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确定 $\xi(2230)$ 自旋的一种新方法

A NEW METHOD FOR THE DETERMINATION  
OF THE SPIN OF  $\xi(2230)$



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# 确定 $\xi(2230)$ 自旋的一种新方法

A NEW METHOD FOR THE DETERMINATION  
OF THE SPIN OF  $\xi(2230)$

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## 摘 要

本文得到了过程 $e^+e^- \rightarrow J/\psi \rightarrow \gamma B(J^0), B(J^0) \rightarrow P_1 P_2$ 的矩的光子角分布, 提供了确定 $B(2230)$ 自旋的新途径。

关键词 矩 角分布 螺旋性

**A NEW METHOD FOR THE  
DETERMINATION OF THE  
SPIN OF  $\xi(2230)$**

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**ABSTRACT**

The angular distributions of the photon for the moments of process  $e^+e^- \rightarrow J/\psi \rightarrow \gamma B(J^*), B(J^*) \rightarrow P_1 + P_2$  have been given. It provides a new way to determine the spin of  $\xi(2230)$ .

## I. INTRODUCTION

A new state  $\xi(2230)$  has been discovered in the radiative decay  $J/\psi \rightarrow \gamma K \bar{K}$  by MARK III group<sup>(1)</sup>. The full process is

$$e^+ + e^- \rightarrow J/\psi \rightarrow \gamma + \xi \quad (1)$$

$\swarrow$   
 $K^+ K^-, K^0 \bar{K}^0$

DMZ has performed a re-analysis of  $J/\psi \rightarrow \gamma K^+ K^-$  and  $J/\psi \rightarrow \gamma K^0 \bar{K}^0$ , but no significant structure at 2.23 GeV shows up in  $KK$  mass spectrum.

MARK III has also performed a spin analysis of the  $\xi(2230)$  using the maximum likelihood technique<sup>(2)</sup>. The procedure is similar to that used for  $\theta/f_2(1720)$ . However it is not certain whether the spin of  $\xi(2230)$  is  $J=2$  or 4.

We pointed out<sup>(1)</sup> that there exists an insensitive region to determine the spin ( $J=2$  or 4) of  $\theta/f_2(1720)$  using the angular distribution in a general helicity formalism. Because the data of  $\theta/f_2$  just fall into the insensitive region we can not say exactly that the spin of  $\theta/f_2$  is  $J=2$ . So far the spin of  $\xi(2230)$  can not be determined ( $J=2$  or 4). We think that an obvious reason is less data and another reason is that the data of  $\xi$  may fall into the insensitive region.

This paper attempts to give a new way to determine the spin of  $\xi$  (and  $\theta/f_2$ ) using moment analysis<sup>(3)</sup>.

## II. ANGULAR DISTRIBUTION

We consider a reaction which produces a boson resonance  $B$  with spin  $J$  and parity  $\eta$

$$e^+ + e^- \rightarrow J/\psi \rightarrow \gamma + B(J^\eta) \quad (2)$$

The resonance  $B$  then decays into two pseudoscalar mesons  $P_1$  and  $P_2$  ( $\eta$  must be  $+$ )

$$B(J^\eta) \rightarrow P_1 + P_2 \quad (3)$$

The angular distribution in a general helicity formalism is given by

$$W(\theta, \theta', \phi) \propto \sum_{\lambda_1, \lambda_2} I(\lambda_1, \lambda_2) A_{\lambda_1, \lambda_2} A_{\lambda_1, \lambda_2}^* D_{-\lambda_1, 0}^J(\phi, \theta, 0) D_{-\lambda_2, 0}^J(\phi, \theta, 0) \quad (4)$$

where  $A_{\lambda_1, \lambda_2} \sim \langle \gamma_{\lambda_1} B_J | T | \psi_{\lambda_2} \rangle \quad (5)$

is the helicity amplitude and  $\lambda_1, \lambda_2$  are helicities of the photon,  $B, J/\psi$

<sup>3</sup>For a system of two pseudoscalar mesons the spin, parity and c-parity of  $\xi(2230)$  should be  $J^{PC} = (\text{even})^{++}$ .

respectively:

$$I(\lambda_1, \lambda_2) = \frac{1}{4} \sum_{\lambda_3} \langle \psi_{\lambda_1} | T | e^+ e^- \rangle \langle \psi_{\lambda_2} | T | e^+ e^- \rangle^* \quad (6)$$

$(\lambda_1, \phi)$  describes the direction of  $P_1$  momentum in the rest frame of  $B$ .

We choose the  $Z$  axis parallel to the direction of the photon and  $e^+ e^-$  beams are in the  $X-Z$  plane. Since  $p \gg m$ , we obtain easily in the rest frame of  $J/\psi$ :

$$I(1, 1) = I(-1, -1) \approx p^2 (1 + \cos^2 \theta)$$

$$I(1, 0) = I(0, 1) = -I(-1, 0) = -I(0, -1) \approx \frac{1}{\sqrt{2}} p^2 \sin^2 \theta \quad (7)$$

$$I(1, -1) = I(-1, 1) \approx p^2 \sin^2 \theta$$

$$I(0, 0) \approx 2p^2 \sin^2 \theta$$

where  $p = |p_+| = |p_-|$ ,  $p_+$  and  $p_-$  are momenta of the positron and the electron,  $\theta$ , is the angle between the photon and positron beam.

### III. MOMENT ANALYSIS

Some important decay modes for example  $B(J^P) \rightarrow B_1(1^-) + B_2(1^-)$ , where  $B_1$  and  $B_2$  mesons in turn decay into 2 pseudoscalar mesons ( $P_1, P_2$  and  $P_2, P_1$ ) were illustrated<sup>21</sup>. They have given the corresponding moments and linear relations among different moments for certain spin-parity combinations of the parent bosons. According to these relations we can determine the spin and parity of  $B$ . We note that some relations are very effective. But we know that the observed decay modes of  $\xi$  (and  $\theta/f_2$ ) are just the two pseudoscalar mesons channels. Therefore we can not use all relations of [5] to discriminate the spin of  $\xi(2230)$  (and  $\theta/f_2$ ).

We generalize the moment analysis to the process

$$e^+ + e^- \rightarrow J/\psi \rightarrow \gamma + B(J^P) \quad (8)$$

$\downarrow$   
 $P_1 + P_2$

Introduce the angular distribution of the photon for the moment which is defined as follows

$$H_J(\theta_\gamma, LM) = \int W_J(\theta_\gamma, \theta, \phi) D_{LM}^J(\phi, \theta, 0) \sin \theta d\theta d\phi \quad (9)$$

This is an experimentally measurable quantity. From eq.(4) we have

$$H_J(\theta_\gamma, LM) = \frac{4\pi}{2J+1} \sum_{\lambda_1, \lambda_2} I(\lambda_1, \lambda_2) A_{\lambda_1, \lambda_2} \cdot$$

$$\cdot (J-A, LM; J-A)(J, L, 0; J, 0)$$

$$= \frac{4\pi}{2J+1} I_{J, L}^{M, 0}(\theta_\gamma) (J, 0, L, 0; J, 0)$$

where we use the notation  $(j_1, m_1; j_2, m_2; j_3, m_3)$  for the usual Clebsch-Gordan  $c$

efficient and the multipole parameter is given by

$$t_{l, \lambda}^m(\theta) = \sum_{\lambda_1 \lambda_2} I(\lambda_1, \lambda_2) A_{l, \lambda_1} A_{l, \lambda_2} (J-A) L M (J-A) \quad (11)$$

We take  $L$  to be even so that  $t_{l, \lambda}^m(\theta)$  is purely real. We can express  $H_l(\theta, LM)$  in terms of eq. (7) and the ratio of helicity amplitudes  $x, y$ .

For  $L=2$  we have

$$\begin{aligned} H_2(\theta, 22) &= H_2(\theta, 2-2) \propto -\frac{16\pi}{35} \rho^2 y \sin^2 \theta, \\ H_2(\theta, 21) &= -H_2(\theta, 2-1) \propto -\frac{4\sqrt{2}\pi}{35} \rho^2 (x - \sqrt{6} xy) \sin 2\theta, \\ H_2(\theta, 20) &\propto \frac{16\pi}{35} \rho^2 [x^2 \sin^2 \theta + (1-y^2)(1+\cos^2 \theta)] \\ &\sim 1 + A_1 \cos^2 \theta, \end{aligned} \quad (12)$$

$$A_1 = \frac{1-y^2-x^2}{1-y^2+x^2} \quad (13)$$

$$\begin{aligned} H_4(\theta, 42) &= H_4(\theta, 4-2) \propto -\frac{16\sqrt{15}\pi}{231} \rho^2 y \sin^2 \theta, \\ H_4(\theta, 41) &= -H_4(\theta, 4-1) \propto -\frac{8\sqrt{15}\pi}{693} \rho^2 (x - \frac{9}{\sqrt{10}} xy) \sin 2\theta, \\ H_4(\theta, 40) &\propto \frac{272\pi}{693} \rho^2 [x^2 \sin^2 \theta + \frac{10}{17} (1+0.4y^2)(1+\cos^2 \theta)] \\ &\sim 1 + A_2 \cos^2 \theta, \end{aligned} \quad (14)$$

$$A_2 = \frac{\frac{10}{17} (1+0.4y^2) - x^2}{\frac{10}{17} (1+0.4y^2) + x^2} \quad (15)$$

We note that the  $H_2(\theta, 20)$  and  $H_4(\theta, 40)$  which are comparable with the angular distribution of the photon in a general helicity formalism are different. While the angular distributions of the photon in a general helicity formalism are same in spite of  $J=2$  or  $4$ . They are

$$W_l(\theta) \sim 1 + A \cos^2 \theta, \quad A = \frac{1+y^2-2x^2}{1+y^2+2x^2} \quad (16)$$

For  $L=4$  we have

$$\begin{aligned} H_4(\theta, 40) &\propto -\frac{64\pi}{105} \rho^2 [x^2 \sin^2 \theta - 0.75(1 + \frac{1}{6} y^2)(1+\cos^2 \theta)] \\ &\sim -(1 + A_3 \cos^2 \theta) \end{aligned} \quad (17)$$

$$A_3 = \frac{-0.75(1 + \frac{1}{6}y^2) - x^2}{-0.75(1 + \frac{1}{6}y^2) + x^2} \quad (18)$$

$$H_4(\theta, 40) \propto \frac{144x}{1001} p^2 [x^2 \sin^2 \theta + (1 - \frac{11}{18}y^2)(1 + \cos^2 \theta)] \quad (19)$$

$$\sim 1 + A_4 \cos^2 \theta,$$

$$A_4 = \frac{(1 - \frac{11}{18}y^2) - x^2}{(1 - \frac{11}{18}y^2) + x^2} \quad (20)$$

The difference between  $H_2(\theta, 40)$  and  $H_4(\theta, 40)$  is more obvious. Therefore we can use these angular distributions of the photon for the moments to discriminate the spin of  $\xi$  (and  $\theta/f_2$ ).

#### IV. CONCLUSION

We know that the results of the ratio of helicity amplitudes of the fit for  $\xi$  and  $\theta/f_2$  are

		+0.14	+0.21
$\xi(J=2)$	$x = -0.67$	$y = 0.13$	
		-0.16	-0.19
		+0.62	+0.76
$\xi(J=4)$	$x = 1.29$	$y = 0.4$	
		-0.30	-0.39
$\theta/f_2$	$x = -1.07 \pm 0.16$	$y = -1.09 \pm 0.15$	(21)

Using these  $x$  and  $y$  (omitting the errors) from eqs. (13), (15), (18) and (20) we have

	$A_1$	$A_2$	$A_3$	$A_4$
$\xi(J=2)$	0.373		3.96	
$\xi(J=4)$		-0.453		-0.297
$\theta/f_2$	-1.39	-0.138	-8.29	-0.614

Applying eqs. (12), (14), (17) and (19) the angular distributions of the photon for the moments are shown in Fig. 1, 2, 3, 4. For  $\theta/f_2$  (1720) as shown in Fig. 2 the behaviors of  $H_2(\theta, 40)$  and  $H_4(\theta, 40)$  are very different, that is the angular distributions of the photon for these moments are very sensitive for different spin ( $J=2$  and  $4$ ) of  $\theta/f_2$ . For  $\xi$  (2230) the behaviors of these angular distributions are very different too (see Fig. 3, 4). We expect that using our generalized moment analysis experimentalists will get valuable results after performing a re-analysis of  $J/\psi \rightarrow \gamma K K$ ,  $J/\psi \rightarrow \gamma \pi \pi$  and  $J/\psi \rightarrow \gamma \eta \eta$ . We hope also that a certain conclusion for the spin of  $\xi$  (2230) can be obtained soon. Moreover after determining the spin of  $\xi$  (2230) (and  $\theta/f_2$ ) we can fit the angular distributions



of the photon for the moments to get the ratio of the helicity amplitudes  $x$  and  $y$  more exactly.

Figure Captions

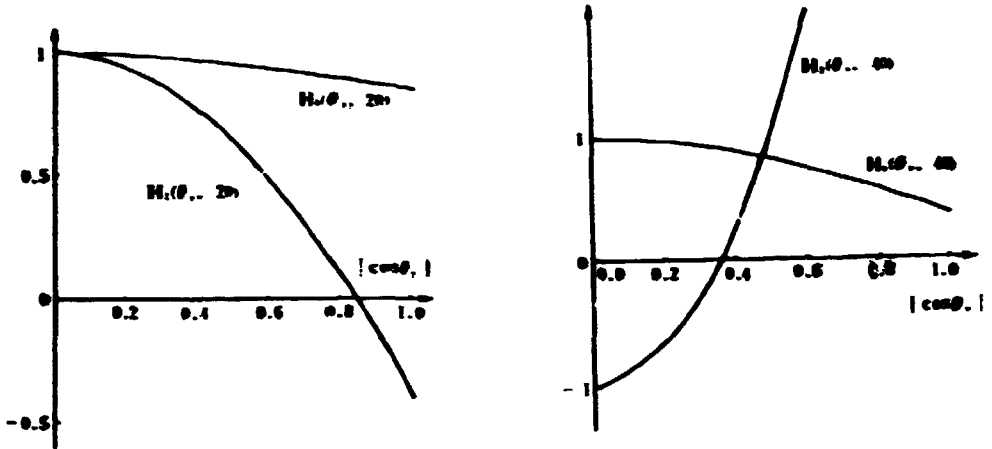


Fig.1,2. The angular distributions of the photon for moments of  $e^+e^- \rightarrow J/\psi \rightarrow \gamma 0$ ,  $(JLM) = (220)$ ,  $(420)$  and  $(240)$ ,  $(440)$ .  
 $\rightarrow P_1 P_2$

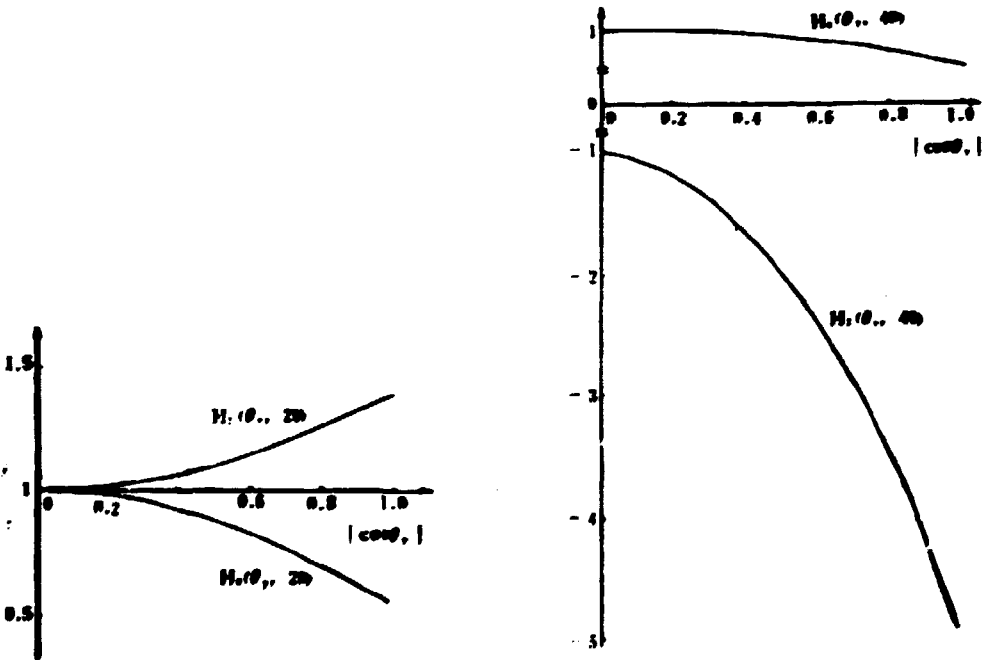


Fig.3,4. The angular distributions of the photon for moments of  $e^+e^- \rightarrow J/\psi \rightarrow \gamma \xi$ ,  $(JLM) = (220)$ ,  $(420)$  and  $(240)$ ,  $(440)$ .  
 $\rightarrow P_1 P_2$

### References

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# 1. 引言

MARK III组通过以下过程

$$e^+e^- \longrightarrow J/\psi \longrightarrow \gamma \chi \quad (1)$$

$\chi \begin{cases} K^+K^- \\ K_s^0\bar{K}_s^0 \end{cases}$

发现了一个新的态 $\chi(2230)^{11}$ 。DM2组考察了同样的过程，但在 $KK$ 质量谱中没有发现2.23 GeV处有明显的结构<sup>12</sup>。MARK III组用最大似然法<sup>13</sup>对 $\chi$ 的自旋进行了分析，所用程序完全类似于对 $\theta/\Upsilon_2(1720)$ 的分析。然而不能确定 $\chi$ 的自旋是2还是4，由于 $\chi$ 和 $\theta/\Upsilon_2$ 一样衰变为两个赝标介子，所以宇称和电荷共轭宇称都是+，自旋为偶。

在文献[4]中，我们指出： $\theta/\Upsilon_2$ 的自旋目前公认为 $J=2$ 。实际上，我们发现若用一般的螺旋性形式中的角分布去定 $\theta/\Upsilon_2$ 的自旋时，存在不敏感区。而 $\theta/\Upsilon_2$ 的数据恰好落入不敏感区。所以我们认为不能确定地说， $\theta/\Upsilon_2$ 的自旋就是 $J=2$ 。对于 $\chi$ 的自旋，目前不能确定它是2还是4，一个明显的原因是数据太少，另一原因就是 $\chi$ 的数据可能正好落入不敏感区。

本文试图用矩分析法<sup>14</sup>给 $\chi$ (和 $\theta/\Upsilon_2$ )的自旋的确定另辟一条新的途径。

## II. 角分布

我们考虑反应过程

$$e^+ + e^- \longrightarrow J/\psi \longrightarrow \gamma + B(J^*) \quad (2)$$

其中，共振底色子 $B$ 的自旋为 $J$ ，宇称为 $\eta$ 。然后 $B$ 继续衰变为两个赝标介子 $P_1$ 和 $P_2$ (这样 $\eta$ 必然为+)

$$B(J^*) \longrightarrow P_1 + P_2 \quad (3)$$

在一般的螺旋性形式中，该过程的角分布公式为

$$W(\theta, \phi, \psi) \propto \sum_{\lambda_1, \lambda_2} I(\lambda_1, \lambda_2) A_{\lambda_1, \lambda_2} A_{\lambda_1, \lambda_2}^* D_{-\lambda_1, 0}^{\lambda_2}(\phi, \theta, 0) D_{-\lambda_2, 0}^{\lambda_1}(\phi, \theta, 0) \quad (4)$$

其中

$$A_{\lambda_1, \lambda_2} \sim \langle \gamma_{\lambda_1} B_{\lambda_2} | \mathbb{T} | \psi_{\lambda_3} \rangle \quad (5)$$

是螺旋性振幅。 $\lambda_1$ 、 $\lambda_2$ 和 $\lambda_3$ 分别是光子、 $B$ 和 $J/\psi$ 粒子的螺旋性。

$$I(\lambda_1, \lambda_2) \propto \frac{1}{4} \sum_{\lambda_3} \langle \psi_{\lambda_3} | \mathbb{T} | e^+e^- \rangle \langle \psi_{\lambda_3} | \mathbb{T} | e^+e^- \rangle^* \quad (6)$$

$(\theta, \phi)$ 描写 $B$ 静止系中 $P_1$ 粒子动量的方向。这里我们选择光子出射方向为 $z$ 轴， $e^+e^-$ 束流在 $x-z$ 平面内。在 $J/\psi$ 静止系，略去包含 $(m_0/p)$ 的小项，我们有

$$I(1, 1) = I(-1, -1) \approx p^2(1 + \cos^2\theta)$$

$$I(1, 0) = I(0, 1) = -I(-1, 0) = -I(0, -1) \approx \frac{1}{\sqrt{2}} p^2 \sin 2\theta, \quad (7)$$

$$I(1, -1) = I(-1, 1) \approx p^2 \sin^2\theta,$$

$$I(0, 0) \approx 2p^2 \sin^2\theta,$$

其中 $p = |p_+| = |p_-|$ ， $p_+$ 和 $p_-$ 是正、负电子的动量， $\theta$ 是光子和正电子束之间的夹角。

### III. 矩分析

在文献[5]中给出了如 $B(J^1) \rightarrow B_1(1^-) + B_2(1^-)$ ,  $B_1$ 和 $B_2$ 继续衰变为两个赝标介子( $B_1 \rightarrow P_1 P_2$ ,  $B_2 \rightarrow P_3 P_4$ )等过程的矩以及对一定的自旋 $J$ 和宇称 $\eta$ 组合的各种矩之间的线性关系式。根据这些关系式,我们能够确定 $B$ 粒子的自旋和宇称。而且某些关系式相当有效。但是,我们现在观察到的 $\xi$ (以及 $\theta/f_2$ )的衰变方式仅是双赝标介子道。因此,我们不能用[5]中给出的任何关系式来辨别 $\xi$ 的自旋。

现在,我们把矩分析推广到过程

$$e^+e^- \rightarrow J/\psi \rightarrow \gamma + B(J^1) \quad (8)$$

$\searrow$   
 $P_1 + P_2$

引进该过程的矩的光子角分布,它被定义为

$$H_J(\theta_\gamma, LM) = \int W_J(\theta_\gamma, \theta, \phi) D_{M,0}^L(\phi, \theta, 0) \sin\theta d\theta d\phi \quad (9)$$

这是一个实验上可测量的量。从(4)式,我们有

$$H_J(\theta_\gamma, LM) = \frac{4\pi}{2J+1} \sum_{\lambda\lambda'} I(\lambda_J, \lambda'_J) A_{\lambda_\gamma, \lambda} A_{\lambda_\gamma, \lambda'} \quad (10)$$

$$(J-A'LM|J-A) \cdot (J0L0|J0)$$

$$= \frac{4\pi}{2J+1} t_{J, L}^{M, 0}(\theta_\gamma) (J0L0|J0)$$

这里  $(j_1 m_1 j_2 m_2 | j_3 m_3)$  是通常的C-G系数,多极参数为

$$t_{J, L}^{M, 0}(\theta_\gamma) = \sum_{\lambda\lambda'} I(\lambda_J, \lambda'_J) A_{\lambda_\gamma, \lambda} A_{\lambda_\gamma, \lambda'} (J-A'LM|J-A) \quad (11)$$

我们取 $L$ 为偶数,则 $t_{J, L}^{M, 0}(\theta_\gamma)$ 为纯实。我们可按照螺旋性振幅之比 $x$ 和 $y$ 以及用式(7)来表示 $H_J(\theta_\gamma, LM)$ 。对于 $L=2$ 的情况,我们有

$$H_2(\theta_\gamma, 22) = H_2(\theta_\gamma, 2-2) \propto -\frac{16\pi}{35} p^2 y \sin^2 \theta_\gamma$$

$$H_2(\theta_\gamma, 21) = -H_2(\theta_\gamma, 2-1) \propto -\frac{4\sqrt{2}\pi}{35} p^2 (x - \sqrt{8}xy) \sin 2\theta_\gamma$$

$$H_2(\theta_\gamma, 20) \propto \frac{16\pi}{35} p^2 [x^2 \sin^2 \theta_\gamma + (1-y^2)(1+\cos^2 \theta_\gamma)] \quad (12)$$

$$\sim 1 + A_1 \cos^2 \theta_\gamma$$

$$A_1 = \frac{1-y^2-x^2}{1-y^2+x^2} \quad (13)$$

$$H_4(\theta_\gamma, 22) = H_4(\theta_\gamma, 2-2) \propto -\frac{16\sqrt{15}\pi}{231} p^2 y \sin^2 \theta_\gamma$$

$$H_4(\theta_\gamma, 21) = -H_4(\theta_\gamma, 2-1) \propto -\frac{8\sqrt{15}\pi}{693} p^2 (x - \frac{9}{\sqrt{10}}xy) \sin 2\theta_\gamma$$

$$H_4(\theta_\gamma, 20) \propto \frac{272\pi}{693} p^2 [x^2 \sin^2 \theta_\gamma + \frac{10}{17} (1 + 0.4y^2)(1 + \cos^2 \theta_\gamma)] \quad (14)$$

$$\sim 1 + A_2 \cos^2 \theta_\gamma,$$

$$A_2 = \frac{\frac{10}{17} (1 + 0.4y^2) - x^2}{\frac{10}{17} (1 + 0.4y^2) + x^2} \quad (15)$$

这里, 和一般的螺旋性形式中光子的角分布<sup>[4]</sup>可相比的 $H_2(\theta_\gamma, 20)$ 和 $H_4(\theta_\gamma, 20)$ 显然是不同的。而在一般的螺旋性形式中的光子的角分布不管 $J=2$ 或者 $4$ 有相同的表达式:

$$W_J(\theta_\gamma) \sim 1 + A \cos^2 \theta_\gamma,$$

$$A = \frac{1 + y^2 - 2x^2}{1 + y^2 + 2x^2} \quad (16)$$

对于 $L=4$ , 我们有

$$H_2(\theta_\gamma, 40) \propto -\frac{64\pi}{105} p^2 [x^2 \sin^2 \theta_\gamma - 0.75(1 + \frac{1}{6}y^2)(1 + \cos^2 \theta_\gamma)] \quad (17)$$

$$\sim -(1 + A_2 \cos^2 \theta_\gamma)$$

$$A_2 = \frac{-0.75(1 + \frac{1}{6}y^2) - x^2}{-0.75(1 + \frac{1}{6}y^2) + x^2} \quad (18)$$

$$H_4(\theta_\gamma, 40) \propto \frac{144\pi}{1001} p^2 [x^2 \sin^2 \theta_\gamma + (1 - \frac{11}{18}y^2)(1 + \cos^2 \theta_\gamma)] \quad (19)$$

$$\sim 1 + A_4 \cos^2 \theta_\gamma,$$

$$A_4 = \frac{(1 - \frac{11}{18}y^2) - x^2}{(1 - \frac{11}{18}y^2) + x^2} \quad (20)$$

$H_2(\theta_\gamma, 40)$  和  $H_4(\theta_\gamma, 40)$  之间的差别更加明显。因此, 我们可以用矩的光子角分布来分辨 $\xi$  (以及 $\nu/f_2$ ) 的自旋。

## IV. 结 果

我们知道, 对于 $J/\psi$ 辐射衰变产生 $\xi$ 和 $\theta/f_2$ 的螺旋性振幅之比  $x, y$ , 拟合的结果是<sup>[6]</sup>:

$$\begin{aligned} \xi(J=2) \quad x &= -0.67 \pm 0.14 & y &= 0.13 \pm 0.19 \\ \xi(J=4) \quad x &= 1.29 \pm 0.62 & y &= 0.4 \pm 0.39 \\ \theta/f_2 \quad x &= -1.07 \pm 0.16 & y &= -1.09 \pm 0.15 \end{aligned} \quad (21)$$

我们把这些值 (略去误差) 代入式 (13), (15), (18), (20), 则有

	$A_1$	$A_2$	$A_3$	$A_4$
$\xi(J=2)$	0.373		3.96	
$\xi(J=4)$		-0.453		-0.297
$\theta/f_2$	-1.39	-0.138	-8.29	-0.614

应用式(12)、(14)、(17)和(19),我们得到矩的光子角分布,如图1,2,3,4所示。对于 $\theta/f_2$ ,从图2可看到 $H_2(\theta, 40)$ 和 $H_4(\theta, 40)$ 的行为很不相同,即这种矩的光子角分布对于辨别 $\theta/f_2$ 的自旋为2或4十分敏感。对于 $\xi$ , $H_2(\theta, 20)$ 和 $H_4(\theta, 20)$ , $H_2(\theta, 40)$ 和 $H_4(\theta, 40)$ 的差别均十分明显。于是,我们可以期望,实验物理学家用这个方法在对 $J/\psi \rightarrow \gamma K \bar{K}$ 、 $\gamma \pi \pi$ 、 $\gamma \eta \eta$ 进行重新分析之后将会得到某些有价值的结论。希望关于 $\xi(2230)$ 的自旋的确定的结论不久将会作出。此外,在确定了 $\xi$ (和 $\theta/f_2$ )的自旋之后,我们通过拟合矩的光子角分布可得到更精确的螺旋性振幅之比 $x$ 和 $y$ 。

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