INSTITUTE FOR HIGH ENERGY PHYSICS

 $iHEP - OTP - P1 - 113$ 

IHEF 91-113 ОТ

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# **Odderon Contribution in U-matrix Method**

Protvino 1991

#### **Abstract**

P.M.Nadolsky. Odderon Contribution in U-matrix Method: IHEP Preprint 91-113. — Protvino,  $1991. -p.$  11, refs.: 15.

The behaviour of the differences of the proton-proton and proton-antjproton cross sections is studied with the help of the U-matrix method in the presence of the C-odd partnei of pomeron.

#### **Аннотаци**

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 $\frac{1}{2} \frac{d^2}{dt^2}$ 

П.М.Надольский. О вкладе оддерона в методе U-матрицы: Препринт ИФВЭ 91-113. — Протвино, 1991. — 11 с., библиогр.: 15.

В методе U-матрицы исследуется поведение разностей протон-протонных и протонантипротонных сечений при наличии вклада нечетного партнера померона.

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## **1 Introduction**

One of the most important results obtained in the expirements on hadronhadron scattering is the discovery of the continuing growth of the total cross-sections in the high-energy region . The data recieved at IHEP , CERN-ISR , FNAL and SppS-colliders suggests that the maximal allowed growth of the total cross-sections , saturating the Proissart bound , is possible :

$$
\sigma_{tot} \sim \log^2 s,\tag{1}
$$

at  $s \rightarrow \infty$ .

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Besides that , the measurement of the differential cross-sections has shown that at  $-t = Q^2 \simeq 1 \div 2$  the differential pp-cross-section is by an order of magnitude higher than the proton-proton one and has the form of a "shoulder " instead of a dip . The recent experiments at SppS reveal that the geometrical scailing is violated: the ratio of the elastic to the total cross - sections  $\sigma_{el}/\sigma_{tot}$ , which remained constant for a long time, increases from 0.175 at  $\sqrt{s} = 53$  to 0.215 at  $\sqrt{s} = 900$ . Due to this fact the modern models take into account not only pomeron , which leads to the asymptotic equality of  $pp-$  and  $p\bar{p}$ -cross-sections, but also its crossing-odd partner named "odderon" . Since the last one dominates in the region of high *t*, its presence must lead to different dependence of particle-particle and particleantiparticle reactions on the scatteing angle ; moreover , it may provide the constancy and even the growth of the difference of the total *pp—* and  $p\bar{p}$ -cross-sections  $\Delta \sigma_{tot} = \sigma_{tot} - \sigma_{tot}^a$ . For instance, in the scenarios of

the "maximal" odderon it grows with the maximal rapidity allowed by the general theory of scattering :

$$
\Delta \sigma_{tot} \sim \log s. \tag{2}
$$

Lately the interest in the models providing the maximal growth of  $\Delta\sigma_{tot}$ has been considerably renewed since they predict the increase of the ratio of the real to the imaginary part of the forward amplitude  $\rho(s, 0) = \frac{Re F(s, 0)}{Im F(s, 0)}$ the effect recently reported by UA4 Collaboration [1] .

However , it has been argued in [2] that the account of the ampli tude unitarity in the framework of the eikonal parametrization permits to achieve at most constant, but not growing,  $\Delta \sigma_{tot}$ . This constancy is obtained only when the leading pomeron and odderon trajectories are degene rate . If the pomeron lies above the odderon,  $\Delta \sigma_{tot}$  vanishes as  $s^{\beta}$ ,  $\beta < 0$ . Certainly , it is interesting to find out if it is possible to achieve the maxi mal odderon in another parametrizations of the scattering amplitude . For example , the approach using the generalized reaction matrix preserves the unitarity of the amplitude [3] and is very convenient for the explicit treat ment of our problem . In this work we shall calculate the total and elastic cross-sections with the help of the U-matrix formalism ; after that we shall make a comparison with the results of the eikonal representation . It will be shown that both approaches give the coinciding predictions about the behaviour of the total cross-sections at  $s \to \infty$ . However, the U-matrix leads to a constant difference of the elastic cross-sections  $\Delta\sigma_{el}$  while the eikonal  $\Delta\sigma_{el}$  and  $\Delta\sigma_{inel}$  grow with the same rate ( as log s ), but have opposite signs , and their contributions vanish.

### **2 General properties of the U-matrix**

In the high-energy region the scattering amplitude  $F(s,t)$  can be written with the help of the generalized reaction matrix ( U-matrix ) , arising from the single-time formulation of the two-body problem in QFT [4] . The essential feature of this theory is the introduction of the quasipotential , which is the analogue of the usual quantum-mechanics potential for the relativistic case . Unlike the Bethe-Salpeter equation , the choice of boundary conditions using the quasipotential can be made in a rather sim ple way ; moreover, due to the non-conservation of the number of the particles in quantum field theory , the effective potential is complex , and

its imaginary part must have definite sign to satisfy the untarity condi tions . There exists a simple relation between the analytical properties of the quasipotential and those of the scattering amplitude , which al lows first to make the analytical continuation from *s—* to t—channel for the quasipotential and after that go over to the analytical continuation of the amplitudes without any extra restrictions on the behaviour of Regge trajectories .

According to [5, 6] , in the centre-of-mass system we can write the fol lowing singletime equation:

$$
F(\vec{p},\vec{q}) = U(\vec{p},\vec{q}) + \frac{i\pi\rho(s)}{8} \int d\Omega_{\vec{k}} U(\vec{p},\vec{k}) F(\vec{k},\vec{q}) , \qquad (3)
$$

where  $F(\vec{p}, \vec{q})$  is the scattering amplitude,  $p = k = q$ ,  $\rho(s) = \sqrt{\frac{s-4m^2}{s}}$ . The U-matrix , just like the amplitude , contains all the nessesary infor mation about the scattering process . It can be shown that non-Hermitian part of the U-matrix appears due to the presence of inelastic channels ; if we introduce the symbolic notations , in which Eq.3 is written as

$$
F = U + i \, UDF,\tag{4}
$$

and the amplitude unitarity condition as

$$
F - F^+ = 2iF^+DF + 2iH \tag{5}
$$

( here H is the inelastic contribution ) , then

$$
U - U^{+} = 2i(1 + iU^{+}D)H(1 - iDU).
$$
 (6)

Passing over to the impact parameter space we get

$$
F(s,t) = \frac{s}{\pi^2} \int_0^\infty bdb \frac{U(b,s)}{1 - iU(b,s)} J_0(b\sqrt{-t})
$$
 (7)

and

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$$
\sigma_{inel}(s,t) = 8\pi \int_0^\infty bdb \frac{Im U(b,s)}{|1 - iU(b,s)|^2} J_0(b\sqrt{-t}), \qquad (8)
$$

where  $U(b,s)$  is the Fourier-Bessel transform for  $U(s,t)$ :

$$
U(b,s) = \frac{\pi^2}{s} \int_0^\infty \sqrt{-t} d\sqrt{-t} U(s,t) J_0(b\sqrt{-t}). \tag{9}
$$

To close this section let us say a few words about the description of Regge poles in this approach. Suppose that not  $F(s,t)$  but  $U(s,t)$  is proportional to  $s^{\boldsymbol{\alpha}}(t)$  , where  $\boldsymbol{\alpha}(t)$  is the pole trajectory in the complex angular momentum plane . A crossing-even (crossing-odd ) pole  $\alpha_{\pm}(t)$  is thus related to the matrix

$$
U_{\pm}(s,t) = -g_{\pm}\xi_{\pm}(t)s^{\alpha_{\pm}(t)}\,,\tag{10}
$$

where  $g_{\pm} > 0$  are real constants and  $\xi_{\pm}(t)$  are signature factors. Such choice makes the conditions of the amplitude unitarity explicit just from the beginning and helps to avoid procedures of the additional unitarisation for superhigh energies . If it is nessesary to take account of several Regge poles , the resulting U-matrix must be the sum of the U-matrices for the individual poles .

# **3 Pomeron and odderon in the U-matrix method**

For a long time , just till the early 70's , the collider data seemed to demonstrate the tendency of the particle-particle and particle-antiparticle total cross-sections to the same constant limit satisfying the well-known Pomeranchuk theorem . Nevertheless the results obtained at Serpukhov and later at CERN-ISR clearly indicated that in the new domain of energies the total cross-sections began to increase again ; soon it was found that the differential *pp—*and *pp—*cross-sections as well had different, behaviour . Since such growth does not depend on the sort of the colliding particles , it is natural to suppose that in the asymptotical region the main contribution is provided by the Pomeranchuk pole , or pomeron ; moreover , the trustworthy description of  $\sigma_{tot}^p$  and  $\sigma_{tot}^q$  must also include its crossing-odd partner , or odderon ( see early references in [7] ) .

From the point of view of QCD the pomeron-odderon structure of the amplitude directly arises from the hypothesis of the"gluon dominance" [8] . The asymptotical interaction must occur due to the exchange by some number of gluons in a colourless state , because the contributions from the quark exchanges fall down like a power of *s.* The reggeization of crossing-even exchanges leads to the pomeron and of crossing-odd ones — to the odderon . At the same time the introduction of odderon does not contradict the basic QFT principles , and a *priori* nothing forbids the maximal growth of **4**

basic QFT principles , and *a priori* nothing forbids the maximal growth of  $\Delta \sigma_{tot}$ , namely as  $\log s$ .

The scenarios with such saturating increase of  $\Delta \sigma_{tot}$  are named " the models of the maximal odderon " : for instance , in [9] the form of the ampli tude , chosen on the base of motto "Strong interactions must be maximally strong", provides both the saturation of  $\Delta \sigma_{tot}$  and the increase of  $\rho(s,0)$ . On the other hand there exists a number of models with the "minimal" odderon [10, 11], which predict  $\Delta \sigma_{tot} \rightarrow 0$ ; in one of these approaches [12] it is even possible to verify the value of  $\rho(s,0)$  and show that the special parametrization of the experimental cross-sections gives the reasonable values of  $\rho$  [ 0.136 instead of 0.24 ]. Certainly,  $\Delta \sigma_{tot}$  in reality may also tend to some constant . Let us now see , which alternative is realized in the U-matrix treatment of the amplitude .

Suppose that the main contributions into the high-energy amplitude are made by one pomeron and one odderon . Of course , there arises a question if the really existing singularities have such simple structure or not . For instance , in the perturbative QCD using the "leading log" approximation, pomeron and odderon appear as two- and three-gluon bound states ; in this case pomeron must consist at least of two Reg ge poles [13] . Nevertheless this calculation implies that the odderon trajectory lies above the pomeron one , which is incompatible with the amplitude unitarity . Besides that , the presence of several Regge poles does not differ , in principle , ( as a consequence of the U-matrix addi tivity ) from the case of the non-coinciding pomeron and odderon and has no influence on the qualitative behaviour of the leading term in the asymptotical expansion : it is still determined only by leading poles .

If the pomeron and odderon trajectories are linear and correspondingly are written as  $\alpha_{\pm}(t)=1+\Delta_{\pm}+\alpha_{\pm}'(t)$  , where  $\Delta_{\pm}>0, \alpha_{\pm}'>0$  , by the direct calculation of Eq. 9 we get

$$
U_{+}(b,s) = \frac{\lambda_{+}}{B_{+}(s)} \bar{s}^{\Delta_{+}} \exp(-\frac{b^{2}}{B_{+}(s)}),
$$
  

$$
U_{-}(b,s) = \frac{i\lambda_{-}}{B_{-}(s)} \bar{s}^{\Delta_{-}} \exp(-\frac{b^{2}}{B_{-}(s)}).
$$
 (11)

Here  $\lambda_+ = \frac{2\pi^2 g_+}{\sin \frac{\pi}{2}(1 + \Delta_+)}, \lambda_- = \frac{2\pi^2 g_-}{\cos \frac{\pi}{2}(1 + \Delta_-)}, \bar{s} = s \exp(-i\frac{\pi}{2}), B_{\pm}(s) = 4\alpha'_{\pm} \log \bar{s}$ 

One can note that the logarythmical behaviour of  $B_{\pm}(s)$  provides the saturation of the Froissart bound : it follows from Eq. 11 that the effective radius of the interaction  $b_{max} \sim \log s$  and  $\sigma_{tot} \sim b^2_{max} \sim \log^2 s$ .  $\hspace{1cm} 5$ 

The *pp—* and *pp—* forward amplitudes look like

$$
F^{p(a)}(s,0)=\frac{s}{\pi^2}\int bdb\frac{U_+(b,s)\pm U_-(b,s)}{1-i(U_+(b,s)\pm U_-(b,s))}.\tag{12}
$$

We can as well denote

$$
F^+(s,0) = F^p(s,0) + F^a(s,0) = \frac{2s}{\pi^2} \int bdb \frac{U_+^2 - U_-^2 + U_+}{[1 + U_+]^2 - U_-^2},
$$
 (13)

$$
F^{-}(s,0) = F^{p}(s,0) - F^{a}(s,0) = \frac{2s}{\pi^{2}} \int bdb \frac{U_{-}}{[1+U_{+}]^{2} - U_{-}^{2}} \tag{14}
$$

and obtain the equations

$$
\sigma_{tot} = \sigma_{tot}^p + \sigma_{tot}^a = \frac{8\pi^3}{s} Im F^+(s,0)
$$
\n(15)

$$
\Delta \sigma_{tot} = \sigma_{tot}^p - \sigma_{tot}^a = \frac{8\pi^3}{s} Im F^-(s, 0). \tag{16}
$$

The unitarity of  $F^{p(a)}(s,0)$  leads to the inequalities  $\Delta_+ \geq \Delta_-$  ,  $\alpha'_+ \geq \alpha'_-$  . In this case the behaviour of the intergrands in Eq. 13 and Eq. 14 at fixed *b* and growing *s* is different : it tends to a constant in the first equation and infinitely vanishes in the second one . This gives some reason to suspect that  $\Delta\sigma_{tot}$  does not grow in the "asymptopia" ; let us prove that for a special choice of the parameters  $\alpha'_{+} = \alpha'_{-} = \alpha'$ ,  $\Delta_{+} = \Delta_{-} = \Delta$ ,  $B_{\pm}(s) = B(s)$ .

# **4** The calculation of  $\Delta\sigma_{tot}$

It can be shown that  $\Delta\sigma_{tot}$  grows more rapidly if the trajectories are degenerate rather if they do not coincide ; moreover , it is argued in [15] , that this degeneracy may appear in QCD as a result of the quark confinement . Then

$$
U^{p(a)}(b,s) = \frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta} \exp(-\frac{b^2}{B(s)}). \tag{17}
$$

From Eq. 12 we come to

$$
F^{p(a)}(s,0)=\frac{s}{\pi^2}\int_0^\infty bdb\frac{\lambda_+\pm i\lambda_-}{B(s)}\bar{s}^\Delta\exp(-\frac{b^2}{B(s)})\frac{1}{1-i\frac{\lambda_+\pm i\lambda_-}{B(s)}\bar{s}^\Delta\exp(-\frac{b^2}{B(s)})}.
$$
(18)

After the standard substitution this integral is easily calculated and we get

$$
\sigma_{tot}^{p(a)} = 4\pi Re \Big\{ B(s) \log(1 + \frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta}) \Big\}.
$$
 (19)

Denote

$$
\rho_{\lambda} = \sqrt{\lambda_+^2 + \lambda_-^2}, \theta_0 = \frac{\pi}{2}(\Delta + 1) - arctg \frac{\pi}{2 \log s} \rightarrow \frac{\pi}{2}(\Delta + 1)
$$

as  $s \to \infty$ . Now we can pick out the growing term  $\log(\frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta})$  and expand the remaining summand into the series of  $\left(\frac{B(s)}{\lambda + \pm i\lambda}\right)^{-\Delta}$ . After the calculation of the real part we find that

$$
\sigma_{tot}^{p(a)} \to 4\pi \Big\{ 4\alpha' \Big\{ \Delta \log^2 s + \log \Big( \frac{\rho_{\lambda}}{4\alpha' \log s} \Big) \log s +
$$
  

$$
+ \frac{4\alpha'}{\rho_{\lambda}} \cos(\theta_0 \mp \arctg(\frac{\lambda_{-}}{\lambda_{+}})) s^{-\Delta} \log^2 s \Big\} - 2\pi \alpha' \Big\{ \theta_0 \mp \arctg(\frac{\lambda_{-}}{\lambda_{+}}) -
$$
  

$$
- \frac{4\alpha'}{\rho_{\lambda}} \sin(\theta_0 \mp \arctg\frac{\lambda_{-}}{\lambda_{+}}) s^{-\Delta} \log s \Big\} \Big\}. \tag{20}
$$

This, in its turn, implies

$$
\sigma_{tot} \simeq 32\pi\alpha' \Delta \log^2 s \tag{21}
$$

and

$$
\Delta \sigma_{tot} = 16\pi \alpha' \arctg \frac{\lambda_{-}}{\lambda_{+}} + \frac{\pi}{2} \lambda_{-} (\frac{16\alpha'}{\rho_{\lambda}})^{2} \cos(\frac{\pi}{2} \Delta) s^{-\Delta} \log^{2} s + + \lambda_{-} (\frac{8\pi \alpha'}{\rho_{\lambda}})^{2} \sin(\frac{\pi}{2} \Delta) s^{-\Delta} \log s.
$$
 (22)

As we have expected, the presence of the pomeron with the non-zero intercept  $\Delta$  leads to the saturating growth of  $\sigma_{tot}$ . However, the odderon provides only constant  $\Delta \sigma_{tot}$ ; we also notice that  $\Delta \sigma_{tot} \to 0$  if  $\lambda_- \to 0$ , i.e. the difference of the total cross-sections is really appearing due to the odderon.

#### The calculation of the total elastic cross- $\bf{5}$ sections

From Eq. 8 and Eq. 17 we get the expression

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$$
\sigma_{inel}(s,0) = 8\pi \int_0^\infty bdbIm \frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta} \exp(-\frac{b^2}{B(s)}) \frac{1}{|1 - i\frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta} \exp(-\frac{b^2}{B(s)})|^2}
$$
(23)

After the substitution  $z = z_0 e^{-\frac{b^2}{B}}, z_0 = -i\frac{\lambda_+ \pm i\lambda_-}{B(s)} \bar{s}^{\Delta}$ , Eq. 23 takes the form

$$
\sigma_{inel}^{p(a)}(s,0) = 8\pi Re \int_0^{s_0} \frac{B}{2} \frac{dz}{|1+z|^2}.
$$
 (24)

Since the integrand has no singularities in the integration region, Eq. 23 is easily calculated when  $s \to \infty$ .

Finally we get

$$
\sigma_{inel}^{p(a)} = 4\pi \Big\{ 4\alpha' \log s + \frac{16\alpha'^2}{\rho_{\lambda}} \Big\{ \cos(\theta_0 \mp \arctg \frac{\lambda_-}{\lambda_+}) - 2 \Big\} s^{-\Delta} \log^2 s - \frac{8\alpha'^2}{\rho_{\lambda}} \pi \sin(\theta_0 \mp \arctg \frac{\lambda_-}{\lambda_+}) s^{-\Delta} \log s \Big\}. \tag{25}
$$

The difference  $\Delta \sigma_{inel} = \sigma_{inel}^p - \sigma_{inel}^a$  vanishes in the high-energy limit:

$$
\Delta \sigma_{inel} = \frac{\pi}{2} \lambda_{-} (\frac{16\alpha'}{\rho_{\lambda}})^{2} \cos(\frac{\pi}{2} \Delta) s^{-\Delta} \log^{2} s +
$$

$$
+ \lambda_{-} (\frac{8\pi \alpha'}{\rho_{\lambda}})^{2} \sin(\frac{\pi}{2} \Delta) s^{-\Delta} \log s; \qquad (26)
$$

with the help of Eq. 22 we find

$$
\Delta \sigma_{el} = \Delta \sigma_{tot} - \Delta \sigma_{inel} = 16 \pi \alpha' arctg \frac{\lambda_{-}}{\lambda_{+}}.
$$
 (27)

In addition, asymptotically  $\sigma_{el} \sim \log^2 s$ .

This relation implies that the saturation of the Froissart bound arises due to the elastic scattering ; though  $\sigma_{inel}$  continues to rise, we find  $\sigma_{el}/\sigma_{tot} \rightarrow 1$ , which is in accordance with the demands of the general field theory.

#### 6 U-matrix in comparison with eikonal

The cross-sections found in Sec.4,5 were previously obtained with the help of the eikonal approximation  $[2],[14]$ . We must emphasize that 8

both methods give coinciding predictions about the behaviour of  $\sigma_{tot}$  and  $\Delta\sigma_{tot}$ , while the description of the scattering mechanisms is not the same. Though eikonal  $\Delta \sigma_{tot}$  also tends to constant when the leading trajectories are degenerate, the inelastic difference  $\Delta \sigma_{inel}$  still grows as log s; at the same time  $\Delta \sigma_{el}$  increases with the same rapidity but with opposite signs , so their contributions into  $\Delta\sigma_{tot}$  compensate each other. In the U-matrix treatment  $\Delta\sigma_{inel}$  falls down as a power of *s*; that is why even the constant  $\Delta\sigma_{tot}$  arises at the expense of the elastic reactions. This fact does not seem surprising since in the eikonal parametrization one obtaines  $\sigma_{el}/\sigma_{tot} \rightarrow \frac{1}{2}$  ; at the same time the U-matrix approach always provides  $\sigma_{el}/\sigma_{tot} \rightarrow 1$ . We shall as well observe that, unlike the eikonal picture where all  $\Delta\sigma$  depend on  $\lambda_{\pm}$  parameters only through their ratio  $\lambda_{-}/\lambda_{+}$  , in our case  $\Delta \sigma_{inel}$  is wholly determined by  $\lambda_-$  and  $\rho_\lambda$ . For the realistic choice of the intercept  $\Delta \approx 0.1 \div 0.2$  the signs of  $\lambda_{-}$  and  $\Delta \sigma_{inel}$  are to be the same , according to Eq. 26 . Moreover it follows from Eq. 22 that the information about the asymptotical signs of  $\Delta\sigma_{tot}$  and  $d\Delta\sigma_{tot}/ds$  is sufficient to make definite conclusions about the signs of  $\lambda_+$  and  $\lambda_-$ .

The same speculations can be conducted in the case of non-degenerate trajectories . Certainly , we cannot get the exact expressions for the values concerned since we have to take into account more than one exponential piece each time . However , the upper estimates show that  $\Delta\sigma_{tot}$  falls down if the pomeron lies above the odderon; namely  $\Delta \sigma_{tot} \sim s^{\beta}, \beta < 0$ , which is rather compatible with the eikonal predictions.

To conclude we stress that all the results of this paper concern the asymptotical behaviour of the cross-sections . Of course the functions in question may have extrema at finite energies . For example , it can be seen from Eq. 22 that in the used approximation  $d\Delta\sigma_{tot}/ds$  has two zeros, which satisfy the quadratic equation for  $\log s$ . These zeros are  $\log s = 0$ and  $\log s = \frac{2}{\Delta}$ , which for  $s_0 \approx 1$  GeV correspond to  $s \approx 1$  GeV and  $s \approx e^{\frac{2}{\Delta}} \approx e^{10} \div e^{20}$  GeV ; due to this  $\Delta \sigma_{tot}$  may temporarily grow at current energies . These speculations are on no account strict but the fact is that even in the one pomeron-one odderon model  $\Delta\sigma_{tot}$  may increase within a finite interval, though slower than log *s .* However , if the collider energies have already reached "asymptopia" ( though the experimental values of  $\sigma_{el}/\sigma_{tot}$  are still suspiciously far from 1), then the measurement of the elastic scattering may become critical to choose between U-matrix and eikonal parametrizations .

# **References**

- [1] . UA4 Collab.,D.Bernard et al.Phys.Lett. B198(1987) 583.
- [2] .J.Finkelstein,H.M.Fried,K.Kang and C.-I.Tan. Phys.Lett. B232(1989) 257.
- [3] .N.E.Tyurin,O.A.Khrastalev. TMF 24(1975) 291; Preprint IHEP 74-119 ,Serpukhov (1974).
- [4] .A.A.Logunov.A.N.Tavkhelidze.Nuovo Cimento 29(1963) 380.
- [5] .A.A.Logunov,V.I.Savrin,N.E.Tyurin,O.A.Khrustalev. TMF 6(1971) 157.
- [6] .V.F.Edneral,O.A.Khrustalev,S.M.Troshin,N.E.Tyurin. Preprint CERN TH.-2126,January 1976.
- [7] .J.Finkelstein.Phys.Rev.Lett.24(1970) 172; V.N.Gribov et al.Phys.Lett. B32(1970) 129.
- [8]  $.S.S.Gerstein, A.A.Logunov.HQ 39(1984) 1514.$
- [9] .P.Gauron,B.Nicolescu,E.Leader.Phys.Rev.Lett. 54(1985) 2656.
- [10] .C.Bourelli,J.Soffer,T.T.Wu.Phys.Rev.Lett. 54(1985) 757.
- [11] .L.L.Jenkovsky,A.N.Shelkovenko,B.V.Struminsky. Z.Phys. 36(1987) 496;ЯФ 466(1987) 1200.
- [12] .L.L.Jenkovsky,A.N.Shelkovenko,B.V.Struminsky. Письма в ЖЭТФ 47(1988) 288.
- [13] .L.N.Lipatov. $X$  $\Theta$ T $\Phi$  90(1986) 1536.

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- [14] .V.A.Petrov,A.P.Samokhin.Preprint CERN-TH.5583/89.
- [15] .A.V.Kisselev,V.A.Petrov.Proc.of the *XXIV* Rencontre de Moriond: New Results in Hadronic Interactions.Ed.by J.Tran Thanh Van. (Editions Frontieres,1989).

*Recieved July 18 , 1991*

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