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# **Design and Ther**m**al Stress Analysis of High Power X-ray Monochro**m**ators Cooled with Liquid Nitrogen.\***

C.S. Ro**g**e**rs** an**d** L.As**s**o**ufi**d Ex**perime**ntal **F**acilit**ies** D**i**vi**s**io**n** Advanced Photon Source, Argonne National Laboratory, Argonne, IL 60439-48**1**4

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 $T$ he submitted manuscript has been authored **by a co**n**trsctor of the U.**S**. Go**v**e**r**nment** I **under** c**ontrac**t **No. W-31-109**-**ENG-38.** I CZ<br>CZ contribution, or allow others to do so, for<br>contribution, or allow others to do so, for

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# **Design and thermal stress analysis of high power x-ray monochromators cooled with liquid nitrogen**

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**C. S. R**o**gers a**n**d L.** Ass**oufid The Advanced** P**hoton Sou**r**ce Argonne National Laboratory** Ar**gonne, IL60439, USA**

C**r**yo**genic**a**lly coo**l**e**d**,** singl**e-c**r**ystal** sili**c**on**,** x**-ray** mono**chr**o**mators** o**ffe**r mu**ch better thermal performance than** r**oom-temperature sil**i**con monochromators. The improved performance can be quantified by a figure-of-merit equal to** t**he** r**atio of the thermal conduc**ti**vity to the coefficient of the**r**mal expansion. This r**ati**o** i**ncre**a**ses by about a facto**r **of 50 as the temperature is decreased from 300 K to 100 K. An extensive** th**ermal and structural fi**ni**te element analysis is presented for an** in**clined, liquid**ni**trogen-cooled***,* **Si monochromator crystal diffracting 4.2 keV photon**s **from the [111] planes using Undulato**r **A at** th**e Advanced Photon** So**urce.** Th**e angula**r **size of the beam accepted on** th**e c**r**ystal was chosen** t**o be 50** \_**rad ve**rti**cally and 120** gr**ad horizontally.** Th**e deflection paramete**r**, K, was 2.1**7 f**or all cases. The peak powe**r **density** a**t normal incidence to** th**e beam was calculated to be 139 W***/***mm 2, and the total** power was 750 W at a distance of 30 m from the source for a positron current of 100 mA. **The crystal was o**r**iented in the** in**clined geome**tr**y wi**th **an inclin**a**tion angle o**f **85**" **fo**r **all cases. The performance of** th**e crystal was** in**ves**ti**gated fo**r **beam currents of 100, 200, and 300 mA. The calcul**a**ted peak slopes of the diffrac**tio**n plane over the extent of the** beam footprint were -1.17, -2.35, and 0.33 µrad, and the peak temperatures were 88.2, **102.6, and 121.4 K,** r**espec**ti**vely. The varia**ti**on in** th**e Bragg angle due** t**o change i**n **dspacing across the beam footpri**n**t was less than I** \_**rad for all cases.** Th**ese results indicate that a p**r**ope**r**ly designed, c**r**yoge**ni**cally c**oo**led,** in**clined silicon monochromato**r **can deliver the full b**r**illiance of U**n**dula**to**r A at even the highest mac**hin**e cu**rr**e**n**ts.**

# **I. INTRODUCTION**

**The use of cryogenically cooled, single-c**r**ystal opt**i**cs fo**r **high-heat-flux undulators is gaining wide spread interest in the synchrotron** r**adiation commun**i**ty. Bilderb**a**ck firs**t**po**i**n**t**ed ou**t **the po**t**en**ti**al for cryoge**ni**cally cooled, synchro**tr**o**n ra**d**iatio**n optical components** in **1986.1 In Orde**r **to take advantage of the full brilliance of the x**r**ay beams at the APS, the thermo-mecha**ni**cal strain** i**n the monoc**hr**omator crystal must be much smal**l**er** th**an** th**e** in**trin***s***ic reflec**ti**on width of the crystal. For example, the Bragg reflection width fo**r **Si [111] at 4.2 keV is** 7**0.6** \_t**rad. An aggressive research p**r**ogram has been mounted at** th**e APS to develop cryogenically cooled opt**i**cs. 2**

**T**hi**s paper presents** a **series of finite element analyses of an inc**li**ned,** cr**yoge**ni**cally cooled Si monoc**hr**omator for use with APS Undulator A. The undulato**r **characteristics can be found** in **Ref. 3. The** in**clined reflectio**n **geome**tr**y is a novel me**th**od of sp**r**eading out** th**e f**oo**tp**r**int of** th**e beam w**hi**le preserving symmetric dif**f**raction.4 At an incl**i**nation angle of 85** °**,** th**e peak heat flux is reduced by an addi**ti**onal facto**r **of 11.5 compared to** th**e standard B**r**agg geometry. Cryogencially cooled op**ti**cs lend** th**emselves very well to** t**he inc**li**ned geome**tr**y. Due to the inc**r**eased** th**ermal conduc**ti**vity,** th**e c**oo**ling** ch**annels can be placed much furthe**r **from** th**e diffractio**n **surface than ca**n **be done wi**t**h wate**r **o**r li**quid- metal cooling. Th**i**s allows fo**r **easier co**n**struc**t**ion of h**i**gh efficiency, heat exchanger config**ur**ations without adversely impac**ti**ng the dif**fr**action surface. Also,** th**e larger volume of** th**e crystal can be used** t**o tra**n**sport the heat***,* **thereby** r**educing** th**e heat flux at** th**e fluid interface** a**nd allevia**ti**ng** th**e possibility of boili**n**g.**

**Wo**r**k has been done** r**ecently to show how a cryoge**ni**cally cooled crystal ope**r**a**ti**ng in** t**he standard Bragg geome**tr**y can wo**r**k fo**r **Undulato**r **A at 100 mA. 5 I**n this work, the x-rays are set to diffract from a thin section, about 0.6 mm thick, of the **crystal. T**hi**s type of crystal is especially suited for low energies whe**r**e most of** t**he high ene**r**gy photons pass t**hr**ough without being absorbed. Use of a thin, par**ti**ally absorb**i**ng**

**crystal decreases the local heat flux and total absorbed powe**r**. This method** i**s** hi**ghly geometry dependent. The thin section must be no wide**r th**a**n th**e beam footp**r**int. Increasing** th**e thermal path length unnecessarily causes** th**e temperature to rise rapidly.**

# **II. THERMAL MODELING**

**The monochromato**r **c**r**ystal was modeled as a simpl**e **block cooled from the bottom surface. The crystal was 50 mm wide, 10 mm thick, and 90 mm long. Th**i**s size was chosen so** th**at** th**e inclined beam footprint at 4.2 keV would fit on the crystal. Fo**r **higher energies,** th**e crystal wo**ul**d necessarily be longe**r **if all other pa**r**amete**r**s a**r**e held constant.** H**owever, much can be done by changing the size of the accepted beam or using different incl**in**ation angles. Fo**r **example, a 190 mm x 25 mm S**i **[111] monochromator inclined at 85" and accepting a beam 1.5 mm x 1**.**5 mm co**ul**d scan to 20 keV.**

**T**h**e beam size normal to** th**e crystal was 1.5 mm vertically and 3.6 mm horizontally. This size includes the entire 1st har**m**o**ni**c in the central cone of radia**ti**on from the undulator. A uniform heat tra**ns**fe**r **coefficient of 5 W***/***cm 2** \***C was applied to** th**e bo**tt**om surface. This value is** r**eadily obtainable by using po**r**ous-media-enhanced coo**li**ng.6 The b**ul**k** nitr**ogen temper**a**t**ur**e was** 77 **K.** Th**e heat load was applied as a s**ur**face heat flux. The incidence angle was 2.35**\* **to** th**e plane of the crystal su**r**face. Because the incidence angle is so small,** th**e assumption of absorption at the surface is adequate. The thermal conductivity and coefficient of thermal expa**ns**ion were treated as temperatu**r**e dependent p**r**ope**r**ties.**

**Five cases were modeled. The c**r**ystal pe**r**fo**r**mance w**a**s simulated fo**r **posit**r**on c**ur**rents of 100, 200, and 300 mA.** In **addi**ti**on, the effect of doubling the heat tra**ns**fe**r coefficient to 10 W/cm<sup>2</sup> °C for the 300 mA case was investigated. The effect of doubling the crystal thickness to 20 mm at 300 mA was also modeled. For the structural analysis,

a **symm**e**try bo**un**d**ar**y co**n**d**i**t**i**o**n **was im**p**osed** on t**he c**entral plan**e,** an**d th**e **ce**n**tr**al no**de under** th**e peak heat flux w**a**s held fixed. The rest of the crystal was unconstrained.**

#### **III. RESULTS AND DISCUSSION**

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**A contou**r **plot of** th**e temperature profile for the 300 mA case is shown in F**i**g.** 1**. The minimum temperature is about 81 K. Note that the heat is** di**ffusing quite readily throughout the en**ti**re crystal. Because** th**e thermal conductivity is so la**r**ge, the coola**n**t can be placed much further from the heated surface than for a** r**oom-tempe**r**a**tu**re crystal. Therefore, th**e **peak local heat flux at the fluid interface is much reduced allevia**tin**g the p**r**oblem of boiling and cri**ti**cal heat flux. The s**ur**face tempe**r**atures** a**long** the central axis of the crystal for the 100, 200, and 300 mA cases are shown in Fig. 2. The **peak temperat**ur**es ar**e **88.2, 102.6, and 121.4 K, respectively. The temperature** di**fference** on the surface across the beam footprint in the beam direction was about 1.5, 4.0 and 8.0 **K,** r**espectively. The peak temperature i**n**creases nonlinearly as the curre**n**t is increased because the the**r**mal conductivity is decreasing.** H**owever, it should be reme**m**bered** th**at the expansi**o**n coefficient app**r**oaches zero as** th**e tempe**r**a**tu**re nears about 125 K.** The effect of doubling the heat transfer coefficient to 10 W/cm<sup>2</sup>  $\degree$ C and the effect of **doub**li**ng** th**e crystal thickness to 20 mm for** th**e 300 mA case are show**n **i**n **Fig. 3. Doubling** t**he thickness caused the p**e**ak tempe**r**ature to** in**crease by about 4 K. T**hi**s is a relatively small amount** in**dicating** th**at the coolant can be placed rela**ti**vely distant from** th**e diffraction surface wi**th**out paying a h**i**gh penalty in tempera**tu**re incre**a**se. The added** t**hic**kn**ess allows** th**e heat to** di**ffuse mo**r**e, the**r**eby, dec**r**easing** t**he** in**terfac**i**al heat flux.** Th**e added thickness also allows a large**r **coolant p**r**essure to be used w**i**thout caus**in**g pressure related s**tr**ain at the** di**ff**r**ac**ti**on surface. Doubli**n**g the heat tra**ns**fer coefficient caused the pe**a**k temperature to decrease by about 8 K. Th**i**s** r**esult ind**i**cates** that much can still be gained by increasing the heat transfer coefficient. Because the Si **conduc**ti**vity is so large, the heat tra**ns**fe**r **is convection limited.**

**Th**e s**lo**pe an**d** di**sp**la**cem**ent of t**he d**iffra**c**tion plane**s a**l**on**g th**e ce**ntral axi**s** of the **c**rystal at **1**00, 200, and 300 **mA** ar**e** shown in Figs. 4, 5, and 6*,* respe**c**tiv**e**ly. The variation in Bragg angle is given by

*i*

$$
\Delta\theta_B = slope + \frac{\Delta d}{d}tan\theta_B << \Delta\theta_0
$$

**where** *slope* **is** th**e thermal slope error,** *d* **is the spaci**n**g between the crystalline planes***,* and  $\Delta\theta_0$  is the Darwin width of the crystal. This equation shows that the total variation **in** th**e B**r**agg a**n**gle must be much less than the int**r**i**n**sic** r**eflection width. The peak slopes under the footprint of** th**e beam were -1.**17**, -2.35, and 0.33** \_tr**ad for th**e**se cases. The varia**ti**on** in **B**ra**gg angle due to change** in **d-spac**in**g was -0.4, -0.8, and -0.9** \_r**ad, respectively. At 100 and 200 mA, the surface normal displacement was found to be concave due to the negative the**r**mal expansion coefficient below about 125 K** r**esul**t**ing in a** "**thermal dimple**"**. At 300 mA, a small** "th**ermal bump**" **was prese**n**t at the hottest pa**r**t of** th**e beam footpr**in**t superimposed on** a**n overall** "**the**rm**al dimple**"**. In this** r**egion,** th**e** th**e**r**mal expansion coefficient is beginning to become positive. The exact temperatu**r**e where the expansion coefficie**n**t zero crossing occurs was about 120 K due** to interpolation. This leads to the interesting result that the slope error at 300 mA is less **than that at 100 or 200 mA. This phenomenon in p**r**inciple allows one to match the inclina**ti**on angle to the partic**ul**ar experimental si**tu**ation so as to cause the peak** t**empe**r**a**tur**e to be around 125 K** r**esult**in**g** in **minimal distortion of the** di**ffraction pla**n**es. Fo**r **the analysis in question, if one is operating at 100 mA, on**l**y abou**t **1***/***3 of the** spreading of the 85° case is required, i.e., an inclination angle of approximately 75°. This **would allow fo**r **smaller crystals and easier** a**lignment due to** th**e large**r **incide**n**ce angle. The thermal er**r**or of the Bragg angle was much less** t**han the Darwin width for all of** t**he c**a**s**es**.**

#### **IV. SUMMARY**

**It h**a**s been shown that** an **inclined, cryogenically cooled, Si monochromator ca**n **handle the AI**\_ **Undulator A beam with** m**inimal disto**r**tion up to a positron cur**r**ent of 300 m**A**. The iriclination angle can be tailored so that, fo**r **a given set of** m**achi**n**e pa**r**ameters,** th**e c**r**ystal performance is optimized. In distinc**ti**on to room-tempe**r**ature crystals, cryogenic crystals are not limited in their heat transfer** pe**rformance by the material p**r**operties. The primary limiting factor fo**r li**quid-nitrogen cooled crystals is** th**e rela**ti**vely low heat flux requi**r**ed for o**ns**e**t **of nucleate boiling and critical heat flux. The dominant resis**t**ance to heat flow is convection resistance. This indicates that continued improvement in performance can be atta**in**ed by applying va**r**ious enhancement techniques, such as, porous media.**

#### **ACKNOWLEDGMENTS**

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# **FIGURE CAPTIONS**

FIG. 1. Temperature contour plot of inclined crystal for Undulator A at 300 mA, crystal **thickness, t**=**10 mm, heat** tr**a**ns**fer coefficie**n**t, h=5 W***/***cm 2** "**C.**

**FIG**. **2**. **Surface tempe**r**at**u**re profi**l**e** al**on**g **centra**l a**xis of cry**s**ta**l (**see F**i**g**. **1**) **fo**r **Undulator A at 100, 200***,* **and 300 mA.**

**FIG. 3. Compa**r**ison of surface temperature profile along central axis of crystal at 300 mA when thick**n**ess is inc**r**eased to 20 mm and when heat transfe**r **coefficient is increased** to  $10 \text{ W/cm}^2$   $^{\circ}$ C.

**FIG. 4. Displacement and slope of diffraction plane along cent**r**al axis of inclined crys**t**al** for 100 mA current, crystal thickness, t=10 mm, heat transfer coefficient, h=5 W/cm<sup>2</sup> °C.

FIG. 5. Displacement and slope of diffraction plane along central axis of inclined crystal for 200 mA current, crystal thickness, t=10 mm, heat transfer coefficient, h=5 W/cm<sup>2</sup> °C.

**FIG**. **6**. D**ispl**a**cement** a**nd sl**o**pe of** dif**frac**ti**o**n **plane** a**long central** axi**s of inc**lin**ed** cry**stal** for 300 mA current, crystal thickness, t=10 mm, heat transfer coefficient, h=5 W/cm<sup>2</sup> °C.

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