eigenfrequency  $\omega$  are used, which can depend on all of the gradients in a nonlinear fashion, and which can thus introduce nonlinear dependence on the gradients into the fluxes. A difficult question is what to do about the undetermined saturation level  $\phi_0$  for the perturbed electrostatic potential that enters the quasilinear flux formulas. It is decided here to take  $\phi_0/T_e = C k_y r_p$ , a mixing-length type assumption, where  $r_p$  is the total pressure gradient scale length, so that all three of the changing equilibrium gradients enter the saturation condition. Here,  $C$  is kept constant during the gradient variation, but is chosen at the end to set the final  $D_e^c$  (often called  $\chi_e$ ) to an experimentally typical value, say  $1 \text{ m}^2/\text{sec}$ . This is an ad-hoc saturation criterion, in the absence of a generally accepted nonlinear theory for these modes, but it should be adequate for the present purpose of investigating the nature of the gradient dependence of the fluxes.

### III. Diagonal and Off-Diagonal Diffusion Coefficients

In this and the next section, results will be presented for several cases. The first corresponds to a Tokamak Fusion Test Reactor (TFTR) "supershot,"<sup>5</sup> (shot 35782).<sup>6</sup> The radial profiles of  $n$ ,  $T_e$ , and  $T_i$  come from experimental measurements, and the MHD equilibrium is computed numerically with the corresponding pressure and  $q$  profiles. Here, the MHD equilibrium is held fixed as the local gradients are varied. The instability calculation is carried out for the trapped-electron- $\eta_i$  mode on a chosen magnetic surface with  $r/a \simeq 1/2$ . The local parameters on this surface are:  $q = 1.54$ ,  $(r/q)(dq/dr) = 1.18$ ,  $n_e = n_i = n = 2.91 \times 10^{19} \text{ m}^{-3}$ ,  $r_\gamma \equiv -1/d \ln n/dr = 0.345 \text{ m}$ ,  $T_e = 4.12 \text{ keV}$ ,  $r_{T_e} = 0.242 \text{ m}$ ,  $\eta_e = 1.43$ ,  $T_i = 7.17 \text{ keV}$ ,  $r_{T_i} = 0.152 \text{ m}$ ,  $\eta_i = 2.27$ ,  $T_i/T_e = 1.74$ ,  $r = 0.415 \text{ m}$ ,  $a = 0.792 \text{ m}$ ,  $R_0 = 2.45 \text{ m}$ ,  $B_0 = 47.2 \text{ kG}$ ,  $\beta = 1.05\%$ , toroidal mode number = 55,  $k_y r_p = 0.495$ , and  $\nu_e = \nu_i = 0$

(collisionless). Then, for the trapped-electron- $\eta_i$  mode on this surface, the eigenfrequency is  $\omega = \omega_{ce} = -0.749 - 0.471i$ , or  $\omega = (2.78 - 1.75i) \times 10^3 \text{sec}^{-1}$ , for the eigenmode with the fewest nodes along the field line for the perturbed potentials, which balloon strongly to the outside of the torus. The corresponding basic gradient parameter values are  $\kappa_n = 2.90 \text{m}^{-1}$ ,  $\kappa_e = 4.14 \text{m}^{-1}$ , and  $\kappa_i = 6.57 \text{m}^{-1}$ . In this case,  $\Delta\kappa_n$ ,  $\Delta\kappa_e$ , and  $\Delta\kappa_i$  are chosen to be 17% of the corresponding basic gradient values. Then, computing  $\tilde{\Gamma}^m$ ,  $\tilde{q}_e^m$ , and  $\tilde{q}_i^m$  for parameter sets  $m = 0$  to 3, as defined in Table I, and substituting the results in Eqs. (6) and (7), Eq. (4) is evaluated for this case as

$$\begin{aligned} \begin{pmatrix} \tilde{\Gamma} \\ \tilde{q}_e \\ \tilde{q}_i \end{pmatrix} &= \begin{pmatrix} -7.3 \\ 1.3 \\ -16.0 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 1.74 & 0.04 & 0.74 \\ -0.93 & 1.00 & -0.44 \\ 0.56 & 1.31 & 2.60 \end{pmatrix} \frac{\text{m}^2}{\text{sec}} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\ &= \begin{pmatrix} -7.3 \\ 1.3 \\ -16.0 \end{pmatrix} \frac{\text{m}}{\text{sec}} - \begin{pmatrix} 10.1 \\ -1.5 \\ 24.1 \end{pmatrix} \frac{\text{m}}{\text{sec}} = \begin{pmatrix} 2.8 \\ -0.2 \\ 8.1 \end{pmatrix} \frac{\text{m}}{\text{sec}} \end{aligned} \quad (12)$$

with  $C = 0.134$ . Qualitatively,  $V_n$  and  $V_i$  are inward while  $V_e$  is slightly outward, and each is somewhat smaller than the corresponding  $D_j^k$  matrix contribution. Thus, there are substantial partial cancellations, leaving net outward fluxes for  $\tilde{\Gamma}$  and  $\tilde{q}_i$ , and a slight net inward flux for  $\tilde{q}_e$ . Of course, if the  $(5/2)\Gamma T_j$  convective terms are included, the total energy fluxes are both outward:  $\hat{Q}_e \equiv \tilde{q}_e + (5/2)\tilde{\Gamma} = 6.7 \text{m/sec}$  and  $\hat{Q}_i \equiv \tilde{q}_i + (5/2)\tilde{\Gamma} = 15.0 \text{m/sec}$  with this normalization. It should be remarked that, physically, the  $V_j$  do not have independent existences in the sense of allowing nonzero fluxes in the limit of zero gradients. Rather, they reflect the finite thresholds on the gradients to have instability, with the fluxes rising steeply above these thresholds. Below the thresholds, the mode is damped and the corresponding fluxes are just zero. This implies that the response to a perturbation of the gradients would be larger than estimated from the steady-state fluxes on the basis of Eq. (1), where there are no anomalous convection velocities. In the  $D_j^k$  term in Eq. (12), it is seen that all of the diagonal and off-diagonal elements are of the same order, except for  $D_n^e = 0.04$ .



and that  $D_e^n$  and  $D_e^i$  are negative. In this case, then, Eq. (1) is a poor approximation to Eq. (4).

The same procedure has been carried out for three other cases. These will now be described more briefly. The next two cases have input parameters taken from runs of the BALDUR transport code<sup>7</sup> for a now superseded design of the Compact Ignition Tokamak (CIT) with major radius  $R_0 = 1.6$  m. Specifically, on the chosen magnetic surface with  $r/a \simeq 0.5$ , at the BALDUR-predicted value of local  $\beta = 8.34\%$ , both the trapped-electron- $\eta_i$  mode and the kinetically calculated MHD ballooning mode are unstable. Both of these modes will be considered as separate cases. Also, for these cases, the so-called "s- $\alpha$ " model MHD equilibrium<sup>8</sup> is employed instead of a numerical MHD equilibrium, with the Shafranov shift parameter  $\alpha \propto dp/dr$  varying as the gradients are changed. In this case, the trapped-electron- $\eta_i$  mode at  $k_{\theta}\rho_i = 0.75$  has eigenfrequency  $\omega/\omega_{*e} = -0.0299 + 0.127i$ , and the MHD ballooning mode at  $k_{\theta}\rho_i = 0.40$  has eigenfrequency  $\omega/\omega_{*e} = -1.76 + 0.0273i$ . The basic parameter set has  $\kappa_n^0 = 1.70 \text{ m}^{-1}$ ,  $\kappa_e^0 = 0.684 \text{ m}^{-1}$ , and  $\kappa_i^0 = 0.917 \text{ m}^{-1}$ , with the  $\Delta\kappa_j$ 's chosen to be 1% of the corresponding  $\kappa_j^0$ 's. Also, for this case,  $\eta_e = 0.403$  and  $\eta_i = 0.541$ . Carrying through the same procedure for the trapped-electron- $\eta_i$  mode for this case results in

$$\begin{aligned} \begin{pmatrix} \dot{\Gamma} \\ \dot{q}_e \\ \dot{q}_i \end{pmatrix} &= \begin{pmatrix} -3.7 \\ 2.5 \\ 4.2 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 3.01 & 0.67 & 0.20 \\ -3.20 & 1.00 & 0.25 \\ -4.57 & -0.73 & 1.30 \end{pmatrix} \frac{\text{m}^2}{\text{sec}} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\ &= \begin{pmatrix} -3.7 \\ 2.5 \\ 4.2 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 5.7 \\ -4.5 \\ -7.1 \end{pmatrix} \frac{\text{m}}{\text{sec}} = \begin{pmatrix} 2.0 \\ -2.0 \\ -2.9 \end{pmatrix} \frac{\text{m}}{\text{sec}} \end{aligned} \quad (13)$$

for  $C = 0.214$ . Here,  $V_n$  is inward while  $V_e$  and  $V_i$  are outward. All of the diagonal and off-diagonal  $D_j^k$  are comparable in magnitude, and the diagonal elements are all positive, while several of the off-diagonal elements are negative. Again, there is substantial cancellation between the  $V_j$  convection terms and the  $D_j^k$  diffusion terms, leading to net outward  $\dot{\Gamma}$  and to net inward  $\dot{q}_e$  and  $\dot{q}_i$ . However, again the total energy fluxes are both outward, with  $\dot{Q}_e = 3.1 \text{ m/sec}$  and  $\dot{Q}_i = 2.3 \text{ m/sec}$ , in the normalization of Eq. (13).

The corresponding result for the MHD ballooning mode is

$$\begin{aligned} \begin{pmatrix} \dot{\Gamma} \\ \dot{q}_e \\ \dot{q}_i \end{pmatrix} &= \begin{pmatrix} -19.4 \\ 7.7 \\ -0.1 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 7.43 & 4.11 & 5.73 \\ -3.76 & 1.00 & -2.55 \\ 1.36 & 21.26 & -11.22 \end{pmatrix} \frac{\text{m}^2}{\text{sec}} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\ &= \begin{pmatrix} -19.4 \\ 7.7 \\ -0.1 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 20.7 \\ -8.0 \\ 6.6 \end{pmatrix} \frac{\text{m}}{\text{sec}} = \begin{pmatrix} 1.2 \\ -0.3 \\ 6.4 \end{pmatrix} \frac{\text{m}}{\text{sec}}. \end{aligned} \quad (14)$$

for  $C = 0.849$ . For this instability,  $V_n$  is inward, while  $V_e$  is outward and  $V_i$  is much smaller. Again, the off-diagonal  $D_j^k$  are of comparable or larger magnitude than the diagonal elements. In this case,  $D_i^i$ ,  $D_e^e$ , and  $D_n^e$  are negative, and the others positive. Here, there is substantial cancellation between the convective  $V_n$  and  $V_e$  and the corresponding  $D_j^k$  contributions, but not for  $V_i$ . The net  $\dot{\Gamma}$  and  $\dot{q}_i$  are outward, while the net  $\dot{q}_e$  is slightly inward. However, the total energy fluxes are again both outward, with  $\dot{Q}_e = 2.8$  m/sec and  $\dot{Q}_i = 9.6$  m/sec with the normalization of Eq. (14).

The last case to be considered here is a TFTR  $\alpha$ -storage mode case<sup>9</sup> (here used without the  $\alpha$ -particles), again with the "s- $\alpha$ " model MHD equilibrium, for the trapped-electron- $\eta_i$  mode with local  $\beta = 1.21\%$ ,  $\eta_e = 0.888$ , and  $\eta_i = 0.713$ . The basic parameter set, from the BALDUR transport code results, has  $\kappa_n^0 = 2.51$  m<sup>-1</sup>,  $\kappa_e^0 = 2.23$  m<sup>-1</sup>, and  $\kappa_i^0 = 1.79$  m<sup>-1</sup>. In this case,  $\Delta\kappa_n$  is chosen as 10% of  $\kappa_n^0$ ,  $\Delta\kappa_e$  as 1% of  $\kappa_e^0$ , and  $\Delta\kappa_i$  as 2.5% of  $\kappa_i^0$ . Carrying through the same procedure results in

$$\begin{aligned} \begin{pmatrix} \dot{\Gamma} \\ \dot{q}_e \\ \dot{q}_i \end{pmatrix} &= \begin{pmatrix} -2.9 \\ 0.9 \\ 2.9 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 1.88 & 0.02 & -0.38 \\ -1.32 & 1.00 & -0.09 \\ -2.83 & 0.02 & 1.44 \end{pmatrix} \frac{\text{m}^2}{\text{sec}} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\ &= \begin{pmatrix} -2.9 \\ 0.9 \\ 2.9 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 4.1 \\ -1.2 \\ -4.5 \end{pmatrix} \frac{\text{m}}{\text{sec}} = \begin{pmatrix} 1.2 \\ -0.3 \\ -1.6 \end{pmatrix} \frac{\text{m}}{\text{sec}}, \end{aligned} \quad (15)$$

for  $C = 0.139$ . For this case,  $V_n$  is inward, while  $V_e$  and  $V_i$  are outward. Again, most of the off-diagonal  $D_j^k$  are of comparable or larger magnitude than the diagonal elements. In this case again, several of the  $D_j^k$  are negative. Also, there is substantial cancellation between

the convective  $V_j$  and the corresponding  $D_j^k$  contributions. The net  $\hat{\Gamma}$  is outward, while the net  $\hat{q}_e$  and  $\hat{q}_i$  are inward. However, the total energy fluxes are again both outward, with  $\hat{Q}_e = 2.6$  m/sec and  $\hat{Q}_i = 1.3$  m/sec with the normalization of Eq. (15).

#### IV. Linear and Quadratic Gradient Dependences

Using the same TFTR supersonic case employed in the previous section, the coefficients in Eq. (5) are evaluated as described in Sec. II. Recomputing the  $\hat{\Gamma}^m$ ,  $\hat{q}_e^m$ , and  $\hat{q}_i^m$  for parameter sets  $m = 0$  to 18 as specified in Table I, and then evaluating the  $D_j^k$ ,  $E_j^{kk}$ , and  $F_j^{kl}$  according to Eqs. (8) to (11), Eq. (5) in this case becomes

$$\begin{aligned}
 \begin{pmatrix} \hat{\Gamma} \\ \hat{q}_e \\ \hat{q}_i \end{pmatrix} &= \begin{pmatrix} -200.3 \\ 95.3 \\ 139.6 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 1.68 & 0.04 & 0.71 \\ -0.87 & 1.00 & -0.41 \\ 0.31 & 1.04 & 2.48 \end{pmatrix} \frac{\text{m}^2}{\text{sec}} \begin{pmatrix} \kappa_n \\ \kappa_e \\ \kappa_i \end{pmatrix} \\
 &+ \begin{pmatrix} 2.14 & 0 & 0.42 \\ -2.14 & 0 & -0.42 \\ 8.56 & 6.31 & 1.87 \end{pmatrix} \frac{\text{m}^3}{\text{sec}} \begin{pmatrix} \kappa_n^2 \\ \kappa_e^2 \\ \kappa_i^2 \end{pmatrix} \\
 &+ \begin{pmatrix} 0 & 8.50 & -0.17 \\ -1.13 & -3.78 & 0.99 \\ -0.38 & -23.84 & 1.65 \end{pmatrix} \frac{\text{m}^3}{\text{sec}} \begin{pmatrix} \kappa_n \kappa_e \\ \kappa_n \kappa_i \\ \kappa_e \kappa_i \end{pmatrix} \\
 &= \begin{pmatrix} -200.3 \\ 95.3 \\ 139.6 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 9.7 \\ -1.1 \\ 21.5 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 36.0 \\ -36.0 \\ 260.7 \end{pmatrix} \frac{\text{m}}{\text{sec}} + \begin{pmatrix} 157.3 \\ -58.4 \\ -413.7 \end{pmatrix} \frac{\text{m}}{\text{sec}} \\
 &= \begin{pmatrix} 2.7 \\ -0.2 \\ 8.1 \end{pmatrix} \frac{\text{m}}{\text{sec}},
 \end{aligned} \tag{16}$$

for  $C = 0.134$ . With this normalization,  $\hat{Q}_e = 6.9$  m/sec and  $\hat{Q}_i = 15.0$  m/sec. In these results, we see that the quadratic (in the gradients)  $E_j^{kk}$  and  $F_j^{kl}$  term contributions are an order of magnitude larger than the linear  $D_j^k$  term contributions! What this means is that the "Taylor series" in powers of the gradients is in fact diverging instead of converging. The  $V_j$ 's are large, giving near cancellations with the  $E_j^{kk}$  and  $F_j^{kl}$  term contributions, and leaving much smaller net fluxes. Thus, approximation of Eq. (5) by Eq. (4), let alone by Eq. (1),

is seen to be quite unacceptable. In fact, the nonlinearity in the gradients appears from Eq. (16) to be sufficiently strong that the only acceptable course is to compute the fluxes from the quasilinear expressions to all orders in the gradients, without ever expanding in powers of the gradients.

## V. Conclusions

A comprehensive electromagnetic kinetic eigenfrequency eigenfunction code<sup>2</sup> for high toroidal mode number tokamak instabilities such as the trapped-electron- $\eta_1$  mode and the MHD ballooning mode also computes the quasilinear particle and energy fluxes for each plasma species. By varying separately the equilibrium density gradient, electron temperature gradient, and ion temperature gradient from an initial set of values, and recalculating the particle flux, the electron energy flux, and the ion energy flux for each new set of values, it has been shown to be possible to evaluate both the diagonal and off-diagonal anomalous diffusion coefficients corresponding to a particular linear instability, as well as the corresponding anomalous convection (pinch) velocity. The results for realistic tokamak cases presented in Sec. III indicate that: a) The anomalous convection velocities for particles and electron energy and ion energy are large enough to give substantial partial cancellation with the diffusion term, but are not big enough to reverse the sign of the flux. b) The diagonal and off-diagonal diffusion coefficients are generally all of the same order, though some of the off-diagonal elements can be small or negative, depending on the element and the case considered.

The formalism has also been extended here to examine the dependence of the fluxes on second powers of the gradients. A procedure for evaluating the corresponding transport coefficients is described in Sec. II. Results were presented for a realistic TFTR supershot case in Sec. IV, which indicate that the quadratic (in the gradients) contributions to the fluxes are much larger than the linear contributions! In other words, the "Taylor series" for the fluxes in powers of the gradients is in fact diverging. This implies that commonly used

approximations for the transport equations, such as Eq. (4), where the fluxes are linear in the gradients, are not acceptable. In this sense, anomalous transport is, in fact, not "diffusive."

### **Acknowledgments**

The author would like to thank M. Zarnstorff for providing the TFTR supershot experimental profiles, J. Manickam and A. Miller for providing the corresponding numerical MHD equilibrium, and M. Redi, D. Stotler, and G. Bateman for providing BALDUR transport code results.

This work was supported by United States Department of Energy Contract No. DE-AC02-76-CHO-3073.

## References

- <sup>1</sup>D. W. Ross. *Comments Plasma Phys. Controlled Fusion* **12**, 155 (1989).
- <sup>2</sup>G. Rewoldt, W. M. Tang, and R. J. Hastie. *Phys. Fluids* **30**, 807 (1987).
- <sup>3</sup>W. Horton, in *Handbook of Plasma Physics*, edited by M. N. Rosenbluth and R. Z. Sagdeev, Vol. 2: Basic Plasma Physics II, edited by A. A. Galeev and R. N. Sudan (Elsevier, New York, 1984), p. 383, cf. Eqs. (129) and (130).
- <sup>4</sup>P. J. Davis and I. Polonsky, in *Handbook of Mathematical Functions*, edited by M. Abramowitz and I. A. Stegun, National Bureau of Standards, Applied Mathematics Series (U.S. Government Printing Office, Washington, D.C., 1964), p. 882-885.
- <sup>5</sup>R. J. Hawryluk, V. Arunasalam, M. G. Bell, M. Bitter, W. R. Blanchard, N. L. Bretz, R. Budny, C. E. Bush, J. D. Callen, S. A. Cohen, S. K. Combs, S. L. Davis, D. L. Dimock, H. F. Dylla, P. C. Efthimion, L. C. Emerson, A. C. England, H. P. Eubank, R. J. Fonck, E. Fredrickson, H. P. Furth, G. Gammel, R. J. Goldston, B. Grek, L. R. Grisham, G. Hammett, W. W. Heidbrink, H. W. Hendel, K. W. Hill, E. Hinnov, S. Hiroe, H. Hsuan, R. A. Hulse, K. P. Jaehnig, D. Jassby, F. C. Jobs, D. W. Johnson, L. C. Johnson, R. Kaita, R. Kamperschroer, S. M. Kaye, S. J. Kilpatrick, R. J. Knize, H. Kugel, P. H. LaMarche, B. LeBlanc, R. Little, C. H. Ma, D. M. Manos, D. K. Mansfield, R. T. McCann, M. P. McCarthy, D. C. McCune, K. McGuire, D. H. McNeill, D. M. Meade, S. S. Medley, D. R. Mikkelsen, S. L. Milora, W. Morris, D. Mueller, V. Mukhovatov, E. B. Neischmidt, J. O'Rourke, D. K. Owens, H. Park, N. Pomphrey, B. Prichard, A. T. Ramsey, M. H. Redi, A. L. Roquemore, P. H. Rutherford, N. R. Sauthoff, G. Schilling, J. Schivell, G. L. Schmidt, S. D. Scott, S. Sesnic, J. C. Sennis, F. J. Stauffer, B. C. Stratton, G. D. Tait, G. Taylor, J. R. Timberlake, H. H. Towner, M. Ulrickson, V. Vershkov, S. von Goeler, F. Wagner, R. Weiland, J. B. Wilgen, M. Williams, K. L. Wong, S. Yoshikawa, R. Yoshino, K. M. Young, M. C. Zarnstorff, V. S. Zaver'yaev, S. J. Zweben, in *Proceedings of the Eleventh International Conference on Plasma Physics and Controlled Nuclear Fusion Research (IAEA, Vienna, 1987)*, Vol. 1, p. 51.

<sup>6</sup>M. C. Zarnstorff (private communication).

<sup>7</sup>D. P. Stotler, G. Bateman, and M. H. Redi, in *Proceedings of the Sherwood Annual Controlled Fusion Theory Conference*, San Diego, 1987 (Science Applications International Corporation, San Diego, 1987), abstract 2D28.

<sup>8</sup>J. W. Connor, R. J. Hastie, and J. B. Taylor, *Phys. Rev. Lett.* **40**, 396 (1978).

<sup>9</sup>S. J. Zweben, H. P. Furth, D. R. Mikkelsen, M. H. Redi, and J. D. Strachan, *Nucl. Fusion* **28**, 2230 (1988).

TABLE I. Parameter sets for gradients. Here,  $\kappa_n \equiv -(1/n)dn/dr$ ,  $\kappa_e \equiv -(1/T_e)dT_e/dr$ , and  $\kappa_i \equiv -(1/T_i)dT_i/dr$ .

parameter set $m$	$\kappa_n$	$\kappa_e$	$\kappa_i$
0	$\kappa_n^0$	$\kappa_e^0$	$\kappa_i^0$
1	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0$
2	$\kappa_n^0$	$\kappa_e^0 + \Delta\kappa_e$	$\kappa_i^0$
3	$\kappa_n^0$	$\kappa_e^0$	$\kappa_i^0 - \Delta\kappa_i$
4	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0$
5	$\kappa_n^0$	$\kappa_e^0 - \Delta\kappa_e$	$\kappa_i^0$
6	$\kappa_n^0$	$\kappa_e^0$	$\kappa_i^0 - \Delta\kappa_i$
7	$\kappa_n^0 + \Delta\kappa_n$	$\kappa_e^0 + \Delta\kappa_e$	$\kappa_i^0$
8	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0 - \Delta\kappa_e$	$\kappa_i^0$
9	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0 + \Delta\kappa_e$	$\kappa_i^0$
10	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0 - \Delta\kappa_e$	$\kappa_i^0$
11	$\kappa_n^0 + \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0 + \Delta\kappa_i$
12	$\kappa_n^0 + \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0 - \Delta\kappa_i$
13	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0 + \Delta\kappa_i$
14	$\kappa_n^0 - \Delta\kappa_n$	$\kappa_e^0$	$\kappa_i^0 - \Delta\kappa_i$
15	$\kappa_n^0$	$\kappa_e^0 + \Delta\kappa_e$	$\kappa_i^0 + \Delta\kappa_i$
16	$\kappa_n^0$	$\kappa_e^0 + \Delta\kappa_e$	$\kappa_i^0 - \Delta\kappa_i$
17	$\kappa_n^0$	$\kappa_e^0 - \Delta\kappa_e$	$\kappa_i^0 + \Delta\kappa_i$
18	$\kappa_n^0$	$\kappa_e^0 - \Delta\kappa_e$	$\kappa_i^0 - \Delta\kappa_i$



EXTERNAL DISTRIBUTION IN ADDITION TO UC-420

Dr. Frank J. Paoloni, Univ of Wollongong, AUSTRALIA  
Prof. M.H. Brennan, Univ Sydney, AUSTRALIA  
Plasma Research Lab., Australian Nat. Univ., AUSTRALIA  
Prof. I.R. Jones, Flinders Univ., AUSTRALIA  
Prof. F. Cap, Inst Theo Phys, AUSTRIA  
Prof. M. Heindler, Institut für Theoretische Physik, AUSTRIA  
M. Goossens, Astronomisch Instituut, BELGIUM  
Ecole Royale Militaire, Lab de Phys Plasmas, BELGIUM  
Commission-European, Dg-XII Fusion Prog, BELGIUM  
Prof. R. Boucique, Rijksuniversiteit Gent, BELGIUM  
Dr. P.H. Sekaneke, Instituto Fisica, BRAZIL  
Instituto De Pesquisas Espaciais-INPE, BRAZIL  
Documents Office, Atomic Energy of Canada Limited, CANADA  
Dr. M.P. Bachynski, NPB Technologies, inc., CANADA  
Dr. H.M. Skarsgard, University of Saskatchewan, CANADA  
Dr. H. Barnard, University of British Columbia, CANADA  
Prof. J. Teichmann, Univ. of Montreal, CANADA  
Prof. S.R. Sreenivasan, University of Calgary, CANADA  
Prof. Tudor W. Johnston, INRS-Energie, CANADA  
Dr. Bolton, Centre canadien de fusion magnetique, CANADA  
Dr. C.R. James, Univ. of Alberta, CANADA  
Dr. Peter Lukac, Kozenskeho Univ, CZECHOSLOVAKIA  
The Librarian, Culham Laboratory, ENGLAND  
The Librarian, Rutherford Appleton Laboratory, ENGLAND  
Mrs. S.A. Hutchinson, JET Library, ENGLAND  
C. Mouttat, Lab. de Physique des Milieux Ionises, FRANCE  
J. Radet, CEN/CADARACHE - Bat 306, FRANCE  
Ms. C. Rinni, Librarian, Univ. of Ioannina, GREECE  
Dr. Tom Hual, Academy Bibliographic Ser., HONG KONG  
Preprint Library, Hungarian Academy of Sciences, HUNGARY  
Dr. B. Das Gupta, Saha Inst of Nucl. Phys., INDIA  
Dr. P. Kaw, Institute for Plasma Research, INDIA  
Dr. Philip Rosenau, Israel Inst. of Tech, ISRAEL  
Librarian, Int'l Ctr Theo Phys, ITALY  
Prof. G. Rostagni, Istituto Ges Ionizzati Del CNR, ITALY  
Miss Clelia De Palo, Assoc EURATOM-ENEA, ITALY  
Dr. G. Grosso, Istituto di Fisica del Plasma, ITALY  
Dr. H. Yamato, Toshiba Res & Dev, JAPAN  
Prof. I. Kawakami, Atomic Energy Res. Institute, JAPAN  
Prof. Kyoji Nishikawa, Univ of Hiroshima, JAPAN  
Director, Dept. Large Tokamak Res. JAERI, JAPAN  
Prof. Satoshi Itoh, Kyushu University, JAPAN  
Research Info Center, Nagoya University, JAPAN  
Prof. S. Tanaka, Kyoto University, JAPAN  
Library, Kyoto University, JAPAN  
Prof. Nobuyuki Inoue, University of Tokyo, JAPAN  
S. Mori, JAERI, JAPAN  
H. Jeong, Librarian, Korea Advanced Energy Res Inst, KOREA  
Prof. D.J. Choi, The Korea Adv. Inst of Sci & Tech, KOREA  
Prof. B.S. Liley, University of Waikato, NEW ZEALAND  
Institute of Plasma Physics, PEOPLE'S REPUBLIC OF CHINA  
Librarian, Institute of Phys., PEOPLE'S REPUBLIC OF CHINA  
Library, Tsing Hua University, PEOPLE'S REPUBLIC OF CHINA  
Z. Li, Southwest Inst. Physics, PEOPLE'S REPUBLIC OF CHINA  
Prof. J.A.C. Cabral, Inst Superior Tecnico, PORTUGAL  
Dr. Octavian Petrus, AL I CUZA University, ROMANIA  
Dr. Jam de Villiers, Fusion Studies, AEC, SO AFRICA  
Prof. M.A. Hellberg, University of Natal, SO AFRICA  
C.I.E.M.A.T., Fusion Div. Library, SPAIN  
Dr. Lennart Stenflo, University of UMEA, SWEDEN  
Library, Royal Institute of Tech, SWEDEN  
Prof. Hans Wilhelmson, Chalmers Univ of Tech, SWEDEN  
Centre Phys des Plasmas, Ecole Polytech Fed, SWITZERLAND  
Bibliotheek, Fom-Inst Voor Plasma-Fysica, THE NETHERLANDS  
Metin Durgut, Middle East Technical University, TURKEY  
Dr. D.D. Ryutov, Siberian Acad Sci, USSR  
Dr. G.A. Eliseev, Kurchatov Institute, USSR  
Dr. V.A. Glukhikh, Inst Electrophysical Apparatus, USSR  
Prof. O.S. Padichenko, inst. of Phys. & Tech. USSR  
Dr. L.M. Kovrizhnykh, Institute of Gen. Physics, USSR  
Nuclear Res. Establishment, Julich Ltd., W. GERMANY  
Bibliothek, Inst. Für Plasmaforschung, W. GERMANY  
Dr. K. Schindler, Ruhr-Universität Bochum, W. GERMANY  
ASDEX Reading Rm, c/o Wagner, IPP/Max-Planck, W. GERMANY  
Librarian, Max-Planck Institut, W. GERMANY  
Prof. R.K. Janev, Inst of Phys, YUGOSLAVIA