

TECHNISCHE UNIVERSITÄT BERGAKADEMIE FREIBERG Die Ressourcenuniversität. Seit 1765.

Stephan Dempe Bilevel optimization: theory, algorithms and applications

PREPRINT 2018-11

Fakultät für Mathematik und Informatik

Stephan Dempe

Bilevel optimization: theory, algorithms and applications

TU Bergakademie Freiberg Fakultät für Mathematik und Informatik Prüferstraße 9 09599 FREIBERG http://tu-freiberg.de/fakult1

ISSN 1433 – 9307Herausgeber:Dekan der Fakultät für Mathematik und InformatikHerstellung:Medienzentrum der TU Bergakademie Freiberg

BILEVEL OPTIMIZATION: THEORY, ALGORITHMS AND APPLICATIONS

STEPHAN DEMPE

ABSTRACT. Bilevel optimization problems are hierarchical optimization problems where the feasible region of the so-called upper level problem is restricted by the graph of the solution set mapping of the lower level problem. Aim of this article is to collect a large number of references on this topic, to show the diversity of contributions and to support young colleagues who try to start research in this challenging and interesting field.

1. INTRODUCTION

Bilevel optimization problems are hierarchical optimization problems of two or more players. For defining them consider first a parametric optimization problem

(1.1)
$$\min_{y} \{ f(x,y) : g(x,y) \le 0, \ y \in Y \},$$

where $f, g_i : \mathbb{R}^m \times \mathbb{R}^n \to \mathbb{R}, i = 1, \dots, p$ and $Y \subseteq \mathbb{R}^n$ is a nonempty, closed set. Here, equality constraints can be added if the regularity conditions are adapted accordingly. This is the problem of the lower level decision maker, sometimes called the follower's problem. If problems with more than one decision maker in the lower level are considered, e.g. a Nash equilibrium is searched for between them. Let

(1.2)
$$\varphi(x) := \min_{y} \{ f(x, y) : g(x, y) \le 0, \ y \in Y \}$$

denote the optimal value function of problem (1.1) and

(1.3)
$$\Psi(x) := \{ y \in Y : g(x, y) \le 0, \ f(x, y) \le \varphi(x) \}$$

the solution set mapping of problem (1.1). If $\mathbf{gph}\Psi := \{(x, y) : y \in \Psi(y)\}$ is used to abbreviate the graph of the solution set mapping Ψ , the bilevel optimization problem

(1.4)
$$\min \{F(x,y) : G(x) \le 0, (x,y) \in \mathbf{gph}\Psi, x \in X\}$$

can be formulated with $X \subseteq \mathbb{R}^m$, $F : \mathbb{R}^m \times \mathbb{R}^n \to \mathbb{R}$, $G_j : \mathbb{R}^m \to \mathbb{R}$, $j = 1, \ldots, q$. Sometimes, this problem is called the upper level optimization problem or the problem of the leader. Here we used quotation marks to indicate that this problem is not well-defined in case of multiple lower level optimal solutions.

Date: August 10, 2018.

Key words and phrases. Bilevel Optimization; Mathematical Programs with Complementarity Constraints; Optimality conditions; Applications; Necessary optimality conditions; Solution algorithms; Metaheuristics; Optimistic and pessimistic bilevel optimization problems.

The author's work has been supported by Deutsche Forschungsgemeinschaft, Projects GZ DE650/7 and DE650/10.

2. HISTORY

Problem (1.1), (1.4) has first be formulated in an economic context by v. Stackelberg [1124]. Many economic articles investigate related principal-agency problems, see some references below. Hence, it is called sometimes Stackelberg game and the solution a Stackelberg equilibrium. About 40 years later, this problem has been introduced into the mathematical community [180, 240, 239, 475, 685, 881]. Since then a large number of articles illustrating different views on the topic, investigating various questions both from theoretical or numerical side or numerous applications of the problem appeared. It is our aim here to give the reader some insight into the topic and its investigations. Without any doubt, this bibliography cannot be complete.

Bilevel optimization problems are nonconvex and nondifferentiable optimization problems, see [290].

3. Overviews and introductions

Well formulated introductory texts on bilevel optimization can be found in [60, 275, 300, 586, 680, 704, 1188]. Sinha et al. [1100] give an overview over evolutionary methods. Pozo et al. [977] compare Nash, Cournot, Bertrand and Stackelberg games, describe ideas for solving them as well as some applications, see also [149, 1278]. An overview over the investigations at the Montreal school in the years before 2008 is given in [190]. An overview over solution algorithms for (mixed-integer) linear bilevel optimization problems can be found in [1026], and for general bilevel optimization problems in [969].

Monographs, textbooks and edited volumes on the topic are Bard [117], Dempe [345], Dempe et al. [373], Kalashnikov et al. [643], Mesanovic et al. [855], Sakawa [1029], Sakawa and Nishizaki [1034], Shimizu et al. [1080], Stein [1128], Talbi [1149], Zhang et al. [1323]. Bilevel optimization problems are the topic of a chapter in the monograph [433].

Bilevel optimization problems with many followers and the three-level optimization problem have been investigated in [57, 37, 548, 549, 550, 552, 796, 791, 931]. A comment to [57] can be found in [1106].

We have used constraints in the upper level problem of the form $G(x) \leq 0$. Sometimes upper level constraints of the form $G(x, y) \leq 0$, so-called joint constraints, are investigated. These problems are not easy to interpret in a game theoretic context since then, the leader has to select first his / her decision and gives it to the follower. The latter then computes one optimal reply on the leader's choice and gives it back to the leader, who only now is able to check if his / her initial selection was a feasible one. If the follower's selection was not unique, feasibility of the leader's selection also depends on the response of the follower. This was the motivation of the authors in [1071] to suggest to move joint upper level constraints into the lower level to derive a "correct" definition. This approach is shown to be not correct in [90, 852] since it changes the problem seriously. Joint constraints can make the feasible set of the bilevel optimization problem empty even if $\Psi(x) \neq \emptyset$ for all $x \in X$, or disconnected even if **gph** Ψ is connected, see [852].

The three-level problem is investigated in [112, 322, 469]. The articles [114, 139, 1015] explain the geometry of bilevel and multilevel optimization problems. A global optimal solution of multilevel optimization problems is approximated in [659]. In [469], three different types of optimistic formulations of three-level optimization

problems are suggested and compared. The electrical network defense is formulated as a three-level mixed-integer linear programming model [1279].

Examples showing nonexistence of optimal solutions can be found in [116]. Survey papers are [131, 299, 344, 347, 641, 646, 787, 393, 834, 835, 860, 1233]. First bibliographies can be found in [346, 1189, 1208].

The formulation of problems with an infinite number of lower level decision makers as a stochastic bilevel optimization problem is given in [797].

4. Theoretical properties and relations to other optimization problems

4.1. Formulation of the bilevel optimization problem.

4.1.1. Optimistic vs. pessimistic formulation. The formulation of the bilevel optimization problem as given in (1.1), (1.4) is not clear in case of multiple lower level optimal solutions for some of the selections of the upper level decision maker. In that case, the leader may assume that the follower can be motivated to select a best optimal solution in $\Psi(x)$ with respect to the leader's objective function. This is the so-called optimistic or weak formulation of the bilevel optimization problem, investigated in most of the references:

$$\min\{\varphi_o(x): G(x) \le 0, \ x \in X\},\$$

where

(4.1)
$$\varphi_o(x) = \min_y \{F(x,y) : y \in \Psi(x)\}.$$

This problem is almost equivalent to

(4.2)
$$\min_{x,y} \{ F(x,y) : G(x) \le 0, \ x \in X, \ (x,y) \in \mathbf{gph}\Psi \},$$

see [345]. If the upper level objective function is of a special type the optimistic bilevel optimization problem can be interpreted as an inverse optimization problem [22, 607, 1333].

Relations to generalized semi-infinite optimization problems [1130]

If this is not possible or even not allowed the leader is forced to bound the damage resulting from an unwelcome selection of the follower resulting in the pessimistic or strong formulation of the bilevel optimization problem:

(4.3)
$$\min\{\varphi_p(x): G(x) \le 0, \ x \in X\},\$$

where

(4.4)
$$\varphi_p(x) = \min_y \{F(x,y) : y \in \Psi(x)\}.$$

The formulation of the pessimistic Stackelberg game is given in [721, 886]. The existence of a pessimistic (strong) or an optimistic (weak) optimal solution is considered in [4, 13, 14, 795], the same based on d.c. optimization is investigated in [7]. For the existence and stability of pessimistic solutions in general spaces, the reader is referred to [741, 742, 743, 744, 746, 745, 748]. Topic of the article [960] is the existence of solutions in Banach spaces if the solution of the lower level problem is strongly stable. The possible nonexistence of pessimistic optimal solutions is shown in [795].

In [1243], the pessimistic bilevel optimization problem with an objective function not depending on the lower level variable is formulated as

(4.5)
$$\min\{F(x) : x \in X, \ G(x,y) \le 0 \ \forall \ y \in \Psi(x)\}.$$

The relations between this formulation and pessimistic bilevel optimization as given in (4.3) are investigated in [1243].

4.1.2. Optimization over the efficient set. The search for a "best" efficient solution of a multicriterial optimization problem is formulated as a bilevel optimization problem [141, 168, 426, 584, 585, 629, 892, 893, 1120, 1159, 1161, 1173].

Properties of the problem and replacement of the upper level objective function $\langle d, x \rangle$ by a constraint $\langle d, x \rangle \geq t$ for unknown t in the lower level problem [140].

A special model is the simple bilevel optimization problem in [352], where a "best" solution of an optimization problem is searched for. Optimality conditions for that problem can be found in [352], a solution algorithm is given in [1019, 1114, 1115]. In [667, 750], a "best" solution in the set of Pareto optimal solutions of a multicriterial optimization problem is searched for.

Stochastic problems of this type are topic of [167].

4.1.3. Semivectorial bilevel optimization – vector-valued lower level problems and problems with multiobjective upper level problems. Bilevel optimization problems where the lower level problem is a multiobjective optimization problem are often called semivectorial bilevel optimization problems [33, 77, 166, 169, 171, 225, 369, 486, 909, 991, 806].

Using the scalarization approach and indicator functions as terms in the upper level objective function the semivectorial bilevel optimization problem is transformed into a single-level one for which the nonsmooth Mangasarian-Fromovitz constraint qualification can be satisfied, see [487].

Use of utility functions as well as optimistic and pessimistic approaches to investigate linear bilevel problems with multiobjective functions in both the leader's and the follower's problems [913], the same in case of stochastic data [915]

Multiobjective optimization in the upper level of a linear bilevel optimization problem [807, 792], application of fuzzy optimization in this case [174]. Problems with multiobjective upper level problems are investigated in [1287] using a combination of the KKT and the optimal value approach.

Optimality conditions for nonlinear bilevel vector optimization problems and a global solver can be found in [501]

4.1.4. *Fuzzy bilevel optimization problems*. The investigation of bilevel optimization problems with fuzzy lower level problems can be found in [390, 596, 757, 1322, 1318, 1318].

The fuzzy linear bilevel optimization problem is transformed into a crisp problem and then solved using a k-th best algorithm in [988, 1030, 1031, 1319] or transformed using the KKT approach [1314, 1317]. Solving this problem using an interactive approach has been the topic of [994, 1031]. Solution algorithm for fuzzy bilevel optimization problems using α -cuts is given in [195, 493, 495]. For an interactive solution approach see [1035, 1037, 1039, 1038].

Computation of a satisfactory solution [707, 978, 979, 1011, 1043]. Here, in some sense, an approach is used which is related to multiobjective optimization, see remarks in [348]. The transformation of a bilevel optimization problem using

ideas from fuzzy optimization into the problem of maximizing membership functions related to both the objective functions of the leader's and the follower's problem at the same time is not a possible approach for solving the bilevel optimization problem, see [348].

Applications of fuzzy (random) bilevel optimization

- (1) in the Shuibuya hydropower project [1257],
- (2) in logistics planning [636],
- (3) in water exchange in eco-industrial parks [99].

4.1.5. *Stochastic problems.* The model and solution algorithms can be found in [38, 251, 284, 372, 327, 489, 580, 606, 650, 686, 794, 944, 946, 947, 971]. Stochastic bilevel multi-leader multi-follower problems are investigated in [328, 1256]. In [328] the authors show uniqueness of the stochastic multi-leader Stackelberg-Nash-Cournot equilibrium and suggest an algorithm for computing it.

4.1.6. Bilevel optimization problems with fixed-point constraints. Existence theorems for bilevel optimization problems with fixed-point constraints are the topic of [754]. Special cases are MPECs and semi-infinite optimization problems.

Robust polynomial bilevel optimization problems are investigated in [286]. Robust Stackelberg problems are the topic of [768].

4.1.7. *Bilevel equilibrium problems.* In 2010 A. Moudafi formulated a bilevel equilibrium problem [889] which has been the topic of investigations of many articles since then, see e.g. [1185]. This problem is an hierarchical problem where both the upper and the lower level problems are formulated as variational inequalities. As in bilevel optimization, the solution of the upper level problem is a parameter of the lower level problem and the solution of the lower level problem is used to formulate the constraint in the upper level one.

4.2. Dependence on data perturbations. The dependence of optimal solutions of bilevel optimization problems on data perturbations has been investigated by some authors, see e.g. [12, 1216]. [11] replaces the lower level problem using ε -optimal solutions and considers convergence of the solutions for $\varepsilon \downarrow 0$. Stability considerations can be found in [359, 463, 616, 741, 742, 743, 744, 819], the same using the transformation by an inclusion constraint is given in [406, 407].

A surprising fact is that, global optimal solutions of the bilevel optimization problem need not to remain globally optimal if a constraint is added to the lower level problem which is inactice at the optimal solution [381, 811].

The structure of the feasible set of bilevel optimization problems has been the topic of [628, 371, 414], see also [1305]. Generic properties of an optimal solution of the bilevel problem if the lower level problem is replaced using the F.-John conditions can be found in [40], see [362] with a comment to that approach.

Optimal value range problem for bilevel problems with interval coefficients is investigated in [220]. Bilevel linear programming problem with interval coefficients have also been considered in [990, 995].

An important result related to this is well-posedness of the problems, see [69].

4.3. **Possible transformations.** To investigate properties, for the formulation of optimality conditions and solution algorithms, the bilevel optimization problem needs to be transformed into a single level problem. For this, different approaches are possible.

4.3.1. Use of the Karush-Kuhn-Tucker conditions of the lower level problem. If the functions $y \mapsto f(x, y), y \mapsto g_i(x, y), i = 1, ..., p$, are differentiable and a regularity condition is satisfied for the lower level problem for all $(x, y) \in \mathbf{gph}\Psi$, problem (4.2) can be replaced by

(4.6)
$$\min_{x,y,u} \{ F(x,y) : G(x) \le 0, \ x \in X, \\ \nabla_y \{ f(x,y) + u^\top g(x,y) \} = 0, \\ u \ge 0, \ g(x,y) \le 0, \ u^\top g(x,y) = 0 \}.$$

It is shown in [867] that this approach is only possible if the lower level problem is a convex one. Problem (4.6) is a so-called mathematical program with equilibrium (or complementarity) constraints (MPEC), see [799]. This problem is a nonconvex optimization problem for which the Mangasarian-Fromovitz constraint qualification is violated at every feasible point [1050]. The relations between problems (4.2) and (4.6) have been investigated in [353]. This transformation is the most often used one, MPECs have been intensively been investigated. In [92, 475, 485] the complementarity constraint in the Karush-Kuhn-Tucker transformation (4.6) are replaced using Boolean variables.

Relations between the KKT and the optimal value transformations as well as between the KKT transformation and the original bilevel optimization problem [353], relations between global optimal solutions of the bilevel optimization problem and its KKT transformation formulated as a mixed Boolean optimization problem [1127]. Combination of the KKT and the optimal value approaches [965, 1289]. The problem (4.6) does not satisfy MPEC-LICQ in general even if the lower level problem satisfies LICQ and the sufficient optimality condition of second order [559].

4.3.2. Use of necessary optimality conditions without Lagrange multipliers. Let, for $x \in X$,

$$M(x) := \{ y : g(x, y) \le 0 \}$$

denote the feaible set of the lower level problem and assume that $y \mapsto f(x, y)$ is a convex function and, for arbitrary, fixed $x \in X$, $M(x) \subseteq \mathbb{R}^m$ is a convex set. Then, $y \in \Psi(x)$ if and only if $0 \in \partial_y f(x, y) + N_{M(x)}(y)$. Thus, (4.2) can be replaced by

(4.7)
$$\min\{F(x,y): G(x) \le 0, \ x \in X, \ 0 \in \partial_y f(x,y) + N_{M(x)}(y)\}$$

where $N_A(z) = \{d : d^{\top}(w-z) \leq 0\}$ denotes the normal cone in the sense of convex analysis to a closed set A and it is assumed that $N_A(z) = \emptyset$ if $z \notin A$. Problem (4.7) is fully equivalent to (4.2). Problem (4.7) is also called an optimization problem with a generalized equation or with a variational inequality, it has been studied in [393, 882, 883, 885, 1288].

4.3.3. Use of the optimal value function. Problem (4.2) can be equivalently replaced by

(4.8)
$$\min\{F(x,y): G(x) \le 0, x \in X, g(x,y) \le 0, f(x,y) \le \varphi(x)\}.$$

This transformation has first been used in [932, 933]. Problem (4.8) is a nonsmooth optimization problem since the optimal value function $\varphi(x)$ is, even under restrictive assumptions, in general not differentiable. Moreover, the nonsmooth Mangasarian-Fromovitz constraint qualification is violated at every feasible point, see [964, 1291].

4.3.4. Transformation using a variational inequality. If the definition of the normal cone is used, problem (4.7) is

(4.9)
$$\min\{F(x,y): G(x) \le 0, \ x \in X, \ y \in M(x), \\ \langle \nabla_y f(x,y), z - y \rangle \ge 0 \ \forall \ z \in M(y)\},$$

where the problem

find min $y \in M(x)$ such that $\langle \nabla_y f(x,y), z-y \rangle \ge 0 \ \forall z \in M(x)$

is often called a generalized variational inequality. Here, f is assumed to be differentiable, see [1293]

Bilevel variational inequalities have been intoduced in [647, 1197].

The existence of solutions for bilevel variational inequalities is topic in [746]. Investigation of bilevel variational inequalities under invexity assumptions [263] Application of bilevel optimization to solve fuzzy variational inequalities [453]. Solution algorithm for bilevel VI [145, 730].

4.3.5. Formulation as a set-valued optimization problem. Using

$$\mathcal{F}(x) := \bigcup_{y \in \Psi(x)} F(x, y),$$

problem (4.2) can be replaced with

(4.10)
$$\min^{n} \{ \mathcal{F}(x) : G(x) \le 0, x \in X \}.$$

This formulation has been the topic of [386, 966]. For this approach, the notion of an optimal solution needs to be defined first.

4.4. General properties. Optimal solutions of certain bilevel optimization problems can be found at vertices of the feasible set [114, 155, 207, 208, 221, 209, 216, 769, 844, 843].

Since the bilevel optimization problem can be interpreted as a hierarchical game it interesting to ask if it is beneficial to act as leader? [48, 635, 638, 1167, 1306]

Optimal solutions of the bilevel optimization problem are in general not Pareto optimal if optimization is done w.r.t. the objective functions of both levels at the same time [1113, 348]. The relationship between the bilevel problem and bicriterial optimization is illustrated in [237, 832, 859, 1232]. The correct formulation of multicriterial optimization problems which are equivalent to the bilevel problem can be found in [468, 484, 605, 962, 1016]. An application of these results to solve linear bilevel optimization problems is given in [511].

In [1239, 1234, 1235], a possible transformation of an optimal solution of the bilevel optimization problem into a Pareto optimal solution is investigated.

For problems with multiple followers see [626, 1315], problems with multiple leaders have been investigated in [327, 1065]. Nine different kinds of relationships between followers in bilevel optimization problems with multiple followers can be found in [788]. For a variational inequality formulation of problems with multiple leaders we refer to [588].

Phenomena of inverse Stackelberg problems are described in [924, 923].

 \mathcal{NP} -hardness of bilevel optimization problems has been shown in [116, 163, 397, 611]. Relations to mixed-integer optimization problems are topic of [476]. Investigation of a special problem which is polynomially solvable can be found in [676, 677, 974].

Computational complexity of the bilevel knapsack problems are the tipic of [244].

4.5. Problems in infinite dimensional spaces. Bilevel optimization problems in general spaces are considered in [408, 682, 845, 846].

Semivectorial bilevel optimization on Riemannian manifolds [172]. Existence of Stackelberg equilibrium points on strategy sets which are geodesic convex in certain Riemannian manifolds [690].

Use of KKT transformation to the bilevel optimization problem in infinite dimensional spaces [845].

Optimal value transformation, regularity conditions and optimality conditions [1285]

Necessary optimality conditions in form of M stationarity condition for problems with second order cone programming problems in the lower level can be found in [274, 1332].

The existence of solutions has been investigated in [745, 753].

Stackelberg games go back to the original definition by H.v. Stackelberg [1124] and refer to problems where the feasible set of the lower level does not depend on the upper level variable. Recent related problems are

- (1) Closed-loop Stackelberg games [664, 876, 1085, 1166],
- (2) Dynamic Stackelberg problems [862, 874, 910, 911],
- (3) Reverse Stackelberg problems [527, 528, 529, 530, 532, 531]: computation of optimal incentive functions resulting in realization of the leader's aim by the follower,
- (4) Stackelberg differential games [935]
- (5) Stackelberg equilibria in an oligopoly are considered in [124].

An application of Stackelberg games to optimal control problems can be found in [887].

Bilevel optimal control problems are a new area of research. Here, two optimal control problems are combined in a hierarchical sense. Such problems have been considered in [143, 135, 136, 673, 848].

Two-level hierarchical control systems are considered in [682].

4.6. Discrete bilevel optimization problems. General introduction into those problems [1192].

Lower level problem is a parametric knapsack problem [187, 186, 387, 981] or a matroid problem [456].

Solution algorithms for mixed-integer bilevel optimization problems are suggested in [246, 396, 413, 429, 537, 684, 880, 1025, 1236, 1265].

The watermelon algorithm proposed in [1210] is an exact algorithm solving discrete linear bilevel optimization problems using multiway disjunction cuts to remove infeasible solutions for the bilevel problem from the search space.

An efficient cutting plane algorithm can be found in [464, 465, 466].

A transformation of bilevel optimization problems with mixed-integer lower level problems into a single-level problem using minima of optimal value functions of (partial) lower level problems is suggested in [728].

Using a special penalization approach, the mixed-discrete bilevel optimization problem can be transformed into a continuous one. Assuming partial calmness, optimality conditions for both the optimistic and the pessimistic problems are derived in [378]. Solution of Boolean bilevel optimization problems using the optimal value reformulation and a cutting plane algorithm [377], a related article is [786].

Exact solution of bilevel assignment problem [128], special cases of this \mathcal{NP} -hard problem can be solved in polynomial time.

Nonlinear integer bilevel optimization problems [413, 610].

Interactive approach to integer bilevel optimization problems [438].

An extended version of the kth best algorithm can be found in [1068, 1067].

Mixture of cutting plane and k-th best algorithm for integer fractional bilevel optimization problems [1160], see also [173]. Cutting plane algorithm for special discrete bilevel optimization problem [571].

Complexity of a bilevel perfect matching problem is the topic of [500], for the bilevel minimum spanning tree problem see [248, 249].

Optimality conditions for problems with discrete parametric lower level problems using the radial subdifferential [454] or in case of a parametric matroid problem in the lower level [456].

5. Optimality conditions

5.1. Strongly stable lower level optimal solution. For necessary optimality conditions and solution algorithms using strongly stationary solutions in the lower level problem see [330, 331, 334, 335, 333, 342, 341, 761, 933, 934]. Necessary optimality conditions using implicit function theorem and variational analysis can be found in [1305]. Here the author verifies that the posed necessary optimality conditions are generically satisfied at local minima of smooth bilevel optimization problems and that partial calmness is often violated. [577] describe an idea to formulate necessary (and sufficient) optimality conditions after deleting some inequality constraints in (4.6).

5.2. Use of the KKT transformation. Necessary optimality conditions using the KKT transformation [392, 394, 1215] and using a generalized equation [16, 392].

Transformation using the F.-John conditions applied to the lower level problem in place of the KKT conditions [40], see also [362] for an example with a nonconvex lower level problem where the global optimum cannot be computed with this approach.

An penalty function algorithm for problems with quadratic lower level problems can be found it [816]

Using Boolean variables the resulting mathematical program with complementarity constraints is transformed into a mixed integer optimization problem in [92], bounds for the necessary large constants can be found in [403].

5.3. Transformation using the optimal value function. Necessary and sufficient optimality conditions based on Fenchel-Lagrange duality is investigated in [5].

Optimality conditions using variational analysis for the pessimistic problem is investigated in [385].

The generalized derivative of the optimal value function of the lower level problem, violation of the MFCQ, and necessary optimality conditions can be found in [267].

Optimality conditions using the optimal value transformation for the optimistic bilevel optimization problem are derived in [354, 355, 356, 423, 384, 391, 761, 884,

1291, 1294]. In the case when the lower level problem is an optimal control problem: [1281, 1283]. For optimality conditions for infinite and semi-infinite bilevel optimization problems, see [410].

Dempe and Gadhi [365, 368] apply the optimal value transformation to a problem with multiobjective upper level problem to derive necessary optimality conditions, see also [434].

Use of generalized derivatives for point-to-set mappings for deriving necessary optimality conditions [1336, 1337]

Calmness properties of the transformed problem can be found in [575], see also [932].

The optimal value transformation is used to find relations between Stackelberg and Nash equilibria in [708]. A related algorithm solving bilevel optimization problems where the lower level problem is fully convex with a parameter independent feasible set is suggested in [709].

5.4. Set-valued optimization approach. Optimality conditions using set-valued optimization [386, 1309].

5.5. Transformation into a semi-infinite optimization problem. Optimality conditions using a semi-infinite transformation of the bilevel optimization problem can be found in [113]. A counterexample to this result is given in [287].

5.6. Optimality conditions for semivectorial bilevel problems. Optimality conditions for the pessimistic semivectorial bilevel optimization problem using variational analysis and the transformation using the optimal value function of the lower level problem can be found in [760].

5.7. Optimality conditions for the simple bilevel optimization problem. Optimality conditions for a simple bilevel optimization problem [25, 352].

5.8. Other approaches. Convexificators are used in [101, 364, 1145].

The extremal principle is used for describing necessary optimality conditions in [125, 367]. For problems with set-valued optimization problems in both levels, optimality conditions using the variational principle can be found in [370].

Different optimality conditions and transformations [375]

Necessary and sufficient optimality conditions using a linearization of the inducible region [261] and by using a description of the tangent cone to the feasible set [1190].

Input optimization is used in [1169].

Necessary and sufficient optimality conditions under generalized invexity assumptions [177].

5.9. Second-order optimality conditions. Second order necessary and sufficient optimality conditions for the optimistic bilevel optimization problem are obtained in [366].

Necessary conditions for a global optimal solution using a bilevel Farkas lemma can be found in [614].

6. Solution Algorithms

6.1. **Pessimistic problem.** A. Aboussoror and A. Mansouri [15] penalize the duality gap of the linear lower level problem in the upper level objective function to solve the pessimistic bilevel optimization problem. Some incorrectness in this article is found and corrected in [1342]. Properties, existence and stability of the pessimistic bilevel problem are investigated in [383, 694, 776, 779, 778, 780, 777, 781, 782, 783, 784, 785].

An algorithm for solving the pessimistic bilevel optimization problem using a regularization approach can be found in [148]. For using an entropy approach see [1356].

Partial cooperation between the leader and the follower (i.e. weighted sum of the optimistic and the pessimistic approaches) for linear bilevel optimization problems is the topic of [242, 1347].

Use of ε -optimal solutions in the lower level problem, convergence to a pessimistic solution for $\varepsilon \downarrow 0$ [818].

The pessimistic linear bilevel optimization problem with multiple followers is solved using a penalization of the duality gap in [1355]. Here, the different followers share some of the resources.

For use of k-th best algorithm to solve the pessimistic linear bilevel problem see [1342].

6.2. Optimistic problem.

6.2.1. *Enumeration*. Enumeration of the basic matrices of the lower level problem in linear bilevel optimization [241, 898]. Using this idea it is shown in [770] that the algorithm is of polynomial time if the number of variables in the lower level problem is fixed.

Vertex enumeration plus descent algorithm [547]. Convergence to a local optimum for linear bilevel optimization problems by investigating adjacent extreme points [155, 157, 329], using a simplex algorithm applied to an exactly penalized problem [235]. A descent algorithm computing a local optimal solution for linearquadratic bilevel optimization problems can be found in [1137, 1140].

The k-th best algorithm has originally be published in [1229], see also [213, 1343]. The same algorithm for bilevel problems with partially shared variables between followers is given in [1072]. Application of the kth best algorithm to three-level optimization problems [548, 1324]. Properties and an algorithm for linear bilevel optimization problems [1013, 1014].

Solution package Pyomo for solving the optimistic bilevel optimization problem is described in [558].

6.2.2. Use of KKT transformation. Solution algorithms using the Karush-Kuhn-Tucker transformation can be found in [108, 109, 111, 115, 118, 631, 632, 633, 789]. Solving the KKT transformation using branch-and-bound [119, 475]. Application of Gomory-like cuts in a branch-and-cut algorithm solving the KKT transformation of the bilevel problem [94].

Solution algorithm for the problem (4.6) after replacing the complementarity constraint using Boolean variables can be found in [93, 556].

Branch-and-bound algorithm [157, 441, 428, 556], branch-and-bound algorithm for problems with multiple followers [790].

Penalization of the duality gap for bilevel problems with linear lower level problem [62, 211, 231, 232, 804, 1241, 1267, 1350, 1348, 1349], for nonlinear problems see [838].

E. Aiyoshi and K. Shimizu [23, 24, 1240] apply a penalty function to the lower level problem to derive an unconstrained optimization problem which can be replaced by its gradient. Similar ideas for problems with connecting upper level constraints [598, 850].

Penalization of the complementarity constraint for linear bilevel optimization problem [926], correction in [233], see also [234, 236].

Exact penalization of the complementarity constraint under partial calmness [764].

An approximate global optimal solution is searched for in [1344].

Solve the KKT-transformation by implicit use of the inequality constraints [576].

Al-Khayyal et al. [29] use the KKT-transformation of the bilevel problem and replace the complementarity constraints by concave inequalities.

Successive approximation of the feasible set using the KKT transformation [1148].

6.3. If the lower level problem has a strongly stationary solution. Investigation of large problems is done in [681].

- (1) Interior point algorithm [723],
- (2) Trust region algorithm [762],

Comparison of different solution algorithms (Hooke-Jeeves algorithm, bilevel descent algorithm, MINOS and others) can be found in [1143].

An inexact restoration algorithm where the lower level problem is solved at each iteration [64].

Bundle algorithm for problems with strongly stationary lower level solutions [343, 344, 351] and in the case of nonunique lower level problems [388]; feasible direction method under the same assumptions [854], steepest descent algorithm [1047, 1191], use of an extragradient cutting-plane-method [409].

Solution algorithm using strong stability of the lower level optimal solution [338, 399, 449, 450].

6.4. Use of the optimal value function of the lower level problem. A cutting plane approach is applied to a reverse-convex transformation of the problem in [10, 52, 55, 894, 1174, 1175, 1176, 1177, 1178].

Solution algorithm using the optimal value function transformation [360, 362, 875, 1079].

Solution algorithm using a smooth upper approximation of the optimal value function of the lower level problem [89].

Upper approximations of the optimal value function of the lower level problem are used for solving mixed-discrete bilevel problems [870, 871].

An algorithm for the computation of an approximate global optimal solution of the optimal value transformation for bilevel optimization problems with nonconvex lower level problems and a global optimal solution for ones with convex lower level problems using semidefinite optimization is presented in [286, 613]. A smoothing SQP method for solving these problems is suggested in [1263], a smoothing augmented Lagrangian method in [1261, 1262] and a smoothing projected gradient method in [752]. If all functions describing the bilevel optimization problem are polynomials and the bilevel optimization problem is transformed equivalently into a semi-infinite optimization problem, a combination of the exchange technique with Lasserre-type semidefinite relaxations [907] can be used to solve the problem. If the constraints in the lower level problem do not depend on the leader's variables, this algorithm converges to a global optial solution [908].

6.5. Discrete problems. Benders decomposition algorithm is realized in [474].

6.6. Global optimization. Global optimization using the α BB approach [536]

A branch-and-sandwich algorithm used for globally solving the bilevel optimization problem can be found in [670, 671, 672, 949].

Global optimization of the KKT-transformation [1195].

Global optimization using sensitivity analysis in the lower level problem [446, 448, 972]

If the lower level problem is replaced by a variational inequality, an active set algorithm is suggested in [1217].

An algorithm for the computation of a global optimal solution for bilevel problems with quadratic upper and linear lower level problems can be found in [1138, 1141, 1142]. Using a transformation with d.c. constraints, the same problems can be solved globally, see [535, 581].

6.7. Metaheuristics. A genetic algorithm is applied to the certain bilevel optimization problem in [61, 222, 223, 224, 229, 490, 545, 569, 683, 731, 737, 733, 759, 840, 841, 842, 914, 1032, 1033, 1036, 1093, 1103, 1219, 1272, 1334].

A memetic algorithm is applied to solve the bilevel optimization problem in [34, 599, 601].

Ant colony systems algorithm is applied in [225].

Tabu search algorithm [502]

Particle swarm optimization [43, 489, 492, 494, 550, 551, 658, 698, 809, 1201, 1326, 1327, 1338, 1339], this algorithm for solving bilevel linear optimization problems with multiple objective functions in the upper level problem [44]. In [43] the algorithm is used to approximate the set of Pareto optimal solutions of the multiobjective, nonlinear bilevel optimization problem with linear optimization problems in the lower level problem which are solved exactly for each particle in the swarm.

Evolutionary algorithm [227, 315, 316, 317, 732, 814, 1098, 1101, 1220]

Evolutionary algorithm applied to multiobjective bilevel optimization problems using quadratic fibres to approximate the set of Pareto optimal solutions of the lower level problem [1096].

Differential evolution algorithm for problems with multiobjective upper level problem [735] and for problems with linear equality constraints [705]. The differential evolution algorithm for general bilevel optimization problems is formulated in [66, 67].

Simulated annealing [624, 952, 1027, 1247]

Estimation of distribution algorithm [1199]

Neural network algorithm [564, 589, 710, 802, 805, 1003, 1075]

A fruit fly algorithm has been developed in [812, 1205].

6.8. **Special algorithms.** Combination of the simplex algorithm with projected gradients [1132]

Direct search algorithm [853, 1311]

Solution algorithms for special problems can be found in [126, 201, 1019, 1115]. A trust-region algorithm [295, 298, 837]

Application of ideas from bicriterial optimization for solving bilevel optimization problems [1181], comment on this algorithm in [237, 1232].

Transformation into multicriterial optimization problem using certain membership functions [437]. [132, 562] show that the algorithms in [111] (Grid search algorithm) and in [158] (parametric complementary pivot algorithm) fail in general.

Application of disjunctive cuts to the KKT transformation of the bilevel optimization problem [91]

Use of fuzzy optimization to compute a satisfactory solution [84, 593, 869, 1040, 1074, 1345]

Use of derivative-free solution algorithms [301].

6.9. Integer bilevel problems. k-th best algorithm [1160], corrected results in [210]

Lower level problem is parametric integer optimization problem [255]

A cutting plane approach [340, 537, 1062], branch and bound [120], using other approaches [457].

6.10. **Related problems.** Here, only some of the algorithms are listed: [65, 75, 76] Interior point algorithms for MPECs: [142]

Problems where the upper level constraints and objective function depend on the optimal value function of the lower level problem [1079].

7. BILEVEL PROBLEMS WITH MULTIOBJECTIVE FUNCTIONS IN THE LOWER OR UPPER LEVEL, OR WITH MULTIPLE FOLLOWERS

Problems with vector-valued objective function in the upper level problem are considered in [218].

Problems with multiple followers [215, 317].

Semivectorial bilevel optimization problems, i.e. bilevel optimization problems where the lower level problem has a vector – valued objective function are topic of [369, 801, 1346].

In [1351], multiobjective (linear) problems in both levels are considered. The lower level problem is replaced using Benson's approach. The authors compute a satisfactory solution applying certain k-th best approach.

Application of Fülöp's idea [484] to problems with multiobjective linear optimization problems in both levels is realized in [963].

8. Applications

(1) Agricultural economics [238, 240], Support of biofuel production [121, 122].

- (2) Agricultural credit distribution to improve rural income [927].
- (3) Aid distribution after the occurrence of a disaster [228].
- (4) Airline revenue management [303].
- (5) Aircraft structural design [555].
- (6) Aluminium production [904, 905, 906].
- (7) Analyzation of the possible mechanisms of optimization of biodiversity [35].

- (8) Bioengineering and biotechnology [199, 959], optimization of bioprocess productivity based on metabolic-genetic network models [608], optimization of low-carbon product family and its manufacturing process [1251].
- (9) Chemical equilibria [288, 1112].
- (10) Optimizing bus-size and headway in transit networks [302, 319].
- (11) Capacity (expansion) planning [498, 469].
- (12) Contact shape optimization [576].
- (13) Control of container cranes in high rack warehouses [673]
- (14) Credit allocation [1021].
- (15) Critical infrastructure protection planning [1048].
- (16) Deception in games [729].
- (17) Defense applications [54, 181]. Interdiction problems below describe also applications related to defense problems. Electric grid defense planning [37, 1279].
- (18) Discount decisions for the retailer [660].
- (19) Dynamic storage pricing strategy in supply hub in industrial park [980].
- (20) Ecological problems: Greenhouse gas emissions [563, 579, 719, 793, 1242], water exchange in eco-industrial parks [99, 1151].
- (21) Electron tomography [1361].
- (22) Environmental policy [339, 538].
- (23) Electricity markets and networks [19, 95, 96, 97, 106, 150, 162, 451, 497, 560, 561, 578, 580, 582, 583, 591, 714, 800, 1136, 1184, 1203, 1227, 1304].
 - (a) Control of renewable energy generation [1147].
 - (b) Optimal location and size of storage devices in transmission networks [424].
 - (c) Bids of wind power producers in the day-ahead market with stochastic market clearing are investigated in [720]. Real-time pricing schemes in electricity markets [1362]. The optimal strategic bidding of energy producers is the topic of [574, 689].
 - (d) Electricity swing option pricing [687].
 - (e) Power system vulnerability analysis is modelled as bilevel optimization problem in [85].
 - (f) Pay-as-clear electricity market with demand elasticity [41].
- (24) Evacuation planning [79, 998, 1253, 1295, 1253, 1340].
- (25) Facility location and production problem [1, 147, 146, 164, 252, 400, 674, 691, 839, 863, 914, 973, 1001, 1028, 1144, 1329], facility location and freight transportation problem [311, 544], production planning problem [798]. Best location of stone industrial parks which pollute the environment [489]. Location allocation problem [817]. Existence of a Stackelberg equilibrium in a location problem is shown in [572]. Facility location problem with customer's patronization [253].
- (26) A polynomial-time algorithm for the bilevel time minimization (or bottleneck) transportation problem can be found in [1061, 1117, 1118, 1252].
- (27) Fisheries management [938].
- (28) Flow shop scheduling problems [2].
- (29) Special game problems [432], multi-leader-follower games [693, 727, 941]. Existence for equilibria in such problems is investigated in [1299].
- (30) Gas cash-out problem [374, 649, 653], entry-exit gas market [524].

- (31) Hazardous materials transportation [230, 440].
- (32) Material transportation at the Lancang River Hydropower Base [810].
- (33) Health insurance problem [1311].
- (34) Human arm movements [31, 32, 877].
- (35) Identification of enzymatic capacity constraints [1276].
- (36) Image Segmentation [985], image reconstruction [404, 1357].
- (37) Inverse optimization [418].
- (38) Local access networks (LAN) [229].
- (39) Misclassification minimization [824, 825, 826, 833].
- (40) Mechanics [940].
- (41) Profitability of merger in Stackelberg markets [594].
- (42) Problems over networks
 - (a) Highway network design [88, 130, 133, 134, 279, 514, 700, 701, 717, 827, 830, 1214, 1217]. The complexity of the highway pricing problem is the topic of [402, 566]. Network design problem with uncertain travel demand [256, 281]. Sensitivity analysis is used to solve the network design problem in [630]. The algorithm in [717] has been shown not to converge in [829]. The network design problem is also the topic in [496]. The mathematical structure of the strategic pricing problem is investigated in [836].
 - (b) O-D adjustment problem [268, 292, 415, 471, 1060, 1274], O-D demands estimation [999], optimal tolls in transportation networks [176, 178, 188, 189, 358, 361, 382, 403, 405, 421, 523, 716, 831, 389]. The same with a real application in Hong Kong [1269]. Network design problem [474, 480, 481, 482, 637, 751, 1042, 1146].
 - (c) Solution algorithms for an application in a traffic network [291] with some comments in [293].
 - (d) Traffic network signal control [553, 657, 1123, 1180, 1275]. Use of traffic flow guidance systems [1082].
 - (e) Hierarchical transportation network with transshipment facilities [306, 305]. Expansion of a highway network [68].
 - (f) An overview over pricing problems in transportation and marketing is given in [567]. Multiobjective pricing problems are considered in [1209].
 - (g) Interaction of public and private sections using the example of Korea [666]. Model for public-private partnerships [715].
 - (h) Review of related problems [858], bilevel traffic management [945]. Investigation of an approximation algorithm for the toll setting problem [523, 1007]. Different models for traffic assignment problems can be found in [774]. A comparison of algorithms for solving a bi-level toll setting problem can be found in [637].
 - (i) Public Rail Transportation under Incomplete Data is the topic of [951].
 - (j) Computational complexity of the problem is investigated and a cutting plane approach is suggested in [568].
 - (k) Pricing toll roads under uncertainty [411].
 - (1) In [890] the problem is transformed using the KKT transformation, the complementarity conditions are replaced using the Fischer-Burmeister function and the resulting problems are solved globally.

- (m) Load balancing in mobile networks [444].
- (n) Transportation of hazardous materials [46, 159, 417, 440, 654, 662].
- (o) Two-level stochastic optimization problem over transportation network [38].
- (p) Trajectory planning for a robot [849].
- (q) Location of hydrogen filling stations to promote the use of electric cars [20, 865].
- (r) Vehicle routing problem [840].
- (s) An hub arc location model is investigated in [1045].
- (t) Railway transport hub planning [663].
- (43) Interdiction problems [28, 37, 102, 105, 191, 192, 193, 194, 243, 504, 775, 902, 916, 953, 1002, 1022, 1049, 1111, 1245, 1246, 1249]. Many interdiction problems are formulated as three-level optimization problems, some of the references describe especially tailored solution algorithms. Heuristic algorithms for generalized interdiction problems where the assumption that the leader and the follower objective functions are one the opposite of the other is removed can be found in [467]. In this article the authors report also very extensive computational results.
- (44) Uncapacitated lot-sizing problem [668].
- (45) Predatory pricing in a multiperiod Stackelberg game [896].
- (46) Pipe network design [1335].
- (47) Physical layer security in cognitive radio networks [452].
- (48) Real-time path planning approach for unmanned aerial vehicles [766].
- (49) Set invariance characterization of dynamical systems affected by time-delay [712].
- (50) Stackelberg-Nash-Cournot equilibria [463, 1066, 1164, 1165, 1300]. A stochastic problem of this type is investigated in [314, 1256]. A critical comment to some of the results in [1066] can be found in [431]. Under some conditions, the Stackelberg equilibrium is also a Cournot equilibrium [635].
- (51) Modeling a subproblem if support vector machines are solved as bilevel optimization problem can be found in [695].
- (52) Machine learning problems [138, 271, 272, 696, 958], statistical learning methods [137], parameter learning in image applications [312, 919, 920].
- (53) Maximally violated valid inequality generation often has a natural interpretation as a bilevel program [772].
- (54) Network design problem with congestion effects [828].
- (55) Newsboy problem [309, 615, 1359].
- (56) New product design [1131].
- (57) Optimal incentive system [337, 1341], Principal-agent problems [257, 488, 533, 534, 612, 665, 713, 901, 986, 987, 1009, 1012, 1087, 1352].
- (58) Optimal standardization [515, 518].
- (59) Optimal nomenclature of products [516, 517].
- (60) Optimal drug combination causing minimal side effects in biomedicine [445].
- (61) Parameter estimation in chemical engineering [165, 873].
- (62) Product selection with partial exterior financing [678].
- (63) Price-based market clearing under marginal pricing [459, 460, 461].

- (64) Price setting problems [702, 703], in part related to toll setting problems in transportation networks. Price setting problems on a network [509] and on an oligopolistic market [1004].
- (65) Process design problem [288, 289].
- (66) Resource allocation problem in wireless networks [201].
- (67) Application in quantitative policy analysis: [184].
- (68) Scheduling problems [656].
- (69) Stackelberg solution in static and dynamic nonzero-sum two-player games (open-loop Stackelberg solution) [525, 1085].
- (70) Relations between central economic units and subunits: [3, 107, 110, 114, 255, 669, 722], hazardous waste management [51, 53], applications in economics [183, 197, 198, 217].
- (71) Resource allocation [255, 546, 899, 900, 1213]. Problems with resource allocation constraints lead to minimization problems over the efficient set [1157].
- (72) Supply chain configuration [222, 697, 1023, 1041, 1272], corporate social responsibility in a supply chain [49, 661], supply chain management [756, 768, 1044, 1211, 1266]. Different metaheuristics are applied to a location-allocation problem related to a supply chain problem.
- (73) Truss topology optimization [479].
- (74) Virtual power plants [655, 1313].
- (75) Water conflict problem between India and Bangladesh [58, 161], water allocation issues [592, 1258, 1260], water distribution system [1110], water rights trading [1222].

9. Test problems

Methods to generate test problems can be found for linear bilevel optimization problems in [888], for more general problems in [203, 204, 205, 206, 930, 1092], see also Chapter 9 of [472]. A bilevel optimization problem library can be found on the internet page. For another test set see [872].

10. MASTER, PHD AND HABILITATION THESIS

S. Addoune [18], G.B. Allende [39], O. Ben-Ayed [129], Bi [151], W.D. Cai [202],
L.M. Case [254], M. Červinka [1186], Y. Chen [264], B. Colson [294, 296], S.M.
Dassanayaka [310], S. Dempe [332], S. DeNegre [395], deSilva [398], J. Deuerlein
[401], S. Dewez [402], J. Eckardt [425], T. Edmunds [427], A. Ehrenmann [430], D.
Fanghänel [455], S. Franke [477], Y. Gao [491], N. Groot [526], F. Harder [557],
C. Henkel [573], X. Hu [590], E. Israeli [602], D. Joksimocic [627], F.M. Kue [692],
S. Lohse [773], P. Mehlitz [847], A.G. Mersha [851], G.M. Moore [878], J. Moore
[879], A. Nwosu [917], W. Oeder [922], F. Parraga [943], T. Petersen [954], A. G.
Petoussis [955], O. Pieume [961], M. Pilecka [964, 966], P. Pisciella [970], R. Rog
[1008], A. Ruziyeva [1017], R. Saboiev [1020], G. Savard [1046], G. Schenk [1051],
H. Schmidt [1052], J. Shaw [1064], S.A Siddiqui [1083], L. Vicente [1187], S. Vogel
[1193], A. Werner [1238], U. Wen [1228], R. Winter [1244], P. Xu [1264], J. Zhang
[1330], A.B. Zemkoho [1307, 1308]

Edited volumes are Anandalingam and Friesz [59], Dempe and Kalashnikov [357], Migdalas et al. [861]

References

- K. Aardal, M. Labbé, J. Leung, and M. Queranne, On the two-level uncapacitated facility location problem, INFORMS Journal on Computing 8 (1996), 289–301.
- S.A. Abass, Bilevel programming approach applied to the flow shop scheduling problem under fuzziness, Computational Management Science 2 (2005), no. 4, 279–293.
- H. Abou-Kandil and P. Bertrand, Government private sector relations as a Stackelberg game: A degenerate case, Journal of Economical Dynamics and Control 11 (1987), 513–517.
- A. Aboussoror, Weak bilevel programming problems: existence of solutions, Advances in Mathematics Research 1 (2002), 83–92.
- A. Aboussoror and S. Adly, A Fenchel-Lagrange duality approach for a bilevel programming problem with extremal-value function., Journal of Optimization Theory and Applications 149 (2011), no. 2, 254–268.
- 6. _____, New necessary and sufficient optimality conditions for strong bilevel programming problems, Journal of Global Optimization **70** (2018), no. 2, 309–327.
- A. Aboussoror, S. Adly, and V. Jalby, Weak nonlinear bilevel problems: existence of solutions via reverse convex and convex maximization problems., Journal of Industrial and Management Optimization 7 (2011), no. 3, 559–571.
- A. Aboussoror, S. Adly, and F.E. Saissi, Strong-weak nonlinear bilevel problems: existence of solutions in a sequential setting, Set-Valued and Variational Analysis 25 (2017), no. 1, 113–132.
- 9. ____, A duality approach for a class of semivectorial bilevel programming problems, Vietnam J. Math. 46 (2018), no. 1, 197 – 214.
- 10. A. Aboussoror, Z. Ankhili, and A. Mansour, *Bilevel programs: approximation results in*volving reverse convex programs, Pacific Journal of Optimization 4 (2008), 279–291.
- A. Aboussoror and P. Loridan, Existence and approximation results involving regularized constrained Stackelberg problems., Journal of Mathematical Analysis and Applications 188 (1994), no. 1, 101–117.
- 12. ____, Sequential stability of regularized constrained Stackelberg problems., Optimization **33** (1995), no. 3, 251–270.
- 13. _____, Strong-weak Stackelberg problems in finite dimensional spaces, Serdica Mathematical Journal **21** (1995), 151–170.
- 14. _____, Existence of solutions to two-level optimization problems with nonunique lowerlevel solutions., Journal of Mathematical Analysis and Applications **254** (2001), no. 2, 348–357.
- A. Aboussoror and A. Mansouri, Weak linear bilevel programming problems: existence of solutions via a penalty method, Journal of Mathematical Analysis and Applications **304** (2005), 399–408.
- L Adam, R Henrion, and J Outrata, On m-stationarity conditions in mpecs and the associated qualification conditions, Tech. report, ÚTIA, Czech Academy of Sciences, Czech Republic, 2016.
- 17. P. Adasme and A. Lisser, A computational study for bilevel quadratic programs using semidefinite relaxations, European Journal of Operational Research 254 (2016), no. 1, 9–18.
- 18. S. Addoune, Optimisation à deux niveaux : Conditions d'optimalité, approximation et stabilité, Ph.D. thesis, Université de Bourgogne, Département de Mathématique, 1994.
- S. Afşar, L. Brotcorne, P. Marcotte, and G. Savard, Achieving an optimal trade-off between revenue and energy peak within a smart grid environment, Renewable Energy 91 (2016), 293–301.
- 20. S. Aghajani and M. Kalantar, Operational scheduling of electric vehicles parking lot integrated with renewable generation based on bilevel programming approach, Energy (2017), in press.
- 21. J. Agor and O.Y. Özaltın, Feature selection for classification models via bilevel optimization, Computers & Operations Research (2018).
- 22. R.K. Ahuja and J.B. Orlin, *Inverse optimization*, Operations Research **49** (2001), no. 5, 771–783.
- 23. E. Aiyoshi and K. Shimizu, *Hierarchical decentralized systems and its new solution by a barrier method*, IEEE Transactions on Systems, Man, and Cybernetics **11** (1981), 444–449.

- 24. _____, A solution method for the static constrained Stackelberg problem via penalty method, IEEE Transactions on Automatic Control **29** (1984), 1111–1114.
- 25. M.A. Aizerman and A.V. Malishevski, *Conditions for universal reducibility of a two-stage extremization problem to a one-stage problem*, Journal of Mathematical Analysis and Applications **119** (1986), 361–388.
- 26. T. Akbari, S. Zolfaghari Moghaddam, E. Poorghanaat, and F. Azimi, *Coordinated planning* of generation capacity and transmission network expansion: A game approach with multileader-follower, International Transactions on Electrical Energy Systems (2017).
- H.G. Akdemir and F. Tiryaki, Bilevel stochastic transportation problem with exponentially distributed demand, Bitlis Eren University Journal of Science and Technology 2 (2012), no. 1.
- 28. D. Aksen, S.S. Akca, and N. Aras, A bilevel partial interdiction problem with capacitated facilities and demand outsourcing, Computers & Operations Research 41 (2014), 346–358.
- F. Al-Khayyal, R. Horst, and P. Pardalos, Global optimization of concave functions subject to quadratic constraints: an application in nonlinear bilevel programming, Annals of Operations Research 34 (1992), 125–147.
- 30. S. Albaek, *Stackelberg leadership as a natural solution under cost uncertainty*, The Journal of Industrial Economics (1990), 335–347.
- S. Albrecht, M. Leibold, and M. Ulbrich, A bilevel optimization approach to obtain optimal cost functions for human arm-movements, Numerical Algebra, Control and Optimization 2 (2012), no. 1, 105–127.
- 32. S. Albrecht, K. Ramirez-Amaro, F. Ruiz-Ugalde, D. Weikersdorfer, M. Leibold, M. Ulbrich, and M. Beetz, *Imitating human reaching motions using physically inspired optimization principles*, 11th IEEE-RAS International Conference on Humanoid Robots (Humanoids), 2011, IEEE, 2011, pp. 602–607.
- 33. E. Alekseeva, Y. Kochetov, and E.-G. Talbi, A matheuristic for the discrete bilevel problem with multiple objectives at the lower level, International Transactions in Operational Research 24 (2017), no. 5, 959–981.
- E. Alekseeva, N. Kochetova, Yu. Kochetov, and A. Plyasunov, A hybrid memetic algorithm for the competitive p-median problem, IFAC Proceedings Volumes 42 (2009), no. 4, 1533– 1537.
- G.M. Aleshchenko and E.N. Bukvareva, Two-level hierarchical model of optimal biological diversity, Biology bulletin 37 (2010), no. 1, 1–9.
- 36. N. Alexandrov and J.E. Dennis, *Algorithms for bilevel optimization*, Institute for Computer Applications in Science and Engineering, NASA Langley Research Center, 1994.
- N. Alguacil, A. Delgadillo, and J.M. Arroyo, A trilevel programming approach for electric grid defense planning, Computers & Operations Research 41 (2014), 282–290.
- S.M. Alizadeh, P. Marcotte, and G. Savard, Two-stage stochastic bilevel programming over a transportation network, Transportation Research Part B: Methodological 58 (2013), 92– 105.
- 39. G.B. Allende, Mathematical programs with equilibrium constraints: solution techniques from parametric optimization, Ph.D. thesis, University of Twente, EEMCS Faculty, 2006.
- 40. G.B. Allende and G. Still, *Solving bilevel programs with the KKT-approach*, Mathematical Programming **138** (2013), 309–332.
- 41. E. Allevi, D. Aussel, and R. Riccardi, On an equilibrium problem with complementarity constraints formulation of pay-as-clear electricity market with demand elasticity, Journal of Global Optimization **70** (2018), 329 346.
- H. Almutairi and S. Elhedhli, Carbon tax based on the emission factor: a bilevel programming approach, Journal of Global Optimization 58 (2014), no. 4, 795–815.
- 43. M.J. Alves, Using mopso to solve multiobjective bilevel linear problems, International Conference on Swarm Intelligence, Springer, 2012, pp. 332–339.
- 44. M.J. Alves and J.P. Costa, An algorithm based on particle swarm optimization for multiobjective bilevel linear problems, Applied Mathematics and Computation **247** (2014), 547–561.
- 45. M.J. Alves, S. Dempe, and J.J. Júdice, Computing the pareto frontier of a bi-objective bi-level linear problem using a multiobjective mixed-integer programming algorithm, Optimization **61** (2012), no. 3, 335–358.
- 46. E. Amaldi, M. Bruglieri, and B. Fortz, On the hazmat transport network design problem, Network Optimization, Springer, 2011, pp. 327–338.

- A.H. Amer, Implementation of the-constraint method in special class of multi-objective fuzzy bi-level nonlinear problems, Pakistan Journal of Statistics and Operation Research 13 (2017), no. 4, 739–756.
- 48. R. Amir and A. Stepanova, Second-mover advantage and price leadership in bertrand duopoly, Games and Economic Behavior 55 (2006), no. 1, 1–20.
- 49. O. Amirtaheri, M. Zandieh, B. Dorri, and A.R. Motameni, A bi-level programming approach for production-distribution supply chain problem, Computers & Industrial Engineering (2017).
- M.A. Amouzegar, A global optimization method for nonlinear bilevel programming problems, IEEE Transactions on Systems, Man, and Cybernetics, Part B (Cybernetics) 29 (1999), no. 6, 771–777.
- M.A. Amouzegar and S.E. Jacobsen, A decision support system for regional hazardous waste management alternatives, Journal of applied mathematics & decision sciences 2 (1998), 23– 50.
- 52. M.A. Amouzegar and K. Moshirvaziri, A penalty method for linear bilevel programming problems, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 251–271.
- 53. _____, Determining optimal pollution control policies: An application of bilevel programming., European Journal of Operational Research **119** (1999), no. 1, 100–120.
- 54. B. An, F. Ordóñez, M. Tambe, E. Shieh, R. Yang, C. Baldwin, J. DiRenzo III, K. Moretti, B. Maule, and G. Meyer, A deployed quantal response-based patrol planning system for the us coast guard, Interfaces 43 (2013), no. 5, 400–420.
- 55. L.T.H. An, P.D. Tao, N.N. Canh, and N.V. Thoai, *DC programming techniques for solving a class of nonlinear bilevel programs.*, Journal of Global Optimization **44** (2009), no. 3, 313–337.
- G. Anandalingam, An analysis of information and incentives in bi-level programming, IEEE 1985 Proceedings of the International Conference on Cybernetics and Society, 1985, pp. 925– 929.
- 57. ____, A mathematical programming model of decentralized multi-level systems., J. Oper. Res. Soc. **39** (1988), no. 11, 1021–1033.
- 58. G. Anandalingam and V. Apprey, *Multi-level programming and conflict resolution.*, European Journal of Operational Research **51** (1991), no. 2, 233–247.
- 59. G. Anandalingam and T.L. Friesz (eds.), *Hierarchical optimization*, Annals of Operations Research **34** (1992).
- 60. G. Anandalingam and T.L. Friesz, *Hierarchical optimization: An introduction.*, Annals of Operations Research **34** (1992), 1–11.
- 61. G. Anandalingam, R. Mathieu, L. Pittard, and N. Sinha, Artificial intelligence based approaches for solving hierarchical optimization problems, Impacts of Recent Computer Advances on Operations Research (R. Sharda, B. Golden, E. Wasil, O. Balci and W. Stewart, ed.), Elsevier Science Publishing Co., Inc., 1983, pp. 289–301.
- G. Anandalingam and D.J. White, A solution method for the linear static Stackelberg problem using penalty functions., IEEE Transactions on Automatic Control 35 (1990), no. 10, 1170–1173.
- 63. M. Andersson, S. Bandaru, A. Ng, and A. Syberfeldt, Parameter tuning of moeas using a bilevel optimization approach, Evolutionary Multi-Criterion Optimization (A. Gaspar-Cunha, Carlos Henggeler, A., and C. Coello Coello, eds.), Lecture Notes in Computer Science, vol. 9018, Springer International Publishing, 2015, genetic algorithm, pp. 233–247.
- R. Andreani, S.L.C. Castro, J.L. Chela, A. Friedlander, and S.A. Santos, An inexactrestoration method for nonlinear bilevel programming problems., Comput. Optim. Appl. 43 (2009), no. 3, 307–328.
- 65. R. Andreani and J.M. Martinez, On the solution of mathematical programs with equilibrium constraints, Z. Oper. Res. 54 (2001), 345–358.
- 66. J.S. Angelo and H.J.C. Barbosa, A study on the use of heuristics to solve a bilevel programming problem, International Transactions in Operational Research 22 (2015), no. 5, 861–882.
- J.S. Angelo, E. Krempser, and H.J.C. Barbosa, Differential evolution for bilevel programming, IEEE Congress on Evolutionary Computation (CEC), IEEE, 2013, pp. 470–477.

- E. Angulo, E. Castillo, R. García-Ródenas, and J. Sánchez-Vizcaíno, A continuous bi-level model for the expansion of highway networks, Computers & Operations Research 41 (2014), 262–276.
- L.Q. Anh, P.Q. Khanh, and D.T.M. Van, Well-posedness under relaxed semicontinuity for bilevel equilibrium and optimization problems with equilibrium constraints, Journal of Optimization Theory and Applications 153 (2012), no. 1, 42–59.
- P.N. Anh, A new extragradient iteration algorithm for bilevel variational inequalities, Acta Math. Vietnam 37 (2012), 95–107.
- P.N. Anh, J.K. Kim, and L.D. Muu, An extragradient algorithm for solving bilevel pseudomonotone variational inequalities, Journal of Global Optimization 52 (2012), no. 3, 627– 639.
- 72. T.T.H. Anh, L.B. Long, and T.V. Anh, A projection method for bilevel variational inequalities, Journal of Inequalities and Applications **2014** (2014), no. 1, 205.
- T.V. Anh, A strongly convergent subgradient extragradient-halpern method for solving a class of bilevel pseudomonotone variational inequalities, Vietnam Journal of Mathematics 45 (2017), no. 3, 317–332.
- 74. T.V. Anh and L.D. Muu, A projection-fixed point method for a class of bilevel variational inequalities with split fixed point constraints, Optimization 65 (2016), no. 6, 1229–1243.
- M. Anitescu, On solving mathematical programs with complementarity constraints as nonlinear programs, Tech. Report ANL/NCS-P864-1200, Department of Mathematics, University of Pittsburgh, 2002.
- 76. _____, Global convergence of an elastic mode approach for a class of mathematical programs with equilibrium constraints, SIAM J. Optimization **16** (2005), 120–145.
- 77. Z. Ankhili and A. Mansouri, An exact penalty on bilevel programs with linear vector optimization lower level, European Journal of Operational Research **197** (2009), no. 1, 36–41.
- 78. T. Aonuma, A facet-following coordination for linear bilevel planning process, Tech. Report 86, Kobe University of Commerce, Institute of Economic Research, 1985.
- 79. P. Apivatanagul, R. A Davidson, and L.K. Nozick, *Bi-level optimization for risk-based regional hurricane evacuation planning*, Natural hazards **60** (2012), no. 2, 567–588.
- 80. C. Arbib and M. Tonelli, A non-metric bilevel location problem, Tech. report, Università degli Studi dell'Aquila, 2015.
- 81. J. Arica and S. Scheimberg, A necessary optimality condition for bilevel programming problem, Tech. report, Programa de Engenharia de Sistemas e Comutacao, Universidade Federal do Rio de Janeiro, Brazil, 1993.
- 82. ____, The bilevel programming problem: Optimality conditions, Tech. report, Universidade Estadual do Norte Fluminense, Rio de Janeiro, Brasil, 1995, Publicação Técnica Interna No. 03/95.
- 83. R. Arora and S.R. Arora, An algorithm for solving an integer linear fractional/quadratic bi-level programming problem, Advanced Modeling and Optimization 14 (2012), 57–78.
- 84. S. R. Arora and R. Gupta, Interactive fuzzy goal programming approach for bilevel programming problem, European Journal of Operational Research **194** (2009), 368–376.
- J.M. Arroyo, Bilevel programming applied to power system vulnerability analysis under multiple contingencies, IET generation, transmission & distribution 4 (2010), no. 2, 178– 190.
- 86. J.M. Arroyo and F.J. Fernández, A genetic algorithm approach for the analysis of electric grid interdiction with line switching, 15th International Conference on Intelligent System Applications to Power Systems, 2009. ISAP'09., IEEE, 2009, pp. 1–6.
- M.G. Ashtiani, A. Makui, and R. Ramezanian, A robust model for a leader?follower competitive facility location problem in a discrete space, Applied Mathematical Modelling 37 (2013), no. 1 2, 62 71.
- R. Askin, F. Camacho, V. Kalashnikov, and N. Kalashnykova, Comparison of algorithms for solving a bi-level toll setting problem, International Journal of Innovative Computing, Information and Control 6 (2010), no. 8, 3529–3549.
- 89. A. Aswani and A. Ouattara, *Duality approach to bilevel programs with a convex lower level*, arXiv preprint arXiv:1608.03260 (2016).
- C. Audet, J. Haddad, and G. Savard, A note on the definition of a linear bilevel programming problem, Applied Mathematics and Computation 181 (2006), 351–355.

- 91. ____, Disjunctive cuts for continuous linear bilevel programming, Optimization Letters 1 (2007), no. 3, 259–267.
- 92. C. Audet, P. Hansen, B. Jaumard, and G. Savard, Links between linear bilevel and mixed 0-1 programming problems, Journal of Optimization Theory and Applications 93 (1997), 273–300.
- 93. _____, On the linear maxmin and related programming problems, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 181–208.
- 94. C. Audet, G. Savard, and W. Zghal, New branch-and-cut algorithm for bilevel linear programming, Journal of Optimization Theory and Applications 134 (2007), no. 2, 353–370.
- 95. D. Aussel, P. Bendotti, and M. Pištěk, Nash equilibrium in a pay-as-bid electricity market: Part 1 existence and characterization, Optimization **0** (0), no. 0, 1–13, online first publication.
- 96. _____, Nash equilibrium in a pay-as-bid electricity market part 2 best response of a producer, Optimization $\mathbf{0}$ (0), no. 0, 1–27, online first publication.
- 97. D. Aussel, R. Correa, and M. Marechal, *Electricity spot market with transmission losses.*, Journal of Industrial and Management Optimization **9** (2013), no. 2, 275–290.
- 98. Y. Averboukh and A. Baklanov, Stackelberg solutions of differential games in the class of nonanticipative strategies, Dynamic Games and Applications 4 (2014), no. 1, 1–9.
- 99. K.B. Aviso, R.R. Tan, A.B. Culaba, and J.B. Cruz, Bi-level fuzzy optimization approach for water exchange in eco-industrial parks, Process Safety and Environmental Protection 88 (2010), no. 1, 31–40.
- 100. N Azarmir and M Zohrehbandian, A lexicographic approach for solving multiobjective bilevel programming problems., Caspian Journal of Applied Sciences Research 5 (2016), no. 4.
- H. Babahadda and N. Gadhi, Necessary optimality conditions for bilevel optimization problems using convexificators., Journal of Global Optimization 34 (2006), no. 4, 535–549.
- 102. M. Backhaus and G. Schaefer, Towards optimally resilient topologies against optimal attacks, Integrated Network and Service Management (IM), 2017 IFIP/IEEE Symposium on, IEEE, 2017, pp. 1065–1070.
- 103. S.A. Bagloee, M. Asadi, M. Sarvi, and M. Patriksson, A hybrid machine-learning and optimization method to solve bi-level problems, Expert Systems with Applications 95 (2018), no. Supplement C, 142 - 152.
- 104. S. Bahmani-Firouzi, B.and Sharifinia, R. Azizipanah-Abarghooee, and T. Niknam, Scenario-based optimal bidding strategies of gencos in the incomplete information electricity market using a new improved preypredator optimization algorithm, IEEE Systems Journal (2015), no. 99, 1–11, Application: competitive electricity market.
- 105. N.O. Bakır, A Stackelberg game model for resource allocation in cargo container security, Annals of Operations Research **187** (2011), no. 1, 5–22.
- 106. A.G. Bakirtzis, N.P. Ziogos, A.C. Tellidou, and G.A. Bakirtzis, *Electricity producer offering strategies in day-ahead energy market with step-wise offers*, IEEE Transactions on Power Systems **22** (2007), no. 4, 1804–1818.
- 107. K.R. Balachandran and J. Ronen, Incentive contracts when production is subcontracted, European Journal of Operations Research 40 (1989), 169–185.
- 108. J.F. Bard, A grid search algorithm for the linear bilevel programming problem, Proceedings of the 14th Annual Meeting of the American Institute for Decision Science, 1982, pp. 256– 258.
- 109. ____, An algorithm for the general bilevel programming problem, Mathematics of Operations Research 8 (1983), 260–272.
- 110. ____, Coordination of a multidivisional organization through two levels of management, OMEGA **11** (1983), 457–468.
- 111. ____, An efficient point algorithm for a linear two-stage optimization problem, Operations Research **31** (1983), 670–684.
- 112. ____, An investigation of the linear three level programming problem, IEEE Transactions on Systems, Man, and Cybernetics 14 (1984), 711–717.
- 113. _____, Optimality conditions for the bilevel programming problem, Naval Research Logistics Quarterly **31** (1984), 13–26.
- 114. _____, Geometric and algorithm developments for a hierarchical planning problem, European Journal of Operational Research **19** (1985), 372–383.

- 115. _____, Convex two-level optimization, Mathematical Programming 40 (1988), 15–27.
- 116. _____, Some properties of the bilevel programming problem, Journal of Optimization Theory and Applications 68 (1991), 371–378.
- 117. _____, Practical bilevel optimization: Algorithms and applications, Kluwer Academic Publishers, Dordrecht, 1998.
- 118. J.F. Bard and J. Falk, An explicit solution to the multi-level programming problem, Computers and Operations Research 9 (1982), 77–100.
- 119. J.F. Bard and J. Moore, A branch and bound algorithm for the bilevel programming problem, SIAM Journal on Scientific and Statistical Computing **11** (1990), 281–292.
- 120. ____, An algorithm for the discrete bilevel programming problem, Naval Research Logistics **39** (1992), 419–435.
- 121. J.F. Bard, J.C. Plummer, and J.C. Sourie, *Determining tax credits for converting nonfood crops to biofuels: an application of bilevel programming*, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 23–50.
- 122. _____, A bilevel programming approach to determining tax credits for biofuel production, European Journal of Operational Research. **120** (2000), 30–46.
- 123. B. Barnhart, Z. Lu, M. Bostian, A. Sinha, K. Deb, L. Kurkalova, M. Jha, and G. Whittaker, *Handling practicalities in agricultural policy optimization for water quality improvements*, Proceedings of the Genetic and Evolutionary Computation Conference, ACM, 2017, pp. 1065–1072.
- 124. K. Basu, Stackelberg equilibrium in oligopoly: an explanation based on managerial incentives, Economics Letters 49 (1995), no. 4, 459–464.
- 125. M. Bazine, A. Bennani, and N. Gadhi, Fuzzy optimality conditions for fractional multiobjective bilevel problems under fractional constraints., Numer. Funct. Anal. Optim. 32 (2011), no. 2, 126–141.
- 126. A. Beck and S. Sabach, A first order method for finding minimal norm-like solutions of convex optimization problems, Mathematical Programming 147 (2014), no. 1, 25–46.
- 127. K. Bedhrinath and J. R. J. Rao, Bilevel models for optimum designs which are insensitive to perturbations in variables and parameters, Tech. report, University of Houston, U. S. A., 2003.
- 128. B. Beheshti, O.A. Prokopyev, and E.L. Pasiliao, Exact solution approaches for bilevel assignment problems, Computational Optimization and Applications 64 (2016), no. 1, 215– 242.
- 129. O. Ben-Ayed, Bilevel linear programming: analysis and application to the network design problem, Ph.D. thesis, University of Illinois at Urbana-Champaign, 1988.
- 130. _____, A bilevel linear programming model applied to Tunisian interegional High way network design problem, Revue Tunesienne d'Economie et de Gestion V (1990), 234–277.
- 131. ____, Bilevel linear programming, Computers and Operations Research **20** (1993), 485–501.
- 132. O. Ben-Ayed and C. Blair, Computational difficulties of bilevel linear programming, Operations Research **38** (1990), 556–560.
- 133. O. Ben-Ayed, C. Blair, D. Boyce, and L. LeBlanc, Construction of a real-world bilevel linear programming model of the highway design problem, Annals of Operations Research 34 (1992), 219–254.
- 134. O. Ben-Ayed, D. Boyce, and C. Blair, A general bilevel linear programming formulation of the network design problem, Transportation Research 22 B (1988), 311–318.
- 135. F. Benita, S. Dempe, and P. Mehlitz, Bilevel optimal control problems with pure state constraints and finite-dimensional lower level, SIAM Journal on Optimization 26 (2016), no. 1, 564–588.
- 136. F. Benita and P. Mehlitz, Bilevel optimal control with final-state-dependent finitedimensional lower level, SIAM Journal on Optimization **26** (2016), no. 1, 718–752.
- 137. K.P. Bennett, J. Hu, X. Ji, G. Kunapuli, and J.-S. Pang, Model selection via bilevel optimization, Neural Networks (2006), 1922–1929, M, statistical learningachine learning.
- 138. K.P. Bennett, G. Kunapuli, J. Hu, and J.-S. Pang, Bilevel optimization and machine learning, Computational Intelligence: Research Frontiers, Springer, 2008, pp. 25–47.
- 139. H. Benson, On the structure and properties of a linear multilevel programming problem, Journal of Optimization Theory and Applications **60** (1989), 353–373.

- 140. H.P. Benson, *Optimization over the efficient set*, Journal of Mathematical Analysis and Applications **98** (1984), 562–580.
- 141. _____, An all-linear programming relaxation algorithm for optimizing over the efficient set, Journal of Global Optimization 1 (1991), no. 1, 83–104.
- 142. H.Y. Benson, D.F. Shanno, and R.J. Vanderbei, *Interior-point methods for nonconvex programming: complementarity constraints*, Tech. report, Operations Research and Financial Engineering Department, Princeton University, 2002.
- 143. A. Bensoussan, M.H.M. Chau, Y. Lai, and S.C.P. Yam, *Linear-quadratic mean field Stack-elberg games with state and control delays*, SIAM Journal on Control and Optimization 55 (2017), no. 4, 2748–2781.
- 144. A. Bensoussan, M.H.M. Chau, and S.C.P. Yam, Mean field Stackelberg games: Aggregation of delayed instructions, SIAM Journal on Control and Optimization 53 (2015), no. 4, 2237– 2266.
- 145. G.C. Bento, J.X. Cruz Neto, J.O. Lopes, P.A. Soares Jr, and A. Soubeyran, Generalized proximal distances for bilevel equilibrium problems, SIAM Journal on Optimization 26 (2016), no. 1, 810–830.
- 146. V. Beresnev, Branch-and-bound algorithm for a competitive facility location problem, Computers & Operations Research 40 (2013), no. 8, 2062–2070.
- 147. V.L. Beresnev and A.A. Melnikov, Approximate algorithms for the competitive facility location problem, Journal of Applied and Industrial Mathematics 5 (2011), no. 2, 180–190.
- M. Bergouniuox and M. Haddou, A regularization method for ill-posed bilevel optimization problems, RAIRO Operations Research 40 (2006), 19–35.
- 149. F. Bernstein and A. Federgruen, *Pricing and replenishment strategies in a distribution system with competing retailers*, Operations Research **51** (2003), no. 3, 409–426.
- 150. C.A. Berry, B.F. Hobbs, W.A. Meroney, R.P. O'Neill, and W.R. Jr. Stewart, Analyzing strategic bidding behavior in transmission networks, Utility Policy 8 (1999), 139–158.
- 151. Z. Bi, Numerical methods for bilevel programming problems, Ph.D. thesis, Department of Systems Design Engineering, University of Waterloo, 1992.
- 152. Z. Bi and P. Calamai, Optimality conditions for a class of bilevel programming problems, Tech. Report #191-O-191291, Department of Systems Design Engineering, University of Waterloo, 1991.
- 153. Z. Bi, P. Calamai, and A. Conn, An exact penalty function approach for the linear bilevel programming problem, Tech. Report #167-O-310789, Department of Systems Design Engineering, University of Waterloo, 1989.
- 154. _____, An exact penalty function approach for the nonlinear bilevel programming problem, Tech. Report #180-O-170591, Department of Systems Design Engineering, University of Waterloo, 1991.
- 155. W. Bialas and M. Karwan, *Multilevel linear programming*, Tech. Report 78–1, Operations Research Program, State University of New York at Buffalo, 1978.
- 156. ____, On two-level optimization, IEEE Transactions on Automatic Control 27 (1982), 211–214.
- 157. _____, Two-level linear programming, Management Science **30** (1984), 1004–1020.
- 158. W. Bialas, M. Karwan, and J. Shaw, A parametric complementary pivot approach for two-level linear programming, Tech. Report 80–82, Operations Research Program, State University of New York at Buffalo, 1980.
- 159. L. Bianco, M. Caramia, and S. Giordani, A bilevel flow model for hazmat transportation network design, Transportation Research Part C: Emerging Technologies 17 (2009), no. 2, 175–196.
- 160. R. Birla, V.K. Agarwal, I.A. Khan, and V.N. Mishra, An alternative approach for solving bi-level programming problems, American Journal of Operations Research 7 (2017), no. 03, 239.
- 161. J. Bisschop, W. Candler, J. Duloy, and G. O'Mara, The indus basin model: a special application of two-level linear programming, Mathematical Programming Study 20 (1982), 30–38.
- 162. M. Bjørndal and K. Jørnsten, The deregulated electricity market viewed as a bilevel programming problem, Journal of Global Optimization 33 (2005), no. 3, 465–475.
- C. Blair, The computational complexity of multi-level linear programs, Annals of Operations Research 34 (1992), 13–19.

- 164. G Boglárka and K. Kovács, Solving a huff-like Stackelberg location problem on networks, Journal of Global Optimization 64 (2016), no. 2, 233–247.
- 165. G.M. Bollas, P.I. Barton, and A. Mitsos, Bilevel optimization formulation for parameter estimation in vapor-liquid (-liquid) phase equilibrium problems, Chemical Engineering Science 64 (2009), no. 8, 1768–1783.
- 166. H. Bonnel, Optimality conditions for the semivectorial bilevel optimization problem, Pacific Journal of Optimization 2 (2006), no. 3, 447–467.
- 167. H. Bonnel and J. Collonge, Stochastic optimization over a Ppareto set associated with a stochastic multi-objective optimization problem, Journal of Optimization Theory and Applications 162 (2014), no. 2, 405–427.
- 168. _____, Optimization over the Pareto outcome set associated with a convex bi-objective optimization problem: theoretical results, deterministic algorithm and application to the stochastic case, Journal of Global Optimization **62** (2015), no. 3, 481–505.
- 169. H. Bonnel and J. Morgan, Semivectorial bilevel optimization problem: penalty approach, Journal of Optimization Theory and Applications **131** (2006), 365–382.
- 170. _____, Semivectorial bilevel convex optimal control problems: existence results, SIAM Journal on Control and Optimization **50** (2012), no. 6, 3224–3241.
- 171. _____, Optimality conditions for semivectorial bilevel convex optimal control problems, Computational and analytical mathematics (H. Bauschke and M. Théera, eds.), Springer, 2013, pp. 45–78.
- 172. H. Bonnel, L. Todjihoundé, and C. Udrişte, Semivectorial bilevel optimization on Riemannian manifolds, Journal of Optimization Theory and Applications 167 (2015), 464 – 486.
- 173. M. Borza, A.S. Rambely, and M. Saraj, A Stackelberg solution to a two-level linear fractional programming problem with interval coefficients in the objective functions, Sains Malaysiana 41 (2012), 1651 – 1656.
- 174. _____, Two-level linear programming problems with two decision-makers at the upper level: An interactive fuzzy approach, Modern Applied Science 8 (2014), 211 222.
- 175. M. Bostian, G. Whittaker, B. Barnhart, R. Färe, and S. Grosskopf, Valuing water quality tradeoffs at different spatial scales: An integrated approach using bilevel optimization, Water Resources and Economics 11 (2015), 1–12.
- 176. M. Bouhtou, S. van Hoesel, A. F van der Kraaij, and J.-L. Lutton, *Tariff optimization in networks*, INFORMS journal on computing **19** (2007), no. 3, 458–469.
- 177. K. Bouibed, H. Slimani, and M.S. Radjef, Global efficiency for multiobjective bilevel programming problems under generalized invexity, Journal of Applied Mathematics and Computing 53 (2017), no. 1-2, 507–530.
- 178. D. Boyce and L. Mattsson, Modeling residential location choice in relation to housing location and road tolls on congested urban highway networks, Transportation Research Part B: Methodological 33 (1999), no. 8, 581–591.
- 179. J. Bracken, J. Falk, and J. McGill, Equivalence of two mathematical programs with optimization problems in the constraints, Operations Research 22 (1974), 1102–1104.
- 180. J. Bracken and J. McGill, Mathematical programs with optimization problems in the constraints, Operations Research **21** (1973), 37–44.
- 181. _____, Defense applications of mathematical programs with optimization problems in the constraints, Operations Research **22** (1974), 1086–1096.
- 182. ____, A method for solving mathematical programs with nonlinear programs in the constraints, Operations Research 22 (1974), 1097–1101.
- 183. _____, Production and marketing decisions with multiple objectives in a competitive environment, Journal of Optimization Theory and Applications 24 (1978), 449–458.
- 184. A. Breiner and M. Avriel, Two-stage approach for quantitative policy analysis using bilevel programming, Journal of Optimization Theory and Applications 100 (1999), 15–27.
- 185. M. Breton, A. Alj, and A. Haurie, Sequential Stackelberg equilibria in two-person games, Journal of Optimization Theory and Applications 59 (1988), 71–97.
- 186. L. Brotcorne, S. Hanafi, and R. Mansi, A dynamic programming algorithm for the bilevel knapsack problem, Operations Research Letters 37 (2009), no. 3, 215–218.
- 187. _____, One-level reformulation of the bilevel knapsack problem using dynamic programming, Discrete Optimization **10** (2013), no. 1, 1–10.
- 188. L. Brotcorne, M. Labbé, P. Marcotte, and G. Savard, A bilevel model and solution algorithm for a freight tariff setting problem, Transportation Science 34 (2000), 289–302.

- 189. ____, A bilevel model for toll optimization on a multicommodity transportation network, Transportation Science **35** (2001), no. 4, 345–358.
- 190. L. Brotcorne, P. Marcotte, and G. Savard, *Bilevel programming: The Montreal school*, INFOR **46** (2008), no. 4, 231 246.
- 191. G. Brown, M. Carlyle, D. Diehl, J. Kline, and K. Wood, A two-sided optimization for theater ballistic missile defense, Operations research 53 (2005), no. 5, 745–763.
- 192. G. Brown, M. Carlyle, J. Salmerón, and K. Wood, *Defending critical infrastructure*, Interfaces 36 (2006), no. 6, 530–544.
- 193. G.G. Brown, W.M. Carlyle, R.C. Harney, E.M. Skroch, and R.K. Wood, Interdicting a nuclear-weapons project, Operations Research 57 (2009), no. 4, 866–877.
- 194. G.G. Brown, W.M. Carlyle, J. Salmeron, and K. Wood, Analyzing the vulnerability of critical infrastructure to attack and planning defenses, Emerging Theory, Methods, and Applications, INFORMS, 2005, pp. 102–123.
- 195. A. Budnitzki, The solution approach to linear fuzzy bilevel optimization problems, Optimization **64** (2015), no. 5, 1195–1209.
- 196. L.F. Bueno, G. Haeser, and J.M. Martínez, An inexact restoration approach to optimization problems with multiobjective constraints under weighted-sum scalarization, Optimization Letters 10 (2016), no. 6, 1315–1325.
- 197. V.A. Bulavski and V.V. Kalashnikov, Equilibrium in generalized Cournot and Stackelberg models, Economica i Matematicheskie Metody **31** (1995), no. 3, 151 – 163.
- 198. _____, Equilibrium in generalized Cournot and Stackelberg models, Zeitschrift für Angewandte Mathematik und Mechanik **76** (1996), 387–388.
- 199. A.P. Burgard, P. Pharkya, and C.D. Maranas, Optknock: A bilevel programming framework for identifying gene knockout strategies for microbial strain optimization, Biotechnology and Bioengineering 84 (2003), no. 6, 647 – 657, Biotechnology application.
- 200. J.A. Bustos, S.H. Olavarria, V.M. Albornoz, S.V. Rodríguez, and M.A. Jiménez-Lizárraga, A Stackelberg game model between manufacturer and wholesaler in a food supply chain., ICORES, 2017, pp. 409–415.
- 201. A. Cabot, Proximal point algorithm controlled by a slowly vanishing term: applications to hierarchical minimization, SIAM Journal on Optimization 15 (2005), no. 2, 555–572.
- 202. W.D. Cai, *Electricity markets for the smart grid: Networks, timescales, and integration with control*, Ph.D. thesis, California Institute of Technology, 2016.
- 203. P. Calamai and L. Vicente, *Generating linear and linear-quadratic bilevel programming* problems, SIAM Journal on Scientific and Statistical Computing 14 (1993), 770–782.
- 204. _____, Algorithm 728: Fortran subroutines for generating quadratic bilevel programming test methods, ACM Transactions on Mathematical Software **20** (1994), 120–123.
- 205. ____, Generating quadratic bilevel programming test problems, ACM Transactions on Mathematical Software **20** (1994), 103–119.
- 206. P.H. Calamai, L.N. Vicente, and J.J. Júdice, A new technique for generating quadratic programming test problems, Mathematical Programming (1993), 215–231.
- 207. H.I. Calvete and C. Galé, On the quasiconcave bilevel programming problem, Journal of Optimization Theory and Applications **98** (1998), 613–622.
- 208. _____, The bilevel linear/linear fractional programming problem, European Journal of Operational Research. **114** (1999), 188–197.
- 209. _____, Local optimality in quasiconcave bilevel programming., Madaune-Tort, M. (ed.) et al., 7th Zaragoza-Pau conference on applied and statistical mathematics, Jaca (Huesca), September 17–18, 2001. Zaragoza: Univ. de Zaragoza, Seminario Matemático "García de Galdeano". Monogr. Semin. Mat. "García de Galdeano" 27, 153–160 (2003)., 2003.
- 210. ____, A note on 'bilevel linear fractional programming problem'., European Journal of Operational Research. 152 (2004), no. 1, 296–299.
- 211. _____, A penalty method for solving bilevel linear fractional/linear programming problems., Asia-Pacific Journal of Operational Research **21** (2004), 207–224.
- 212. _____, Optimality conditions for the linear fractional/quadratic bilevel problem, VIII Journées Zaragoza-Pau de Mathématiques Appliquées et de Statistiques, Monogr. Semin. Mat. García Galdeano, no. 31, Prensas Univ. Zaragoza, Zaragoza, 2004, pp. 285–294.
- 213. ____, Solving linear fractional bilevel programs., Oper. Res. Lett. 32 (2004), no. 2, 143– 151.

- 214. _____, Note on the 'Optimality conditions for linear fractional bilevel programs'., Indian J. Pure Appl. Math. 36 (2005), no. 1, 23–34.
- 215. ____, Linear bilevel multi-follower programming with independent followers., Journal of Global Optimization **39** (2007), no. 3, 409–417.
- 216. _____, Bilevel multiplicative problems: A penalty approach to optimality and a cutting plane based algorithm., Journal of Computational and Applied Mathematics 218 (2008), no. 2, 259–269 (English).
- 217. _____, A multiobjective bilevel program for production-distribution planning in a supply chain., Ehrgott, Matthias (ed.) et al., Multiple criteria decision making for sustainable energy and transportation systems. Proceedings of the 19th international conference on multiple criteria decision making, Auckland, New Zealand, 7th 12th January 2008. Berlin: Springer. Lecture Notes in Economics and Mathematical Systems 634, 155–165 (2010)., 2010.
- 218. _____, Linear bilevel programs with multiple objectives at the upper level., Journal of Computational and Applied Mathematics **234** (2010), no. 4, 950–959.
- 219. ____, On linear bilevel problems with multiple objectives at the lower level, Omega **39** (2011), 33–40.
- 220. _____, Linear bilevel programming with interval coefficients., Journal of Computational and Applied Mathematics **236** (2012), no. 15, 3751–3762.
- 221. H.I. Calvete, C. Galé, S. Dempe, and S. Lohse, *Bilevel problems over polyhedra with extreme point optimal solutions.*, Journal of Global Optimization **53** (2012), no. 3, 573–586.
- 222. H.I. Calvete, C. Galé, and J.A. Iranzo, Planning of a decentralized distribution network using bilevel optimization, Omega 49 (2014), 30–41.
- 223. H.I. Calvete, C. Galé, and P.M. Mateo, A new approach for solving linear bilevel problems using genetic algorithms., European Journal of Operational Research. 188 (2008), no. 1, 14–28.
- 224. ____, A genetic algorithm for solving linear fractional bilevel problems., Annals of Operations Research **166** (2009), 39–56.
- 225. H.I. Calvete, C. Galé, and M.-J. Oliveros, Bilevel model for production-distribution planning solved by using ant colony optimization., Comput. Oper. Res. 38 (2011), no. 1, 320–327.
- 226. F. Camacho, *Two examples of a bilevel toll setting problem*, Proceedings, International Business and Economics Research Conference, Las Vegas, 2006, 2006.
- 227. J.-F. Camacho-Vallejo, Á.E. Cordero-Franco, and R.G. González-Ramírez, Solving the bilevel facility location problem under preferences by a Stackelberg-evolutionary algorithm, Mathematical Problems in Engineering **2014** (2014), 14 pages.
- 228. J.-F. Camacho-Vallejo, E. González-Rodríguez, F.-J. Almaguer, and R.G. González-Ramírez, A bi-level optimization model for aid distribution after the occurrence of a disaster, Journal of Cleaner Production 105 (2014), 134 – 145.
- 229. J.-F. Camacho-Vallejo, J. Mar-Ortiz, López-Ramos F., and Rodríguez R.P., A genetic algorithm for the bi-level topological design of local area networks, PLoS ONE 10 (2015), no. 6, 21 pages.
- 230. J.F. Camacho-Vallejo and R. Muñoz S.ánchez, A path based algorithm for solve the hazardous materials transportation bilevel problem, Applied Mechanics and Materials (G. Li and C. Chen, eds.), vol. 253, Trans. Tech. Publ., 2013, pp. 1082–1088.
- 231. M. Campêlo, S. Dantas, and S. Scheimberg, A note on a penalty function approach for solving bilevel linear programs, Journal of Global Optimization 16 (2000), 245–255.
- 232. M. Campêlo and S. Scheimberg, An analysis of the bilevel linear problem by a penalty approach, Tech. report, Universidade Federal do Rio de Janeiro, Brazil, 1998.
- 233. _____, A note on a modified simplex approach for solving bilevel linear programming problems, European Journal of Operational Research **126** (2000), 454–458.
- 234. _____, Theoretical and computational results for a linear bilevel problem, Advances in Convex Analysis and Global Optimization, Springer, 2001, pp. 269–281.
- 235. _____, A simplex approach for finding local solutions of a linear bilevel program by equilibrium points, Annals of operations research **138** (2005), no. 1, 143–157.
- 236. _____, A study of local solutions in linear bilevel programming, Journal of optimization theory and applications **125** (2005), no. 1, 63–84.
- 237. W. Candler, A linear bilevel programming algorithm: a comment, Computers and Operations Research 15 (1988), 297–298.

- 238. W. Candler, J. Fortuny-Amat, and B. McCarl, *The potential role of multilevel programming* in agricultural economics, American Journal of Agricultural Economics **63** (1981), 521–531.
- 239. W. Candler and R. Norton, *Multilevel programming*, Tech. Report 20, World Bank Development Research Center, Washington D.C., 1977.
- 240. ____, Multilevel programming and development policy, Tech. Report 258, World Bank Development Research Center, Washington D.C., 1977.
- 241. W. Candler and R. Townsley, A linear two-level programming problem, Computers and Operations Research 9 (1982), 59–76.
- 242. D. Cao and L.C. Leung, A partial cooperation model for non-unique linear two-level decision problems, European Journal of Operational Research 140 (2002), 134–141.
- 243. P. Cappanera and M.P. Scaparra, *Optimal allocation of protective resources in shortest-path networks*, Transportation Science **45** (2011), no. 1, 64–80.
- 244. A. Caprara, M. Carvalho, A. Lodi, and G.J. Woeginger, A study on the computational complexity of the bilevel knapsack problem, SIAM Journal on Optimization 24 (2014), no. 2, 823–838.
- 245. _____, Bilevel knapsack with interdiction constraints, INFORMS Journal on Computing 28 (2016), no. 2, 319–333.
- 246. M. Caramia and R. Mari, Enhanced exact algorithms for discrete bilevel linear problems, Optimization Letters 9 (2015), no. 7, 1447–1468.
- 247. _____, A decomposition approach to solve a bilevel capacitated facility location problem with equity constraints, Optimization Letters **10** (2016), no. 5, 997–1019.
- 248. J. Cardinal, E. D. Demaine, S. Fiorini, G. Joret, S. Langerman, I. Newman, and O. Weimann, *The Stackelberg minimum spanning tree game.*, Dehne, Frank (ed.) et al., Algorithms and data structures. 10th international workshop, WADS 2007, Halifax, Canada, August 15–17, 2007. Proceedings. Berlin: Springer. Lecture Notes in Computer Science 4619, 64–76 (2007)., 2007.
- 249. J. Cardinal, E.D. Demaine, S. Fiorini, G. Joret, S. Langerman, I. Newman, and O. Weimann, *The Stackelberg minimum spanning tree game*, Algorithmica **59** (2011), no. 2, 129–144.
- 250. R. Carli and M. Dotoli, Bi-level programming for the energy retrofit planning of street lighting systems, Networking, Sensing and Control (ICNSC), 2017 IEEE 14th International Conference on, IEEE, 2017, pp. 543–548.
- 251. M. Carrion, J.M. Arroyo, and A.J. Conejo, A bilevel stochastic programming approach for retailer futures market trading, IEEE Transactions on Power Systems 24 (2009), no. 3, 1446–1456.
- 252. M.-S. Casas-Ramírez and J.-F. Camacho-Vallejo, Solving the p-median bilevel problem with order through a hybrid heuristic, Applied Soft Computing **60** (2017), 73–86.
- 253. M.-S. Casas-Ramrez, J.-F. Camacho-Vallejo, and I.-A. Martnez-Salazar, Approximating solutions to a bilevel capacitated facility location problem with customer's patronization toward a list of preferences, Applied Mathematics and Computation **319** (2018), no. Supplement C, 369 – 386, Recent Advances in Computing.
- 254. L.M. Case, An l₁ penalty function approach to the nonlinear bilevel programming problem, Ph.D. thesis, University of Waterloo, Canada, 1999.
- 255. R. Cassidy, M. Kirby, and W. Raike, *Efficient distribution of resources through three levels of government*, Management Science **17** (1971), 462–473.
- 256. M. Catalano and M. Migliore, A Stackelberg-game approach to support the design of logistic terminals, Journal of Transport Geography **41** (2014), 63–73.
- 257. M. Cecchini, J. Ecker, M. Kupferschmid, and R. Leitch, Solving nonlinear principal-agent problems using bilevel programming, European Journal of Operational Research 230 (2013), no. 2, 364–373.
- 258. L.-C. Ceng, Y.-C. Liou, and C.-F. Wen, A hybrid extragradient method for bilevel pseudomonotone variational inequalities with multiple solutions, Journal of Nonlinear Science and Applications **9** (2016), no. 6, 4052–4069.
- 259. L.-C. Ceng, Y.-C. Liou, C.-F. Wen, and A. Latif, Hybrid steepest-descent viscosity methods for triple hierarchical variational inequalities with constraints of mixed equilibria and bilevel variational inequalities, Journal of Nonlinear Sciences and Applications 10 (2017), no. 3, 1126–1147.

- 260. O. Chadli, Q.H. Ansari, and S. Al-Homidan, Existence of solutions and algorithms for bilevel vector equilibrium problems: An auxiliary principle technique, Journal of Optimization Theory and Applications 172 (2017), no. 3, 726–758.
- 261. T.-S. Chang and P.B. Luh, Derivation of necessary and sufficient conditions for singlestage Stackelberg games via the inducible region concept, IEEE Transactions on Automatic Control AC-29 (1984), 63 – 66.
- 262. H. Chen, B. An, D. Niyato, Y. Soh, and C. Miao, Workload factoring and resource sharing via joint vertical and horizontal cloud federation networks, IEEE Journal on Selected Areas in Communications (2017).
- 263. J. Chen, Z. Wan, and Y. Zou, Bilevel invex equilibrium problems with applications, Optimization Letters 8 (2014), no. 2, 447–461.
- 264. Y. Chen, Bilevel programming problems: analysis, algorithms and applications, Ph.D. thesis, Université de Montréal, École Polytechnique, 1993.
- 265. Y. Chen and M. Florian, The nonlinear bilevel programming problem: a general formulation and optimality conditions, Tech. Report CRT-794, Centre de Recherche sur les Transports, 1991.
- 266. _____, On the geometry structure of linear bilevel programs: a dual approach, Tech. Report CRT-867, Centre de Recherche sur les Transports, 1992.
- 267. ____, The nonlinear bilevel programming problem: formulations, regularity and optimality conditions, Optimization **32** (1995), 193–209.
- 268. _____, Congested O-D trip demand adjustment problem: bilevel programming formulation and optimality conditions, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 1–22.
- 269. Y. Chen, M. Florian, and S. Wu, A descent dual approach for linear bilevel programs, Tech. Report CRT-866, Centre de Recherche sur les Transports, 1992.
- 270. Y. Chen, H. Lu, J. Li, L. Ren, and L. He, A leader-follower-interactive method for regional water resources management with considering multiple water demands and ecoenvironmental constraints, Journal of Hydrology 548 (2017), 121 – 134.
- 271. Y. Chen, T. Pock, R. Ranftl, and H. Bischof, *Revisiting loss-specific training of filter-based mrfs for image restoration*, Pattern Recognition, Springer, 2013, pp. 271–281.
- 272. Y. Chen, R. Ranftl, and T. Pock, Insights into analysis operator learning: From patch-based sparse models to higher order mrfs, IEEE Transactions on Image Processing 23 (2014), no. 3, 1060–1072.
- 273. C.-B. Cheng, H.-S. Shih, and B. Chen, Subsidy rate decisions for the printer recycling industry by bi-level optimization techniques, Operational Research (2017), 1–19, online first.
- 274. X. Chi, Z. Wan, and Z. Hao, Second order sufficient conditions for a class of bilevel programs with lower level second-order cone programming problem, Journal of Industrial and Management Optimization 11 (2015), no. 4, 1111–1125.
- 275. A. Chinchuluun, P.M. Pardalos, and H.-X. Huang, Multilevel (hierarchical) optimization: complexity issues, optimality conditions, algorithms, Advances in Applied Mathematics and Global Optimization 17 (2009), 197–221.
- 276. S.-W. Chiou, Optimization of area traffic control for equilibrium network flows, Transportation Science 33 (1999), no. 3, 279–289.
- 277. _____, TRANSYT derivatives for area traffic control optimisation with network equilibrium flows, Transportation Research Part B: Methodological **37** (2003), no. 3, 263–290.
- 278. _____, Bilevel programming for the continuous transport network design problem, Transportation Research Part B: Methodological **39** (2005), no. 4, 361–383.
- 279. _____, A bi-level programming for logistics network design with system-optimized flows, Information Sciences **179** (2009), no. 14, 2434–2441.
- 280. _____, Optimization of robust area traffic control with equilibrium flow under demand uncertainty, Computers & Operations Research **41** (2014), 399–411.
- 281. ____, A bi-level decision support system for uncertain network design with equilibrium flow, Decision Support Systems 69 (2015), 50–58.
- 282. _____, A cutting plane projection method for bi-level area traffic control optimization with uncertain travel demand, Applied Mathematics and Computation **266** (2015), 390 403.
- 283. A. Chowdhury, A.R. Zomorrodi, and C.D. Maranas, Bilevel optimization techniques in computational strain design, Computers & Chemical Engineering 72 (2015), 363–372.

- 284. S. Christiansen, M. Patriksson, and L. Wynter, *Stochastic bilevel programming in structural optimization*, Structural and Multidisciplinary Optimization **21** (2001), 361 371.
- T.D. Chuong, Optimality conditions for nonsmooth multiobjective bilevel optimization problems, Annals of Operations Research (2017), 1–26.
- 286. T.D. Chuong and V. Jeyakumar, Finding robust global optimal values of bilevel polynomial programs with uncertain linear constraints, Journal of Optimization Theory and Applications (2017), 1–21.
- 287. P. Clarke and A. Westerberg, A note on the optimality conditions for the bilevel programming problem, Naval Research Logistics **35** (1988), 413–418.
- 288. ____, Bilevel programming for steady-state chemical process design I. Fundamentals and algorithms, Computers & Chemical Engineering 14 (1990), 87–98.
- 289. _____, Bilevel programming for steady-state chemical process design II. Performance study for nondegenerate problems, Computers & Chemical Engineering 14 (1990), 99–110.
- 290. P.A. Clarke and A.W. Westerberg, *Optimization for design problems having more than one objective*, Computers & Chemical Engineering **7** (1983), 259–278.
- 291. J. Clegg and M.J. Smith, Cone projection versus half-space projection for the bilevel optimization of transportation networks, Transportation Research, Part B **35** (2001), 71–82.
- 292. E. Codina and L. Montero, Approximation of the steepest descent direction for the od matrix adjustment problem, Annals of Operations Research 144 (2006), no. 1, 329–362.
- 293. G. Cohen, J.-P. Quadrat, and L. Wynter, *Technical note: On the halfplane and cone algorithms for bilevel programming problems by Clegg and Smith*, Tech. report, INRIA, 2001.
- 294. B. Colson, Mathematical programs with equilibrium constraints and nonlinear bilevel programming problems, Master's thesis, Department of Mathematics, FUNDP, Namur, Belgium, 1999.
- 295. _____, BIPA (Bllevel Programming with Approximate methods) software guide and test problems, Tech. report, Département de Mathématique, Facultés Universitaires Notre-Dame de la Paix, Namur, Belgique, 2002.
- 296. _____, Trust-region algorithms for derivative-free optimization and nonlinear bilevel programming, Ph.D. thesis, Department of Mathematics, The University of Namur (Belgium), 2003.
- 297. _____, Trust-region algorithms for derivative-free optimization and nonlinear bilevel programming, 4OR, Quarterly Journal of the Belgian, French and Italian Operations Research Societies 2 (2004), no. 1, 85–88.
- 298. B. Colson, P. Marcotte, and G. Savard, A trust-region method for nonlinear bilevel programming: algorithm and computational experience., Computational Optimization and Applications **30** (2005), no. 3, 211–227.
- 299. ____, Bilevel programming: a survey., 4OR 3 (2005), 87–107.
- 300. ____, An overview of bilevel optimization., Annals of Operations Research 153 (2007), 235–256.
- 301. A.R. Conn and L.N. Vicente, Bilevel derivative-free optimization and its application to robust optimization., Optim. Methods Softw. 27 (2012), no. 3, 561–577.
- 302. I. Constantin and M. Florian, Optimizing frequencies in a transit network: a nonlinear bilevel programming approach, International Transactions in Operational Research 2 (1995), no. 2, 149–164.
- 303. J.-P. Côté, P. Marcotte, and G. Savard, A bilevel modelling approach to pricing and fare optimisation in the airline industry, Journal of Revenue and Pricing Management 2 (2003), no. 1, 23–36.
- 304. J.B.Jr. Cruz, Leader-follower strategies for multilevel systems, IEEE Transactions on Automatic Control AC-23 (1978), 244–255.
- 305. J. Current and H. Pirkul, The hierarchical network design problem with transshipment facilities, European Journal of Operational Research 52 (1991), 338 347.
- 306. J.R. Current, The design of a hierarchical transportation network with transshipment facilities, Transportation Science 22 (1988), no. 4, 270 – 277.
- 307. D.D. Čvokić, Y.A. Kochetov, and A.V. Plyasunov, A leader-follower hub location problem under fixed markups, International Conference on Discrete Optimization and Operations Research, Springer, 2016, pp. 350–363.

- 308. P. Daniele, Evolutionary variational inequalities and applications to complex dynamic multi-level models, Transportation Research Part E: Logistics and Transportation Review 46 (2010), no. 6, 855 – 880.
- 309. B. Das and M. Maiti, An application of bi-level newsboy problem in two substitutable items under capital cost, Applied Mathematics and Computation **190** (2007), no. 1, 410 422.
- 310. S.M. Dassanayaka, Methods of variational analysis in pessimistic bilevel programming, Ph.D. thesis, Wayne University Detroit, 2010.
- 311. I. Davydov, Y. Kochetov, and S. Dempe, Local search approach for the competitive facility location problem in mobile networks, International Journal of Artificial Intelligence 16 (2018), no. 1, 130–143.
- 312. J.C. De los Reyes, C.B. Schönlieb, and T. Valkonen, Bilevel parameter learning for higherorder total variation regularisation models, Journal of Mathematical Imaging and Vision 57 (2017), no. 1, 1–25.
- 313. C.H.M. de Sabóia, M. Campêlo, and S. Scheimberg, A computational study of global algorithms for linear bilevel programming, Numerical Algorithms 35 (2004), no. 2-4, 155–173.
- 314. D. De Wolf and Y. Smeers, A stochastic version of a Stackelberg-Nash-Cournot equilibrium model, Management Science 43 (1997), no. 2, 190–197.
- 315. K. Deb and A. Sinha, Constructing test problems for bilevel evolutionary multi-objective optimization, IEEE Congress on Evolutionary Computation, 2009. CEC'09., IEEE, 2009, pp. 1153–1160.
- 316. _____, Solving bilevel multi-objective optimization problems using evolutionary algorithms, Evolutionary Multi-Criterion Optimization, Springer, 2009, pp. 110–124.
- 317. _____, An efficient and accurate solution methodology for bilevel multi-objective programming problems using a hybrid evolutionary-local-search algorithm, Evolutionary computation 18 (2010), no. 3, 403–449.
- 318. A. Dekdouk, A. Azzouz, H. Yahyaoui, and S. Krichen, Solving energy ordering problem with multiple supply-demand using bilevel optimization approach, Procedia Computer Science 130 (2018), 753 – 759, The 9th International Conference on Ambient Systems, Networks and Technologies (ANT 2018) / The 8th International Conference on Sustainable Energy Information Technology (SEIT-2018) / Affiliated Workshops.
- 319. L. dell'Olio, A. Ibeas, and F. Ruisánchez, Optimizing bus-size and headway in transit networks, Transportation 39 (2012), no. 2, 449–464.
- 320. V.T. Dement'ev, A.I., R.M. Larin, and Yu.V. Shamardin, *Problems of the optimization of hierarchical structures (russian)*, Izdatel'stvo Novosibirskogo Universiteta, Novosibirsk, 1996.
- 321. V.T. Dement'ev and A.V. Pyatkin, On a decentralized transportation problem. (russian), Diskretn. Anal. Issled. Oper. 15 (2008), no. 3, 22 – 30, 95 – 96, translation in J. Appl. Ind. Math. 3 (2009), no. 1, 32?37.
- 322. V.T. Dement'ev and Y.V. Shamardin, A three-level model for the choice of nomenclature of products, Diskretnyi Analiz i Issledovanie Operatsii 8 (2001), no. 1, 40–46.
- 323. _____, The problem of price selection for production under the condition of obligatory satisfaction of demand. (russian), Diskretn. Anal. Issled. Oper. Ser. 2 9 (2002), no. 2, 31 40.
- 324. _____, A two-level assignment problem with a generalized Monge condition (russian), Diskretn. Anal. Issled. Oper. Ser. 2 10 (2003), no. 2, 19?28.
- 325. ____, On a polynomially solvable case of a decentralized transportation problem. (russian), Diskretn. Anal. Issled. Oper. **18** (2011), no. 1, 20 – 26, 102.
- 326. V. DeMiguel and W. Murray, A local convergence analysis of bilevel decomposition algorithms, Optimization and Engineering 7 (2006), no. 2, 99–133.
- 327. V. DeMiguel and H. Xu, A stochastic multiple-leader Stackelberg model: analysis, computation, and application, Operations Research 57 (2009), no. 5, 1220–1235.
- 328. ____, A stochastic multiple-leader Stackelberg model: analysis, computation, and application, Operations Research 57 (2009), no. 5, 1220–1235.
- 329. S. Dempe, A simple algorithm for the linear bilevel programming problem, Optimization **18** (1987), 373–385.
- 330. S. Dempe, On an optimality condition for a two-level optimization problem., Vestn. Leningr. Univ., Ser. I 1989 (1989), no. 3, 10–14 (Russian).

- 331. _____, Optimality condition for bilevel programming problems., Vestn. Leningr. Univ., Math. 22 (1989), no. 3, 11–16.
- 332. S. Dempe, Richtungsdifferenzierbarkeit der Lösung parametrischer Optimierungsaufgaben und ihre Anwendung bei der Untersuchung von Zwei-Ebenen-Problemen, Ph.D. thesis, Technische Universität Karl-Marx-Stadt, Sektion Mathematik, 1991, Habilitation thesis.
- 333. _____, A necessary and a sufficient optimality condition for bilevel programming problems, Optimization **25** (1992), 341–354.
- 334. _____, Optimality conditions for bilevel programming problems, System Modelling and Optimization (P. Kall et al., ed.), Lecture Notes in Control and Information Science, no. 180, Springer-Verlag, Berlin, 1992, pp. 17–24.
- 335. _____, On the directional derivative of a locally upper Lipschitz continuous point-toset mapping and its application to optimization problems, Parametric Optimization and Related Topics, III (J. Guddat, H.Th. Jongen, B. Kummer, and F. Nožička, eds.), P. Lang, 1993.
- 336. _____, On the leader's dilemma and a new idea for attacking bilevel programming problems, Tech. report, Technische Universität Chemnitz, Fachbereich Mathematik, 1993.
- 337. ____, Computing optimal incentives via bilevel programming., Optimization **33** (1995), 29–42.
- 338. _____, On generalized differentiability of optimal solutions and its application to an algorithm for solving bilevel optimization problems, Recent advances in nonsmooth optimization (D.-Z. Du, L. Qi, and R.S. Womersley, ed.), World Scientific Publishers, Singapore, 1995, pp. 36–56.
- 339. _____, Applicability of two-level optimization to issues of environmental policy, Modelling the environmental concerns of production (K. Richter, ed.), Discussion Paper, no. 62, Europa-Universität Viadrina Frankfurt (Oder), Fakultät für Wirtschaftswissenschaften, 1996, pp. 41–50.
- 340. _____, Discrete bilevel optimization problems, Tech. Report 12, Universität Leipzig, Wirtschaftswissenschaftliche Fakultät, 1996, http://www.mathe.tu-freiberg.de/~dempe.
- 341. _____, First-order necessary optimality conditions for general bilevel programming problems, Journal of Optimization Theory and Applications **95** (1997), 735–739.
- 342. _____, An implicit function approach to bilevel programming problems, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 273–294.
- 343. _____, A bundle algorithm applied to bilevel programming problems with non-unique lower level solutions, Computational Optimization and Applications 15 (2000), 145–166.
- 344. _____, Bilevel programming: the implicit function approach, Encyclopedia of Optimization, Kluwer Academic Publishers, Dordrecht, 2001, pp. 167–173.
- 345. ____, Foundations of bilevel programming, Kluwer Academic Publishers, Dordrecht et al., 2002.
- 346. _____, Annotated bibliography on bilevel programming and mathematical programs with equilibrium constraints, Optimization 52 (2003), 333–359.
- 347. _____, Bilevel programming, Essays and Surveys in Global Optimization (C. Audet, P. Hansen, and G. Savard, eds.), Kluwer Academic Publishers, Boston et al., 2005, pp. 165–194.
- 348. _____, Comment to Interactive fuzzy goal programming approach for bilevel programming problem by S.R. Arora and R. Gupta, European Journal of Operational Research 212 (2011), no. 2, 429 - 431.
- 349. _____, Bilevel optimization: Reformulation and first optimality conditions, Generalized Nash Equilibrium Problems, Bilevel Programming and MPEC (D. Aussel and C.S Lalitha, eds.), Springer, 2017, pp. 1–20.
- 350. S. Dempe and J.F. Bard, A bundle trust region algorithm for bilinear bilevel programming, Operations Research Proceedings 1999, Springer, 2000, pp. 7–12.
- 351. S. Dempe and J.F. Bard, Bundle trust-region algorithm for bilinear bilevel programming., Journal of Optimization Theory and Applications **110** (2001), no. 2, 265–288.
- 352. S. Dempe, N. Dinh, and J. Dutta, *Optimality conditions for a simple convex bilevel pro*gramming problem, Variational Analysis and Generalized Differentiation in Optimization and Control (R.S. Burachik and J.-C. Yao, eds.), Springer Optimization and Its Applications, vol. 47, Springer, 2010, pp. 149–162.
- 353. S. Dempe and J. Dutta, Is bilevel programming a special case of a mathematical program with complementarity constraints?, Mathematical Programming 131 (2012), 37–48.
- 354. S. Dempe, J. Dutta, and S. Lohse, *Optimality conditions for bilevel programming problems*, Optimization **55** (2006), 505–524.
- 355. S. Dempe, J. Dutta, and B.S. Mordukhovich, New necessary optimality conditions in optimistic bilevel programming, Optimization 56 (2007), 577–604.
- 356. _____, Variational analysis in bilevel programming, Mathematical Programming and Game Theory for Decision Making (S.K. Neogy et al., ed.), World Scientific, 2008.
- 357. S. Dempe and V. Kalashnikov (Eds.), *Optimization with multivalued mappings: Theory,* applications and algorithms, Springer Science+Business Media, LLC, 2006.
- 358. S. Dempe, D. Fanghänel, and T. Starostina, Optimal toll charges: fuzzy optimization approach, Methods of Multicriteria Decision Theory and Applications (F. Heyde, A. Löhne, and C. Tammer, eds.), Shaker Verlag, Aachen, 2009, pp. 29–45.
- 359. S. Dempe and S. Franke, *Bilevel programming: Stationarity and stability*, Pacific Journal of Optimization **9** (2013), no. 2, 183 199.
- 360. _____, Solution algorithm for an optimistic linear Stackelberg problem, Computers & Operations Research **41** (2014), 277 281.
- 361. ____, The bilevel road pricing problem, International Journal of Computing and Optimization **2** (2015), 71 92.
- 362. _____, On the solution of convex bilevel optimization problems, Computational Optimization and Applications **63** (2016), 685 703.
- 363. ____, Solution of bilevel optimization problems using the KKT approach, Tech. report, TU Bergakademie Freiberg, No. 11/2016, 2016.
- 364. S. Dempe and N. Gadhi, Necessary optimality conditions for bilevel set optimization problems., Journal of Global Optimization 39 (2007), no. 4, 529–542.
- 365. _____, Necessary optimality conditions of a D.C. set-valued bilevel optimization problem., Optimization **57** (2008), 777–793.
- 366. _____, Second order optimality conditions for bilevel set optimization problems., Journal of Global Optimization **47** (2010), no. 2, 233–245.
- 367. ____, Optimality results for a specific bilevel optimization problem., Optimization **60** (2011), no. 7–9, 813–822.
- 368. ____, A new equivalent single-level problem for bilevel problems, Optimization **63** (2014), no. 5, 789–798.
- 369. S. Dempe, N. Gadhi, and A.B. Zemkoho, New optimality conditions for the semivectorial bilevel optimization problem., Journal of Optimization Theory and Applications 157 (2013), no. 1, 54–74.
- 370. S. Dempe, N.A. Gadhi, and L. Lafhim, Fuzzy and exact optimality conditions for a bilevel set-valued problem via extremal principles., Numer. Funct. Anal. Optim. **31** (2010), no. 8, 907–920.
- 371. S. Dempe, H. Günzel, and H.Th. Jongen, On reducibility in bilevel problems, SIAM Journal on Optimization 20 (2009), 718–727.
- 372. S. Dempe, S. Ivanov, and A. Naumov, Reduction of the bilevel stochastic optimization problem with quantile objective function to a mixed-integer problem, Applied Stochastic Models in Business and Industry 33 (2017), no. 5, 544–554.
- 373. S. Dempe, V. Kalashnikov, G.A. Pérez-Valdés, and N. Kalashnykova, Bilevel programming problems: Theory, algorithms and application to energy networks, Springer-Verlag, 2015.
- 374. S. Dempe, V. Kalashnikov, and R.Z. Rios-Mercado, Discrete bilevel programming: Application to a natural gas cash-out problem, European Journal on Operational Research 166 (2005), 469–488.
- 375. S. Dempe, V.V. Kalashnikov, and N. Kalashnykova, Optimality conditions for bilevel programming problems, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Springer Science+Business Media, LLC, 2006, pp. 3–28.
- 376. S. Dempe, V.V. Kalashnikov, N.I. Kalashnykova, and A.A. Franco, A new approach to solving bi-level programming problems with integer upper level variables, ICIC Express Letters 3 (2009), no. 4.
- 377. S. Dempe and F.M. Kue, Solving discrete linear bilevel optimization problems using the optimal value reformulation, Journal of Global Optimization (2016), 1–23.

- 378. S. Dempe, F.M. Kue, and P. Mehlitz, *Optimality conditions for mixed discrete bilevel* optimization problems, Optimization **0** (2018), no. 0, 1–20.
- 379. S. Dempe, F.M. Kue, and P. Mehlitz, *Optimality conditions for special semidefinite bilevel* optimization problems, SIAM Journal on Optimization **28** (2018), no. 2, 1564–1587.
- 380. S. Dempe and S. Lohse, *Inverse linear programming*, Recent Advances in Optimization. Proceedings of the 12th French-German-Spanish Conference on Optimization held in Avignon, September 20-24, 2004 (A. Seeger, ed.), Lectures Notes in Economics and Mathematical Systems, vol. 563, Springer-Verlag, Berlin Heidelberg, 2006, pp. 19–28.
- 381. _____, Dependence of bilevel programming on irrelevant data, Tech. Report 2011-01, TU Bergakademie Freiberg, Department of Mathematics and Computer Science, www.optimization-online.org, 2011.
- 382. ____, Optimale Mautgebühren Ein Modell und ein Optimalitätstest, at Automatisierungstechnik **60** (2012), no. 4, 225–232.
- 383. S. Dempe, G. Luo, and S. Franke, *Pessimistic bilevel linear optimization*, Journal of Nepal Mathematical Society 1 (2018), 1 – 10.
- 384. S. Dempe, B.S. Mordukhovich, and A.B. Zemkoho, Sensitivity analysis for two-level value functions with applications to bilevel programming, SIAM Journal on Optimization 22 (2012), 1309–1343.
- 385. ____, Necessary optimality conditions in pessimistic bilevel programming, Optimization **63** (2014), no. 4, 505–533.
- 386. S. Dempe and M. Pilecka, Necessary optimality conditions for optimistic bilevel programming problems using set-valued programming, Journal of Global Optimization 61 (2015), no. 4, 769–788.
- 387. S. Dempe and K. Richter, *Bilevel programming with knapsack constraints*, Central European Journal of Operations Research 8 (2000), 93–107.
- 388. S. Dempe and H. Schmidt, On an algorithm solving two-level programming problems with nonunique lower level solutions, Computational Optimization and Applications 6 (1996), 227-249.
- 389. S. Dempe and T. Starostina, Optimal toll charges in a fuzzy flow problem, Computational Intelligence, Theory and Applications. Advances in Soft Computing (B. Reusch, ed.), Springer Verlag, Berlin, 2006, pp. 405–413.
- 390. _____, On the solution of fuzzy bilevel programming problems, Tech. report, TU Bergakademie Freiberg, Department of Mathematics and Computer Science, 2007.
- 391. S. Dempe and A. B. Zemkoho, The generalized Mangasarian-Fromowitz constraint qualification and optimality conditions for bilevel programs., Journal of Optimization Theory and Applications 148 (2011), no. 1, 46–68.
- 392. _____, On the Karush-Kuhn-Tucker reformulation of the bilevel optimization problem, Nonlinear Analysis: Theory, Methods & Applications **75** (2012), 1202–1218.
- 393. S. Dempe and A.B. Zemkoho, *The bilevel programming problem: reformulations, constraint qualifications and optimality conditions*, Mathematical Programming **2013** (138), 447 473.
- 394. _____, KKT reformulation and necessary conditions for optimality in nonsmooth bilevel optimization, SIAM Journal on Optimization **24** (2014), no. 4, 16391669.
- 395. S. DeNegre, Interdiction and discrete bilevel linear programming, Ph.D. thesis, Lehigh University, 2011.
- 396. S.T. DeNegre and T.K. Ralphs, A branch-and-cut algorithm for integer bilevel linear programs, Operations Research and Cyber-Infrastructure (J.W. Chinneck, B. Kristjansson, and M. Saltzman, eds.), Operations Research/Computer Science Interfaces, vol. 47, Springer US, 2009, pp. 65–78.
- 397. X. Deng, Complexity issues in bilevel linear programming, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 149–164.
- 398. A. deSilva, Sensitivity formulas for nonlinear factorable programming and their application to the solution of an implicitly defined optimization model of us crude oil production, Ph.D. thesis, George Washington University, 1978.
- 399. A. deSilva and G. McCormick, Implicitly defined optimization problems, Annals of Operations Research 34 (1992), 107–124.
- 400. M. Desrochers, P. Marcotte, and M. Stan, *The congested facility location problem*, 14th International Symposium on Mathematical Programming, Amsterdam, August 5 - 9, 1991.

- 401. J. Deuerlein, *Hydraulische systemanalyse von wasserversorgungsnetzen*, Ph.D. thesis, Universität Karlsruhe, 2002.
- 402. S. Dewez, On the toll setting problem, Ph.D. thesis, Université Libre de Bruxelles, 2004.
- 403. S. Dewez, M. Labbé, P. Marcotte, and G. Savard, New formulations and valid inequalities for a bilevel pricing problem, Oper. Res. Lett. 36 (2008), no. 2, 141–149.
- 404. S. Diamond, V. Sitzmann, S. Boyd, G. Wetzstein, and F. Heide, *Dirty pixels: Optimizing image classification architectures for raw sensor data*, arXiv preprint arXiv:1701.06487 (2017).
- 405. M. Didi-Biha, P. Marcotte, and G. Savard, *Path-based formulations of a bilevel toll setting problem*, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Optimization and its Applications, vol. 2, Springer Science+Business Media, LLC, New York, 2006, pp. 29–50.
- 406. P.H. Dien and N.D. Yen, On implicit function theorems for set-valued maps and their application to mathematical programming under inclusion constraints, Applied Mathematics and Optimization 24 (1991), no. 1, 35–54.
- 407. _____, Correction: On implicit function theorems for set-valued maps and their application to mathematical programming under inclusion constraints, Applied Mathematics & Optimization **26** (1992), no. 1, 111–111.
- 408. X.-P. Ding and Y.-C. Liou, Bilevel optimization problems in topological spaces, Taiwanese Journal of Mathematics 10 (2006), no. 1, 173–179.
- 409. B.V. Dinh, P.G. Hung, and L.D. Muu, Bilevel optimization as a regularization approach to pseudomonotone equilibrium problems, Numerical Functional Analysis and Optimization 35 (2014), no. 5, 539–563.
- 410. N Dinh, B Mordukhovich, and T.T.A. Nghia, Subdifferentials of value functions and optimality conditions for dc and bilevel infinite and semi-infinite programs, Mathematical Programming 123 (2010), no. 1, 101–138.
- 411. T. Dokka, A. Zemkoho, S.S. Gupta, and F.T. Nobibon, *Pricing toll roads under uncertainty*, OASIcs-OpenAccess Series in Informatics, vol. 54, Schloss Dagstuhl-Leibniz-Zentrum fuer Informatik, 2016.
- 412. V.F. Dökmeci, Optimum location of hierarchical production units with respect to priceelastic demand, Environment and Planning A 23 (1991), no. 11, 1671–1678.
- 413. L.F. Domínguez and E.N. Pistikopoulos, Multiparametric programming based algorithms for pure integer and mixed-integer bilevel programming problems, Computers & Chemical Engineering 34 (2010), no. 12, 2097–2106.
- 414. D. Dorsch, H.Th. Jongen, and V. Shikhman, On intrinsic complexity of nash equilibrium problems and bilevel optimization, Journal of Optimization Theory and Applications 159 (2013), no. 3, 606-634.
- 415. O. Drissi-Kaitouni and J.T. Lundgren, Bilevel origin-destination matrix estimation using a descent approach, Tech. Report LiTH-MAT-R-1992-49, Linköping Institute of Technology, Department of Mathematics, Sweden, 1992.
- 416. G. Du, Y. Xia, R.J. Jiao, and X. Liu, Leader-follower joint optimization problems in product family design, Journal of Intelligent Manufacturing (2017), 1–19.
- 417. J. Du, X. Li, L. Yu, R. Dan, and J. Zhou, Multi-depot vehicle routing problem for hazardous materials transportation: A fuzzy bilevel programming, Information Sciences (2017).
- 418. Z. Duan and L. Wang, *Heuristic algorithms for the inverse mixed integer linear program*ming problem, Journal of Global Optimization **51** (2011), no. 3, 463–471.
- 419. P.M. Duc and L.D. Muu, A splitting algorithm for a class of bilevel equilibrium problems involving nonexpansive mappings, Optimization **65** (0), 1855 1866.
- 420. T. Dudas, B. Klinz, and G.J. Woeginger, *The computational complexity of multi-level bottleneck programming problems*, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 165–179.
- 421. J.-P. Dussault, P. Marcotte, S. Roch, and G. Savard, A smoothing heuristic for a bilevel pricing problem, European Journal of Operational Research 174 (2006), no. 3, 1396–1413.
- 422. J. Dutta, Optimality conditions for bilevel programming: An approach through variational analysis, Generalized Nash Equilibrium Problems, Bilevel Programming and MPEC (D. Aussel and C.S. Lalitha, eds.), Springer Singapore, Singapore, 2017, pp. 43–64.

- 423. J. Dutta and S. Dempe, Bilevel programming with convex lower level problems, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Springer Science+Business Media, LLC, 2006.
- 424. Y. Dvorkin, R. Fernández-Blanco, D. S Kirschen, H. Pandžić, J.P. Watson, and C.A. Silva-Monroy, *Ensuring profitability of energy storage*, IEEE Transactions on Power Systems **32** (2017), no. 1, 611–623.
- 425. J. Eckardt, Zwei-Ebenen-Optimierung mit diskreten Aufgaben in der unteren Ebene, Master's thesis, TU Bergakademie Freiberg, Fakultät für Mathematik und Informatik, 1998.
- 426. J.G. Ecker and J.H. Song, *Optimizing a linear function over an efficient set*, Journal of Optimization Theory and Applications 83 (1994), no. 3, 541–563.
- 427. T. Edmunds, Algorithms for nonlinear bilevel mathematical programs, Ph.D. thesis, Department of Mechanical Engineering, University of Texas at Austin, 1988.
- 428. T. Edmunds and J.F. Bard, Algorithms for nonlinear bilevel mathematical programming, IEEE Transactions on Systems, Man, and Cybernetics 21 (1991), 83–89.
- 429. _____, An algorithm for the mixed-integer nonlinear bilevel programming problem, Annals of Operations Research **34** (1992), 149–162.
- 430. A. Ehrenmann, Equilibrium problems with equilibrium constraints and their application to electricity markets, Ph.D. thesis, University of Cambridge, Cambridge, 2004.
- 431. _____, Manifolds of multi-leader cournot equilibria, Operations Research Letters **32** (2004), no. 2, 121–125.
- 432. H. Ehtamo and T. Raivio, On applied nonlinear and bilevel programming for pursuitevasion games, Journal of Optimization Theory and Applications **108** (2001), 65–96.
- G. Eichfelder, Adaptive scalarization methods in multiobjective optimization., Vector Optimization. Berlin: Springer. xiii, 241 p., 2008.
- 434. _____, Multiobjective bilevel optimization., Mathematical Programming **123** (2010), 419–449.
- 435. H.A. Eiselt, G. Laporte, and J.-F. Thisse, Competitive location models: A framework and bibliography, Transportation Science 27 (1993), no. 1, 44–54.
- 436. B. El-Sobky and Y. Abo-Elnaga, A penalty method with trust-region mechanism for nonlinear bilevel optimization problem, Journal of Computational and Applied Mathematics 340 (2018), 360 – 374.
- 437. O.E. Emam, A fuzzy approach for bi-level integer non-linear programming problem, Applied Mathematics and Computation **172** (2006), 62–71.
- 438. _____, Interactive approach to bi-level integer multi-objective fractional programming problem, Applied Mathematics and Computation **223** (2013), 17–24.
- 439. E. Erkut and O. Alp, *Designing a road network for hazardous materials shipments*, Computers & Operations Research **34** (2007), no. 5, 1389–1405.
- 440. E. Erkut and F. Gzara, Solving the hazmat transport network design problem, Computers & Operations Research **35** (2008), no. 7, 2234–2247.
- 441. M.S. Ershova, The branch and bound method for a quadratic problem of bilevel programming, Diskretnyi Analiz i Issledovanie Operatsii **13** (2006), no. 1, 40–56, in russian.
- 442. J.B.E. Etoa, Solving convex quadratic bilevel programming problems using an enumeration sequential quadratic programming algorithm, Journal of Global Optimization 47 (2010), no. 4, 615-637.
- 443. _____, Solving quadratic convex bilevel programming problems using a smoothing method, Applied Mathematics and Computation **217** (2011), no. 15, 6680 – 6690.
- 444. J.B. Eytard, M. Akian, M. Bouhtou, and S. Gaubert, A bilevel optimization model for load balancing in mobile networks through price incentives, 15th International Symposium on Modeling and Optimization in Mobile, Ad Hoc, and Wireless Networks (WiOpt), 2017, IEEE, 2017, pp. 1–8.
- 445. G Facchetti and C Altafini, Partial inhibition and bilevel optimization in flux balance analysis, BMC bioinformatics 14 (2013), 14 pages.
- 446. N.P. Faísca, V. Dua, B. Rustem, P.M. Saraiva, and E.N. Pistikopoulos, *Parametric global* optimisation for bilevel programming, Journal of Global Optimization **38** (2007), no. 4, 609–623.
- 447. N.P. Faísca, V. Dua, P.M. Saraiva, B. Rustem, and E.N. Pistikopoulos, A global parametric programming optimisation strategy for multilevel problems, 16th European Symposium on Computer Aided Process Engineering and 9th International Symposium on Process Systems

Engineering (W. Marquardt and C. Pantelides, eds.), Computer Aided Chemical Engineering, vol. 21, Elsevier, 2006, pp. 215 – 220.

- 448. N.P. Faísca, P.M. Saraiva, B. Rustem, and E.N. Pistikopoulos, A multi-parametric programming approach for multilevel hierarchical and decentralised optimisation problems, Computational management science 6 (2009), no. 4, 377–397.
- 449. J.E. Falk and J. Liu, Algorithms for general nonlinear bilevel programs, Central European Journal of Operations Research 2 (1993), 101–117.
- 450. ____, On bilevel programming, Part I: General nonlinear cases, Mathematical Programming **70** (1995), 47–72.
- 451. M. Fampa, L.A. Barroso, D. Candal, and L. Simonetti, Bilevel optimization applied to strategic pricing in competitive electricity markets, Computational Optimization and Applications **39** (2008), no. 2, 121–142.
- 452. H. Fang, L. Xu, and K.-K.R. Choo, Stackelberg game based relay selection for physical layer security and energy efficiency enhancement in cognitive radio networks, Applied Mathematics and Computation 296 (2017), 153 – 167.
- 453. S.-C. Fang and C.-F. Hu, Solving fuzzy variational inequalities, Fuzzy Optimization and Decision Making 1 (2002), no. 1, 113–133.
- 454. D. Fanghänel, Optimality criteria for bilevel programing problems using the radial subdifferential, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Optimization and its Applications, vol. 2, Springer Science+Business Media, LLC, New York, 2006, pp. 73–95.
- 455. ____, Zwei-Ebenen-Optimierung mit diskreter unterer Ebene und stetiger oberer Ebene, Ph.D. thesis, TU Bergakademie Freiberg, 2006.
- 456. D. Fanghänel, *Optimality conditions for a bilevel matroid problem*, Journal of combinatorial optimization **22** (2011), no. 4, 594–608.
- 457. D. Fanghänel and S. Dempe, Bilevel programming with discrete lower level problems, Optimization 58 (2009), 1029 – 1047.
- 458. A.M.F. Fard and M. Hajaghaei-Keshteli, A tri-level location-allocation model for forward/reverse supply chain, Applied Soft Computing 62 (2018), 328–346.
- 459. R. Fernández-Blanco, J. M Arroyo, and N. Alguacil, On the solution of revenue-and network-constrained day-ahead market clearing under marginal pricingpart i: An exact bilevel programming approach, IEEE Transactions on Power Systems **32** (2017), no. 1, 208– 219.
- 460. R. Fernández-Blanco, J.M. Arroyo, and N. Alguacil, A unified bilevel programming framework for price-based market clearing under marginal pricing, Power Systems, IEEE Transactions on 27 (2012), no. 1, 517–525.
- 461. _____, Network-constrained day-ahead auction for consumer payment minimization, Power Systems, IEEE Transactions on **29** (2014), no. 2, 526–536.
- 462. B. Fernando and S. Gould, Discriminatively learned hierarchical rank pooling networks, International Journal of Computer Vision 124 (2017), no. 3, 335–355.
- 463. F.A. Ferreira, F. Ferreira, M. Ferreira, and A.A. Pinto, *Flexibility in a Stackelberg leadership with differentiated goods*, Optimization **64** (2015), no. 4, 877–893.
- 464. M. Fischetti, I. Ljubić, M. Monaci, and M. Sinnl, *Intersection cuts for bilevel optimization*, Integer Programming and Combinatorial Optimization. 18th International Conference International Conference on Integer Programming and Combinatorial Optimization (Q. Louveaux and Skutella M., eds.), Springer, 2016, pp. 77–88.
- 465. _____, A new general-purpose algorithm for mixed-integer bilevel linear programs, Operations Research 65 (2017), no. 6, 1615–1637.
- 466. _____, On the use of intersection cuts for bilevel optimization, Mathematical Programming (2017).
- 467. M. Fischetti, M. Monaci, and M. Sinnl, A dynamic reformulation heuristic for generalized interdiction problems, European Journal of Operational Research 267 (2018), no. 1, 40 – 51.
- 468. J. Fliege and L.N. Vicente, Multicriteria approach to bilevel optimization., Journal of Optimization Theory and Applications 131 (2006), no. 2, 209–225.
- 469. C. Florensa, P. Garcia-Herreros, P. Misra, E. Arslan, S. Mehta, and I.E. Grossmann, Capacity planning with competitive decision-makers: Trilevel MILP formulation, degeneracy, and solution approaches, European Journal of Operational Research 262 (2017), 449 – 463.

- 470. M. Florian and Y. Chen, A bilevel programming approach to estimating O-D matrix by traffic counts, Tech. Report CRT-750, Centre de Recherche sur les Transports, 1991.
- 471. _____, A coordinate descent method for bilevel O-D matrix estimation problems, International Transactions of Operations Research 2 (1995), 165–179.
- 472. C.A. Floudas, P.M. Pardalos, C. Adjiman, W.R. Esposito, Z.H. Gümüs, S.T. Harding, J.L. Klepeis, C.A. Meyer, and C.A. Schweiger, *Handbook of test problems in local and global optimization*, vol. 33, Springer Science & Business Media, 2013.
- 473. C.A. Floudas, P.M. Pardalos, C.S. Adjiman, W.R. Esposito, Z.H. Gümüs, S.T. Harding, J.L. Klepeis, C.A. Meyer, and C.A. Schweiger, *Handbook of test problems in local and global optimization*, Nonconvex Optimization and Its Applications, no. 33, Kluwer Academic Publishers, Dordrecht, 1999.
- 474. P. Fontaine and S. Minner, Benders decomposition for discrete-continuous linear bilevel problems with application to traffic network design, Transportation Research Part B: Methodological 70 (2014), 163–172.
- 475. J. Fortuny-Amat and B. McCarl, A representation and economic interpretation of a twolevel programming problem, Journal of the Operational Research Society 32 (1981), 783– 792.
- 476. A. Frangioni, On a new class of bilevel programming problems and its use for reformulating mixed integer problems, European Journal of Operational Research 82 (1995), 615–646.
- 477. S. Franke, Bilevel programming: optimal value and Karush-Kuhn-Tucker reformulation, Ph.D. thesis, TU Bergakademie Freiberg, 2014.
- 478. S. Franke, P. Mehlitz, and M. Pilecka, Optimality conditions for the simple convex bilevel programming problem in banach spaces, Optimization 67 (2018), no. 2, 237–268.
- 479. A. Friedlander and F.A.M. Gomes, Solution of a truss topology bilevel programming problem by means of an inexact restoration method, Computational & Applied Mathematics 30 (2011), no. 1, 109–125.
- 480. T. Friesz, C. Suwansirikul, and R. Tobin, Equilibrium decomposition optimization: a heuristic for the continuous equilibrium network design problem, Transportation Science 21 (1987), 254–263.
- 481. T.L. Friesz, G. Anandalingam, N.J. Mehta, K. Nam, S.J. Shah, and R.L. Tobin, *The mul*tiobjective equilibrium network design problem revisited: A simulated annealing approach, European Journal of Operational Research. 65 (1993), no. 1, 44–57.
- 482. T.L. Friesz, H.-J. Cho, N.J. Mehta, R.L. Tobin, and G. Anandalingam, A simmulated annealing approach to the network design problem with variational inequality constraints, Transpostation Science 26 (1992), 18–26.
- 483. T.L. Friesz, R.L. Tobin, H.-J. Cho, and N.J. Mehta, Sensitivity analysis based heuristic algorithms for mathematical programs with variational inequality constraints, Mathematical Programming 48 (1990), no. 1–3, 265–284.
- 484. J. Fülöp, On the equivalence between a linear bilevel programming problem and linear optimization over the efficient set, Tech. Report WP 93–1, Laboratory of Operations Research and Decision Systems, Computer and Automation Institute, Hungarian Academy of Sciences, 1993.
- 485. S.A. Gabriel and F.U. Leuthold, Solving discretely-constrained MPEC problems with applications in electric power markets, Energy Economics **32** (2010), no. 1, 3–14.
- 486. N. Gadhi and S. Dempe, Necessary optimality conditions and a new approach to multiobjective bilevel optimization problems, Journal of Optimization Theory and Applications 155 (2012), 100–114.
- 487. N Gadhi and M. El idrissi, An equivalent one level optimization problem to a semivectorial bilevel problem, Positivity (2017), 1–14, to appear.
- 488. A.A. Gaivoronski and A. Werner, *Stochastic programming perspective on the agency problems under uncertainty*, Managing Safety of Heterogeneous Systems, Springer, 2012, pp. 137–167.
- 489. J. Gang, Y. Tu, B. Lev, J. Xu, W. Shen, and L. Yao, A multi-objective bi-level location planning problem for stone industrial parks, Computers & Operations Research 56 (2015), 8–21.
- 490. J. Gao and B. Liu, Fuzzy multilevel programming with a hybrid intelligent algorithm, Computers & Mathematics with Applications 49 (2005), no. 9, 1539–1548.

- 491. Y. Gao, *Bi-level decision making with fuzzy sets and particle swarm optimisation*, Ph.D. thesis, Faculty of Engineering and Information Technology, University of Technology, Sydney, 2010.
- 492. Y. Gao, G. Zhang, and J. Lu, A particle swarm optimization based algorithm for fuzzy bilevel decision making with constraints-shared followers, Proceedings of the 2009 ACM symposium on Applied Computing, ACM, 2009, pp. 1075–1079.
- 493. Y. Gao, G. Zhang, J. Lu, T. Dillon, and X. Zeng, A λ-cut approximate algorithm for goalbased bilevel risk management systems, International Journal of Information Technology & Decision Making 7 (2008), no. 04, 589–610.
- 494. Y. Gao, G. Zhang, J. Lu, and H.-M. Wee, Particle swarm optimization for bi-level pricing problems in supply chains, Journal of Global Optimization 51 (2011), no. 2, 245–254.
- 495. Y. Gao, G. Zhang, J. Ma, and J. Lu, A-cut and goal-programming-based algorithm for fuzzy-linear multiple-objective bilevel optimization, IEEE Transactions on Fuzzy Systems 18 (2010), no. 1, 1–13.
- 496. Z. Gao, H. Sun, and H. Zhang, A globally convergent algorithm for transportation continuous network design problem, Optimization and Engineering 8 (2007), no. 3, 241–257.
- 497. L.P. Garcés, A.J. Conejo, R. García-Bertrand, and R. Romero, A bilevel approach to transmission expansion planning within a market environment, IEEE Transactions on Power Systems 24 (2009), no. 3, 1513–1522.
- 498. P. Garcia-Herreros, L. Zhang, P. Misra, E. Arslan, S. Mehta, and I.E. Grossmann, Mixedinteger bilevel optimization for capacity planning with rational markets, Computers & Chemical Engineering 86 (2016), 33–47.
- 499. I. Gaspar, J. Benavente, M. Bordagaray, B. Alonso, J.L. Moura, and A. Ibeas, A bilevel mathematical programming model to optimize the design of cycle paths, Transportation Research Procedia 10 (2015), 423–432.
- 500. E. Gassner and B. Klinz, The computational complexity of bilevel assignment problems, 4OR 7 (2009), 379–394.
- 501. E. Gebhardt and J. Jahn, *Global solver for nonlinear bilevel vector optimization problems.*, Pacific Journal of Optimization **5** (2009), no. 3, 387–401.
- 502. M. Gendreau, P. Marcotte, and G. Savard, A hybrid tabu-ascent algorithm for the linear bilevel programming problem, Journal of Global Optimization 8 (1996), 217–233.
- 503. R. Gessing, Optimal control laws for two-level hierarchical ressource allocation, Large Scale Systems 12 (1987), 69–82.
- 504. N. Ghaffarinasab and R. Atayi, An implicit enumeration algorithm for the hub interdiction median problem with fortification, European Journal of Operational Research 267 (2018), no. 1, 23 - 39.
- 505. N. Ghaffarinasab and A. Motallebzadeh, *Hub interdiction problem variants: Models and metaheuristic solution algorithms*, European Journal of Operational Research (2018), online first.
- 506. M. Ghamkhari, A. Sadeghi-Mobarakeh, and H. Mohsenian-Rad, Strategic bidding for producers in nodal electricity markets: A convex relaxation approach, IEEE Transactions on Power Systems 32 (2017), no. 3, 2324–2336.
- 507. E. Ghotbi and A.K. Dhingra, A bilevel game theoretic approach to optimum design of flywheels, Engineering Optimization 44 (2012), no. 11, 1337–1350.
- 508. A. Gibali, K.-H. Küfer, and P. Süss, Reformulating the pascoletti-serafini problem as a bi-level optimization problem, Infinite Products of Operators and Their Applications 636 (2015), 121.
- 509. F. Gilbert, P. Marcotte, and G. Savard, A numerical study of the logit network pricing problem, Transportation Science 49 (2015), no. 3, 706–719.
- 510. E.Kh. Gimadi and E.N. Goncharov, A two-level choice problem for a system of machines and nodes with a nonlinear production function, Sibirskii Zhurnal Industrial'noi Matematiki 9 (2006), no. 2, 44–54, in russian.
- 511. J. Glackin, J.G. Ecker, and M. Kupferschmid, Solving bilevel linear programs using multiple objective linear programming, Journal of optimization theory and applications **140** (2009), no. 2, 197–212.
- 512. A.I. Gladyshev, V.T. Dement'ev, and A.I. Erzin, Models and problems of the optimal synthesis of homogeneous hierarchical systems. (russian), Models and methods of optimization

(Russian), Trudy Inst. Mat., 28, Izdat. Ross. Akad. Nauk Sib. Otd. Inst. Mat., Novosibirsk (1994), 63 – 76, 149.

- 513. P.H. Gonzalez, L. Simonetti, P. Michelon, C. Martinhon, and E. Santos, A variable fixing heuristic with local branching for the fixed charge uncapacitated network design problem with user-optimal flow, Computers & Operations Research 76 (2016), 134–146.
- 514. V.J.L. González, J.F. Camacho Vallejo, and G. Pinto Serrano, A scatter search algorithm for solving a bilevel optimization model for determining highway tolls, Computación y Sistemas 19 (2015), no. 1, 3529–3549.
- 515. L.E. Gorbachevskaya, Algorithms and complexity of the bilevel standardization problems with profit correction, Diskretnij Analiz i Issledovanie Operazij, Seriya 2 5 (1998), 20–33.
- 516. _____, On the two-level extremal problem of selecting the nomenclature of products, Tech. Report 41, Russian Academy of Sciences, Siberian Branch, Insitut of Mathemetics, Novosibirsk, 1998, (in Russian).
- 517. L.E. Gorbachevskaya, V.T. Dement'ev, and Yu.V. Shamardin, *Two-level extremal problems* of selecting the nomenclature of products, Tech. Report 41, Russian Academy of Sciences, Siberian Branch, Institut of Mathemetics, Novosibirsk, 1997, (in Russian).
- 518. _____, The bilevel standardization problem with uniqueness condition for an optimal customer choice, Diskretnij Analiz i Issledovanie Operazij, Seriya 2 6 (1999), 3–11, in russian.
- 519. V.A. Gorelik, Approximate search for the maximin with constraints connecting the variables, Zhurnal Vychislitelnoi Matematiki i Matematicheskoi Fiziki 12 (1972), 510–519, (in Russian).
- 520. ____, Dynamic systems with hierarchical control structure, Cybernetics 14 (1978), no. 3, 427 430.
- 521. ____, *Hierarchical optimization-coordination systems*, Kibernetika 1 (1978), 87–94, (in Russian).
- 522. V.A. Gorelik and M.S. Shtil'man, On one class of two-level models for the regularization of economic-ecologic processes, Economica i Matematicheskie Metody XIII (1977), 1251– 1263, (in Russian).
- 523. A. Grigoriev, S. Van Hoesel, A.F. Van Der Kraaij, M. Uetz, and M. Bouhtou, *Pricing network edges to cross a river*, Lecture Notes in Computer Science, vol. 3351, pp. 140–153, Springer, 2004.
- 524. V. Grimm, L. Schewe, M. Schmidt, and G. Zöttl, A multilevel model of the european entryexit gas market, Tech. report, Friedrich-Alexander - Universität Erlangen-Nürnberg, 2017.
- 525. F. Groot, C. Withagen, and A. De Zeeuw, Note on the open-loop von stackelberg equilibrium in the cartel versus fringe model, The Economic Journal **102** (1992), no. 415, 1478–1484.
- 526. N. Groot, *Reverse Stackelberg games: Theory and applications in traffic control*, Ph.D. thesis, Delft Center for Systems and Control, 2013.
- 527. N. Groot, B. De Schutter, and H. Hellendoorn, A full characterization of the set of optimal affine leader functions in the reverse Stackelberg game, Proceedings of the 51st IEEE Conference on Decision and Control, 2012, pp. 6484–6488.
- 528. _____, A full characterization of the set of optimal affine solutions to the reverse Stackelberg game, Decision and Control (CDC), 2012 IEEE 51st Annual Conference on, IEEE, 2012, pp. 6483–6488.
- 529. ____, Reverse Stackelberg games, part ii: Results and open issues, Control Applications (CCA), 2012 IEEE International Conference on, IEEE, 2012, pp. 427–432.
- 530. _____, Optimal leader functions for the reverse Stackelberg game: Splines and basis functions, Control Conference (ECC), 2013 European, IEEE, 2013, pp. 696–701.
- 531. _____, On systematic computation of optimal nonlinear solutions for the reverse Stackelberg game, Systems, Man, and Cybernetics: Systems, IEEE Transactions on 44 (2014), no. 10, 1315–1327.
- 532. N. Groot and H. Schutter, B.and Hellendoorn, Optimal affine leader functions in reverse Stackelberg games, Journal of Optimization Theory and Applications 168 (2014), no. 1, 348–374.
- 533. S.J. Grossman and O.D. Hart, An analysis of the principal-agent problem, Econometrica 51 (1983), 7–45.

- 534. S.J. Grossman and O.D. Hart, An analysis of the principal-agent problem, Foundations of Insurance Economics (Georges Dionne and ScottE. Harrington, eds.), Huebner International Series on Risk, Insurance and Economic Security, vol. 14, Springer Netherlands, 1992, pp. 302 – 340.
- 535. T.V. Gruzdeva and E.G. Petrova, Numerical solution of a linear bilevel problem, Computational Mathematics and Mathematical Physics **50** (2010), no. 10, 1631–1641.
- 536. Z.H. Gümüs and C.A. Floudas, Global optimization of nonlinear bilevel programming problems, Journal of Global Optimization 20 (2001), 1–31.
- 537. ____, Global optimization of mixed-integer bilevel programming problems, Computational Management Science 2 (2005), 181–212.
- 538. Z. Guo, J. Chang, Q. Huang, L. Xu, C. Da, and H. Wu, Bi-level optimization allocation model of water resources for different water industries, Water Science and Technology: Water Supply 14 (2014), no. 3, 470–477.
- 539. A. Gupta and C.D. Maranas, A two-stage modeling and solution framework for multisite midterm planning under demand uncertainty, Industrial & Engineering Chemistry Research 39 (2000), no. 10, 3799–3813.
- 540. W.J. Gutjahr and N. Dzubur, *Bi-objective bilevel optimization of distribution center locations considering user equilibria*, Transportation Research Part E: Logistics and Transportation Review **85** (2016), 1–22.
- 541. F. Gzara, A cutting plane approach for bilevel hazardous material transport network design, Operations Research Letters **41** (2013), no. 1, 40–46.
- 542. M. Haan and H. Maks, Stackelberg and Cournot competition under equilibrium limit pricing, Journal of Economic Studies 23 (1996), no. 5/6, 110–127.
- 543. A. Hafezalkotob, Competition of domestic manufacturer and foreign supplier under sustainable development objectives of government, Applied Mathematics and Computation 292 (2017), 294 - 308.
- 544. L. Hajibabai, Y. Bai, and Y. Ouyang, Joint optimization of freight facility location and pavement infrastructure rehabilitation under network traffic equilibrium, Transportation Research Part B: Methodological **63** (2014), 38–52.
- 545. M. Hajinassiry, N. Amjady, and H. Sharifzadeh, *Hydrothermal coordination by bi-level* optimization and composite constraint handling method, International Journal of Electrical Power & Energy Systems **62** (2014), 476–489.
- 546. S Hakim, A Seifi, and A Ghaemi, A bi-level formulation for dea-based centralized resource allocation under efficiency constraints, Computers & Industrial Engineering 93 (2015), 2835.
- 547. J. Han, G. Liu, and S. Wang, A new descent algorithm for solving quadratic bilevel programming problems, Acta Math. Appl. Sin., Engl. Ser. 16 (2000), 235–244.
- 548. J. Han, J. Lu, Y. Hu, and G. Zhang, *Tri-level decision-making with multiple followers:* Model, algorithm and case study, Information Sciences **311** (2015), 182–204.
- 549. J. Han, J. Lu, G. Zhang, and S. Ma, *Multi-follower tri-level decision making with uncoop*erative followers, The 11th International FLINS Conference, Brazil, 2014, pp. 524–529.
- 550. J. Han, G. Zhang, Y. Hu, and J. Lu, Solving tri-level programming problems using a particle swarm optimization algorithm, IEEE 10th Conference on Industrial Electronics and Applications (ICIEA), 2015, IEEE, 2015, pp. 569–574.
- 551. ____, A solution to bi/tri-level programming problems using particle swarm optimization, Information Sciences **370** (2016), 519–537.
- 552. J. Han, G. Zhang, J. Lu, Y. Hu, and S. Ma, Model and algorithm for multi-follower tri-level hierarchical decision-making, Neural Information Processing, Springer, 2014, pp. 398–406.
- 553. K. Han, Y. Sun, H. Liu, T.L. Friesz, and T. Yao, A bi-level model of dynamic traffic signal control with continuum approximation, Transportation Research Part C: Emerging Technologies 55 (2015), 409–431.
- 554. S.D. Handoko, L.H. Chuin, A. Gupta, O.Y. Soon, H.C. Kim, and T.P. Siew, Solving multivehicle profitable tour problem via knowledge adoption in evolutionary bi-level programming, IEEE Congress on Evolutionary Computation (CEC), 2015, IEEE, 2015, pp. 2713–2720.
- 555. L.U. Hansen and P. Horst, Multilevel optimization in aircraft structural design evaluation, Computers & structures 86 (2008), no. 1, 104–118.
- 556. P. Hansen, B. Jaumard, and G. Savard, New branch-and-bound rules for linear bilevel programming, SIAM Journal on Scientific and Statistical Computing **13** (1992), 1194–1217.

- 557. F. Harder, Optimal control of the obstacle problem using the value function, Master's thesis, TU Chemnitz, Department of Mathematics, 2016.
- 558. W.E. Hart, R.L.-Y. Chen, J.D. Siirola, and J.-P. Watson, *Modeling bilevel programs in pyomo.*, Tech. report, Sandia National Laboratories (SNL-NM), Albuquerque, NM (United States); Sandia National Laboratories, Livermore, CA, 2015.
- 559. K. Hatz, S. Leyffer, J.P. Schlöder, and H.G. Bock, *Regularizing bilevel nonlinear programs* by lifting, Preprint ANL/MCS-P4076-0613 (2013).
- 560. A. Haurie, R. Loulou, and G. Savard, A two-level systems analysis model of power cogeneration under asymmetric pricing, Proceedings of IEEE Automatic Control Conference (San Diego), 1990.
- 561. _____, A two player game model of power cogeneration in new england, IEEE Transactions on Automatic Control **37** (1992), 1451–1456.
- 562. A. Haurie, G. Savard, and D. White, A note on: an efficient point algorithm for a linear two-stage optimization problem, Operations Research **38** (1990), 553–555.
- 563. L. He, G.H. Huang, and H. Lu, Greenhouse gas emissions control in integrated municipal solid waste management through mixed integer bilevel decision-making, Journal of hazardous materials 193 (2011), 112–119.
- 564. X. He, C. Li, T. Huang, and C. Li, Neural network for solving convex quadratic bilevel programming problems, Neural Networks **51** (2014), 17–25.
- 565. X. He, Y. Zhou, and Z. Chen, Evolutionary bilevel optimization based on covariance matrix adaptation, IEEE Transactions on Evolutionary Computation (2018).
- 566. G. Heilporn, M. Labbé, P. Marcotte, and G. Savard, *The highway problem: models, complexity and valid inequalities*, 2006.
- 567. _____, A parallel between two classes of pricing problems in transportation and marketing, Journal of Revenue and Pricing Management **9** (2010), no. 1-2, 110–125.
- 568. _____, A polyhedral study of the network pricing problem with connected toll arcs, Networks 55 (2010), no. 3, 234–246.
- 569. S.R. Hejazi, A. Memariani, G. Jahanshaloo, and M.M. Sepehri, *Linear bilevel programming* solution by genetic algorithm, Computers & Operations Research **29** (2002), 1913–1925.
- 570. H. Held and D.L. Woodruff, Heuristics for multi-stage interdiction of stochastic networks, Journal of Heuristics 11 (2005), no. 5-6, 483–500.
- 571. M. Hemmati and J.C. Smith, A mixed-integer bilevel programming approach for a competitive prioritized set covering problem, Discrete Optimization **20** (2016), 105–134.
- 572. E.M.T. Hendrix, On competition in a Stackelberg location-design model with deterministic supplier choice, Annals of Operations Research 246 (2016), no. 1-2, 19–30.
- 573. C. Henkel, An algorithm for the global resolution of linear stochastic bilevel programs, Ph.D. thesis, Universität Duisburg-Essen, Fakultät für Mathematik, 2014.
- 574. R. Henrion, J. Outrata, and T. Surowiec, Analysis of m-stationary points to an epec modeling oligopolistic competition in an electricity spot market, ESAIM: Control, Optimisation and Calculus of Variations 18 (2012), no. 2, 295–317.
- 575. R. Henrion and T. Surowiec, On calmness conditions in convex bilevel programming., Applicable Analysis **90** (2011), no. 5–6, 951–970.
- 576. J. Herskovits, A. Leontiev, G. Dias, and G. Santos, *Contact shape optimization: a bilevel programming approach*, Int. J. of Struc. and Multidisc. Optim. **20** (2000), 214–221.
- 577. J. Herskovits, M. Tanaka Filho, and A. Leontiev, An interior point technique for solving bilevel programming problems, Optimization and Engineering 14 (2013), no. 3, 381–394.
- 578. M.R. Hesamzadeh and M. Yazdani, *Transmission capacity expansion in imperfectly competitive power markets*, IEEE Transactions on Power Systems **29** (2014), no. 1, 62–71.
- 579. G. Hibino, M. Kainuma, and Y. Matsuoka, *Two-level mathematical programming for analyzing subsidy options to reduce greenhouse-gas emissions*, Tech. Report WP-96-129, IIASA, Laxenburg, Austria, 1996.
- 580. Y.-C. Ho, P.B. Luh, and R. Muralidharan, Information structure, Stackelberg games, and incentive controllability, IEEE Transactions on Automatic Control 26 (1981), no. 2, 454– 460.
- 581. L.T. Hoai An, P.D. Tao, N. Nguyen Canh, and N. Van Thoai, DC programming techniques for solving a class of nonlinear bilevel programs, Journal of Global Optimization 44 (2008), no. 3, 313.

- 582. B. Hobbs and S. Nelson, A nonlinear bilevel model for analysis of electric utility demandside planning issues, Annals of Operations Research 34 (1992), 255–274.
- 583. B.F. Hobbs, C.B. Metzler, and J.-S. Pang, Strategic gaming analysis for electric power systems: An mpec approach, IEEE transactions on power systems 15 (2000), no. 2, 638– 645.
- 584. R. Horst and N.V. Thoai, *Maximizing a concave function over the efficient set or weakly-efficient set*, European Journal of Operational Research **117** (1999), 239–252.
- 585. R. Horst, N.V. Thoai, Y. Yamamoto, and D. Zenke, On optimization over the efficient set in linear multicriteria programming, Journal of optimization theory and applications 134 (2007), no. 3, 433–443.
- 586. S. Hsu and U. Wen, A review of linear bilevel programming problems, Proceedings of the National Science Council, Republic of China, Part A: Physical Science and Engineering, vol. 13, 1989, pp. 53–61.
- 587. C.-F. Hu and F.-B. Liu, Solving mathematical programs with fuzzy equilibrium constraints, Computers & Mathematics with Applications **58** (2009), no. 9, 1844–1851.
- 588. M. Hu and M. Fukushima, Variational inequality formulation of a class of multi-leaderfollower games, Journal of optimization theory and applications **151** (2011), no. 3, 455–473.
- 589. T. Hu, X. Guo, X. Fu, and Y. Lv, A neural network approach for solving linear bilevel programming problem, Knowledge-Based Systems 23 (2010), no. 3, 239–242.
- 590. X. Hu, Mathematical Programs with Complementarity Constraints and Game Theory Models in Electricity Markets, Ph.D. thesis, University of Melbourne, 2002.
- 591. X. Hu and D. Ralph, Using EPECs to model bilevel games in restructured electricity markets with locational prices, Operations Research 55 (2007), no. 5, 809–827.
- 592. Z. Hu, C. Wei, L. Yao, C. Li, and Z. Zeng, *Integrating equality and stability to resolve water allocation issues with a multiobjective bilevel programming model*, Journal of Water Resources Planning and Management (2016), 04016013.
- 593. C. Huang, D. Fang, and Z. Wan, An interactive intuitionistic fuzzy method for multilevel linear programming problems, Wuhan University Journal of Natural Sciences 20 (2015), no. 2, 113–118.
- 594. S. Huck, K.A. Konrad, and W. Müller, *Big fish eat small fish: on merger in Stackelberg markets*, Economics letters **73** (2001), no. 2, 213–217.
- 595. Y. Huo, The upper semi-convergence of optimal solution sets of approximation problems for bilevel stochastic programming, Journal of Systems Science and Mathematical Sciences 34 (2014), 674 – 681, in Chinese.
- 596. M. Inuiguchi and P. Sariddichainunta, Bilevel linear programming with ambiguous objective function of the follower, Fuzzy Optimization and Decision Making 15 (2016), no. 4, 415– 434.
- 597. Y. Ishizuka, Optimality conditions for quasi-differentiable programs with applications to two-level optimization, SIAM Journal on Control and Optimization **26** (1988), 1388–1398.
- 598. Y. Ishizuka and E. Aiyoshi, *Double penalty method for bilevel optimization problems*, Annals of Operations Research **34** (1992), 73–88.
- 599. M.M. Islam, H.K. Singh, and T. Ray, A memetic algorithm for solving bilevel optimization problems with multiple followers, 2016 IEEE Congress on Evolutionary Computation (CEC), 2016, pp. 1901–1908.
- 600. _____, Use of a non-nested formulation to improve search for bilevel optimization, Australasian Joint Conference on Artificial Intelligence, Springer, 2017, pp. 106–118.
- 601. M.M. Islam, H.K. Singh, T. Ray, and A. Sinha, An enhanced memetic algorithm for singleobjective bilevel optimization problems, Evolutionary Computation (2016).
- 602. E. Israeli, System interdiction and defense., Ph.D. thesis, Naval Postgraduate School Monterey, U.S.A., 1999.
- 603. E. Israeli and R.K. Wood, *Shortest-path network interdiction*, Networks **40** (2002), no. 2, 97–111.
- 604. D. Ivanenko and A. Plyasunov, Lower and upper bounds for the bilevel capacitated facility location problem, Tech. report, Sobolev Institute of Mathematics, Novosibirsk, 2003.
- 605. D.S. Ivanenko and A.V. Plyasunov, *Reducibility of bilevel programming problems to vector optimization problems*, Journal of Applied and Industrial Mathematics 2 (2008), no. 2, 179 195.

- 606. S.V. Ivanov, Bilevel stochastic linear programming problems with quantile criterion, Automation and Remote Control **75** (2014), no. 1, 107–118.
- 607. G. Iyengar and W. Kang, *Inverse conic programming with applications*, Operations Research Letters **33** (2005), no. 3, 319–330.
- 608. B. Jabarivelisdeh and S. Waldherr, Optimization of bioprocess productivity based on metabolic-genetic network models with bilevel dynamic programming, Biotechnology and bioengineering 115 (2018), no. 7, 1829–1841.
- 609. M.Z. Jamaludin and C.L.E. Swartz, A bilevel programming formulation for dynamic realtime optimization, IFAC-PapersOnLine 48 (2015), no. 8, 906–911.
- R.-H. Jan and M.-S. Chern, Nonlinear integer bilevel programming, European J. Operational Research 72 (1994), 574–587.
- 611. R.G. Jeroslow, The polynomial hierarchy and a simple model for competitive analysis, Mathematical Programming **32** (1985), 146–164.
- 612. I. Jewitt, Justifying the first-order approach to principal-agent problems, Econometrica: Journal of the Econometric Society (1988), 1177–1190.
- 613. V. Jeyakumar, J.-B. Lasserre, G. Li, and T.S. Pham, Convergent semidefinite programming relaxations for global bilevel polynomial optimization problems, SIAM Journal on Optimization 26 (2016), no. 1, 753–780.
- 614. V. Jeyakumar and G. Li, A bilevel Farkas lemma to characterizing global solutions of a class of bilevel polynomial programs, Operations Research Letters 43 (2015), no. 4, 405–410.
- 615. X. Ji and Z. Shao, Model and algorithm for bilevel newsboy problem with fuzzy demands and discounts, Applied Mathematics and Computation 172 (2006), 163–174.
- 616. F. Jia, F. Yang, and S.-Y. Wang, Sensitivity analysis in bilevel linear programming, Systems Science and Mathematical Sciences 11 (1998), 359–366.
- 617. L. Jia and Z. Li, An ameliorated teaching-learning based optimization algorithm for nonlinear bilevel programming, Computational Intelligence and Security (CIS), 2016 12th International Conference on, IEEE, 2016, pp. 52–56.
- L. Jia, Y. Wang, and L. Fan, Multiobjective bilevel optimization for production-distribution planning problems using hybrid genetic algorithm, Integrated Computer-Aided Engineering 21 (2014), no. 1, 77–90.
- 619. L. Jia, G. Zou, and Z. Li, Target-vector based particle swarm optimization for multiobjective bilevel programming problem, Computational Intelligence and Security (CIS), 2015 11th International Conference on, IEEE, 2015, pp. 295–298.
- 620. M. Jiang, Z. Meng, R. Shen, and X. Xu, A quadratic objective penalty function for bilevel programming, Journal of Systems Science and Complexity 27 (2014), no. 2, 327–337.
- 621. Y. Jiang, X. Li, C. Huang, and X. Wu, Application of particle swarm optimization based on CHKS smoothing function for solving nonlinear bilevel programming problem, Applied Mathematics and Computation 219 (2013), no. 9, 4332 – 4339.
- 622. Y. Jiang, X. Li, C. Huang, and X. Wu, An augmented lagrangian multiplier method based on a chks smoothing function for solving nonlinear bilevel programming problems, Knowledge-Based Systems 55 (2014), 9–14.
- 623. Z. Jiang, J. Yuan, and E. Feng, Robust identification and its properties of nonlinear bilevel multi-stage dynamic system, Applied Mathematics and Computation 219 (2013), no. 12, 6979 - 6985.
- 624. Q. Jin and S. Feng, *Bi-level simulated annealing algorithm for facility location*, Systems Engineering **2** (2007), no. 007.
- 625. S. Jin, R. Fan, G. Wang, and X. Bu, Network utility maximization in wireless networks over fading channels with uncertain distribution, IEEE Communications Letters (2017).
- 626. Y.W. Jing and S.Y. Zhang, The solution to a kind of Stackelberg game system with multifollower: coordinative and incentive, Analysis and Optimization of Systems (Antibes, 1988), Lecture Notes in Control and Information Sciences, vol. 111, Springer-Verlag, Berlin et al., 1988, pp. 593 – 602.
- 627. D. Joksimocic, Dynamic bi-level optimal toll design approach for dynamic traffic networks, Ph.D. thesis, Delft University of Technology, 2007.
- 628. H.Th. Jongen and V. Shikhman, Bilevel optimization: on the structure of the feasible set., Mathematical Programming 136 (2012), 65–90.

- 629. J.M. Jorge, A bilinear algorithm for optimizing a linear function over the efficient set of a multiple objective linear programming problem, Journal of Global Optimization **31** (2005), no. 1, 1–16.
- 630. M. Josefsson and M. Patriksson, Sensitivity analysis of separable traffic equilibrium equilibria with application to bilevel optimization in network design, Transportation Research Part B: Methodological 41 (2007), no. 1, 4–31.
- 631. J. Júdice and A. Faustino, The solution of the linear bilevel programming problem by using the linear complementarity problem, Investigação Operacional 8 (1988), 77–95.
- 632. ____, A sequential LCP method for bilevel linear programming, Annals of Operations Research **34** (1992), 89–106.
- 633. _____, The linear-quadratic bilevel programming problem, INFOR 32 (1994), 87–98.
- 634. J. J. Judice, A. M. Faustino, I. M. Ribeiroa, and A. S. Neves, On the use of bilevel programming for solving a structural optimization problem with discrete variables, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Optimization and its Applications, vol. 2, Springer Science+Business Media, LLC, New York, 2006, pp. 123–142.
- 635. L.A. Julien, A note on Stackelberg competition, Journal of Economics 103 (2011), no. 2, 171–187.
- 636. C. Kahraman, G. Zhang, and J. Lu, Model and approach of fuzzy bilevel decision making for logistics planning problem, Journal of Enterprise Information Management 20 (2007), no. 2, 178–197.
- 637. V. Kalashnikov, F. Camacho, R. Askin, and N. Kalashnykova, Comparison of algorithms for solving a bi-level toll setting problem, International Journal of Innovative Computing, Information and Control 6 (2010), no. 8, 3529–3549.
- 638. V. Kalashnikov, A.E. Cordero, and V. Kalashnikov, *Cournot and Stackelberg equilibrium in mixed duopoly models*, Optimization **59** (2010), no. 5, 689–706.
- 639. V. Kalashnikov, S. Dempe, B. Mordukhovich, and S.V. Kavun, *Bilevel optimal control, equilibrium, and combinatorial problems with applications to engineering*, Mathematical Problems in Engineering **2017** (2017).
- 640. V. Kalashnikov, N. Kalashnykova, and J.G. Flores-Muñiz, Solution of the portfolio optimization model as a fuzzy bilevel programming problem, International Forum for Interdisciplinary Mathematics, Springer, 2015, pp. 164–178.
- 641. V. Kalashnikov, T.I. Matis, J.F. Camacho Vallejo, and S.V. Kavun, *Bilevel programming, equilibrium, and combinatorial problems with applications to engineering*, Mathematical Problems in Engineering (2015), 3 pages.
- 642. V.V. Kalashnikov, Actuality of the portfolio optimization model as a bilevel programming problem, Rezensenty, Proceedings International forum for safety (INFOS-2017) (2017), 211 214.
- 643. V.V. Kalashnikov, S. Dempe, and N.I. Kalashnykova, *Operations research and bilevel programming*, Instituto Tecnológico y de Estudios Superiores de Monterrey, México, 2011, ebook.
- 644. V.V. Kalashnikov, S. Dempe, G.A. Pérez-Valdés, and N.I. Kalashnykova, *Reduction of dimension of the upper level problem in a bilevel programming model part 1*, Intelligent Decision Technologies, Springer, 2011, pp. 255–264.
- 645. _____, Reduction of dimension of the upper level problem in a bilevel programming model part 2, Intelligent Decision Technologies, Springer, 2011, pp. 265–272.
- 646. V.V. Kalashnikov, S. Dempe, G.A. Pérez-Valdés, N.I. Kalashnykova, and J.-F. Camacho-Vallejo, *Bilevel programming and applications*, Mathematical Problems in Engineering **2015** (2015), 16 pages.
- 647. V.V. Kalashnikov and N.I. Kalashnikova, *Solving two-level variational inequality*, Journal of Global Optimization **17** (1991), 289–294.
- 648. V.V. Kalashnikov, N.I. Kalashnykova, and M.A. LEAL-CORONADO, Solution of the portfolio optimization model as a bilevel programming problem, Cherkasy University Bulletin: Economics Sciences (2017), no. 1.
- 649. V.V. Kalashnikov, G.A. Pérez-Valdés, and N.I. Kalashnykova, A linearization approach to solve the natural gas cash-out bilevel problem, Annals of Operations Research 181 (2010), no. 1, 423–442.

- 650. V.V. Kalashnikov, G.A. Pérez-Valdés, A. Tomasgard, and N.I. Kalashnykova, Natural gas cash-out problem: Bilevel stochastic optimization approach, European Journal of Operational Research 206 (2010), no. 1, 18–33.
- 651. V.V. Kalashnikov and R.Z. Ríos-Mercado, An algorithm to solve a gas cash out problem, Proceedings of the International Business and Economic Research Conference (IBERC2002), Puerto Vallarta, Mexico, 2002.
- 652. _____, A penalty-function approach to a mixed-integer bilevel programming problem, Tech. report, Universidad Autónoma de Nuevo León, Mexico, 2002.
- 653. _____, A natural gas cash-out problem: A bilevel programming framework and a penalty function method, Optimization and Engineering 7 (2006), 403–420.
- 654. B.Y. Kara and V. Verter, *Designing a road network for hazardous materials transportation*, Transportation Science **38** (2004), no. 2, 188–196.
- 655. E.G. Kardakos, C.K. Simoglou, and A.G. Bakirtzis, Optimal offering strategy of a virtual power plant: A stochastic bi-level approach, IEEE Transactions on Smart Grid 7 (2016), no. 2, 794–806.
- 656. J.K. Karlof and W. Wang, Bilevel programming applied to the flow shop scheduling problem, Computers & Operations Research 23 (1996), 443–451.
- 657. A. Karoonsoontawong and S.T. Waller, Integrated network capacity expansion and traffic signal optimization problem: robust bi-level dynamic formulation, Networks and Spatial Economics 10 (2010), no. 4, 525–550.
- 658. C. Kasemset and V. Kachitvichyanukul, A pso-based procedure for a bi-level multi-objective toc-based job-shop scheduling problem, International Journal of Operational Research 14 (2012), no. 1, 50–69.
- 659. A.M. Kassa and S.M. Kassa, A branch-and-bound multi-parametric programming approach for non-convex multilevel optimization with polyhedral constraints, Journal of Global Optimization 64 (2016), no. 4, 745–764.
- 660. G.Y. Ke and J.H. Bookbinder, Coordinating the discount policies for retailer, wholesaler, and less-than-truckload carrier under price-sensitive demand: A tri-level optimization approach, International Journal of Production Economics **196** (2018), 82–100.
- 661. M. Khademi, M. Ferrara, M. Salimi, and S. Sharifi, A dynamic Stackelberg game for green supply chain management, arXiv preprint arXiv:1506.06408 (2015).
- 662. A. Kheirkhah, H.-R. Navidi, and M. Messi Bidgoli, A bi-level network interdiction model for solving the hazmat routing problem, International Journal of Production Research 54 (2016), no. 2, 459–471.
- 663. A.I. Kibzun, A.V. Naumov, and S.V. Ivanov, *Bilevel optimization problem for railway* transport hub planning, Upravlenie Bol'shimi Sistemami **38** (2012), 140–160.
- 664. R. Kicsiny, Z. Varga, and A. Scarelli, *Backward induction algorithm for a class of closed*loop Stackelberg games, European Journal of Operational Research 237 (2014), 1021–1036.
- 665. S. Kiener, Die Prinzipal-Agenten-Theorie aus informationsökonomischer Sicht, Physica-Verlag, Heidelberg, 1990.
- 666. T. Kim and S. Suh, Toward developing a national transportation planning model: a bilevel programming approach for Korea, Annals of Regional Science **22** (1988), 65–80.
- 667. G. Kirlik and S. Sayın, Bilevel programming for generating discrete representations in multiobjective optimization, Mathematical Programming **169** (2018), 585 604.
- 668. T. Kis and A. Kovács, *Exact solution approaches for bilevel lot-sizing*, European Journal of Operational Research **226** (2013), no. 2, 237–245.
- 669. K.-P. Kistner and M. Switalski, *Hierarchical production planning: necessity, problems, and methods*, Zeitschrift für Operations Research **33** (1989), 199–212.
- 670. P.-M. Kleniati and C.S. Adjiman, Branch-and-sandwich: a deterministic global optimization algorithm for optimistic bilevel programming problems. I: theoretical development., Journal of Global Optimization 60 (2014), no. 3, 425–458.
- 671. _____, Branch-and-sandwich: a deterministic global optimization algorithm for optimistic bilevel programming problems. Part II: Convergence analysis and numerical results., Journal of Global Optimization **60** (2014), no. 3, 459–481.
- 672. P.-M. Kleniati and C.S. Adjiman, A generalization of the branch-and-sandwich algorithm: From continuous to mixed-integer nonlinear bilevel problems, Computers and Chemical Engineering 72 (2015), 373–386.

- 673. M. Knauer, Fast and save container cranes as bilevel optimal control problems, Mathematical and Computer Modelling of Dynamical Systems **18** (2012), no. 4, 465–486.
- 674. Y. Kochetov, N. Kochetova, and A. Plyasunov, A matheuristic for the leader-follower facility location and design problem, Proceedings of the 10th Metaheuristics International Conference (MIC 2013), vol. 32, Citeseer, 2013.
- 675. Y.A. Kochetov, A.A. Panin, and A.V. Plyasunov, Comparison of metaheuristics for the bilevel facility location and mill pricing problem, Journal of Applied and Industrial Mathematics 9 (2015), no. 3, 392–401.
- 676. Y.A. Kochetov and A.V. Pljasunov, Efficient algorithm for a class of bilevel linear programming problems, Operations Research Proceedings 1996, Springer, 1997, pp. 10–13.
- 677. _____, A polynomially solvable class of two-level linear programming problems, Diskretnyi Analiz i Issledovanie Operatsii 4 (1997), no. 2, 23–33.
- 678. _____, The problem of selecting a number of products with partial exterior financing, Diskretnyi Analiz i Issledovanie Operatsii, Serija 2 9 (2002), no. 2, 78 96, in russian.
- 679. B. Kohli, Variational inequalities and optimistic bilevel programming problem via convexifactors, Topics in Nonconvex Optimization: Theory and Applications (S.K. Mishra, ed.), Springer New York, New York, NY, 2011, pp. 243–255.
- 680. C. Kolstad, A review of the literature on bi-level mathematical programming, Tech. Report LA-10284-MS, US-32, Los Alamos National Laboratory, 1985.
- 681. C. Kolstad and L. Lasdon, Derivative evaluation and computational experience with large bilevel mathematical programs, Journal of Optimization Theory and Applications 65 (1990), 485–499.
- 682. A.F. Kononenko and V.V. Chumakov, Decision making in a two-level hierarchical control system in the presence of exogeneous noncontrollable factors, Avtomat. i Telech. (1988), 92–101, (in Russian).
- 683. D. Konur and M.M. Golias, Analysis of different approaches to cross-dock truck scheduling with truck arrival time uncertainty, Computers & Industrial Engineering 65 (2013), no. 4, 663–672.
- 684. M. Köppe, M. Queyranne, and C.T. Ryan, Parametric integer programming algorithm for bilevel mixed integer programs, Journal of optimization theory and applications 146 (2010), no. 1, 137–150.
- 685. J. Kornaj and T. Liptak, Two-level planning, Econometrica 33 (1965), 141–169.
- 686. S. Kosuch, P. Le Bodic, J. Leung, and A. Lisser, On a stochastic bilevel programming problem, Networks 59 (2012), no. 1, 107–116.
- 687. R.M. Kovacevic and G.Ch. Pflug, *Electricity swing option pricing by stochastic bilevel optimization: a survey and new approaches*, European Journal of Operational Research 237 (2014), no. 2, 389–403.
- 688. A. Kovács, Bilevel programming approach to optimizing a time-variant electricity tariff for demand response, Smart Grid Communications (SmartGridComm), 2016 IEEE International Conference on, IEEE, 2016, pp. 674–679.
- 689. G. Kozanidis, E. Kostarelou, P. Andrianesis, and G. Liberopoulos, Mixed integer parametric bilevel programming for optimal strategic bidding of energy producers in day-ahead electricity markets with indivisibilities, Optimization **62** (2013), no. 8, 1045–1068.
- 690. A. Kristály and S. Nagy, Followers strategy in Stackelberg equilibrium problems on curved strategy sets, Acta Polytechnica Hungarica 10 (2013), no. 7, 69–80.
- 691. H. Küçükaydin, N. Aras, and I.K. Altınel, Competitive facility location problem with attractiveness adjustment of the follower: A bilevel programming model and its solution, European Journal of Operational Research **208** (2011), no. 3, 206–220.
- 692. F.M. Kue, *Mixed integer bilevel programming problems*, Ph.D. thesis, TU Bergakademie Freiberg, 2017.
- 693. A.A. Kulkarni and U.V. Shanbhag, A shared-constraint approach to multi-leader multifollower games, Set-valued and variational analysis **22** (2014), no. 4, 691–720.
- 694. _____, An existence result for hierarchical Stackelberg v/s Stackelberg games, IEEE Transactions on Automatic Control **60** (2015), no. 12, 3379–3384.
- 695. G. Kunapuli, K.P. Bennett, Jing Hu, and Jong-Shi Pang, Classification model selection via bilevel programming, Optim. Methods Softw. 23 (2008), no. 4, 475–489.
- 696. K. Kunisch and T. Pock, A bilevel optimization approach for parameter learning in variational models, SIAM Journal on Imaging Sciences 6 (2013), no. 2, 938–983.

- 697. R.J. Kuo and Y.S. Han, A hybrid of genetic algorithm and particle swarm optimization for solving bi-level linear programming problem-a case study on supply chain model, Applied Mathematical Modelling 35 (2011), no. 8, 3905–3917.
- 698. R.J. Kuo and C.C. Huang, Application of particle swarm optimization algorithm for solving bi-level linear programming problem, Computers & Mathematics with Applications 58 (2009), no. 4, 678–685.
- 699. R.J. Kuo, Y.H. Lee, F.E. Zulvia, and F.C. Tien, Solving bi-level linear programming problem through hybrid of immune genetic algorithm and particle swarm optimization algorithm, Applied Mathematics and Computation 266 (2015), 1013 – 1026.
- 700. M. Labbé, P. Marcotte, and G. Savard, A bilevel model of taxation and its application to optimal highway pricing, Management Science 44 (1998), 1608–1622.
- 701. _____, On a class of bilevel programs, Nonlinear Optimization and Applications (D. di Pillo and F. Gianessi, eds.), vol. 2, Springer, 1998, pp. 1–24.
- 702. M. Labbé and A. Violin, Bilevel programming and price setting problems, 4OR 11 (2013), no. 1, 1–30.
- 703. _____, Bilevel programming and price setting problems, Annals of Operations Research **240** (2016), 141 169.
- 704. K. Lachhwani and A. Dwivedi, Bi-level and multi-level programming problems: Taxonomy of literature review and research issues, Archives of Computational Methods in Engineering (2017), 1–31.
- 705. K. A. P. Lagares, J. S. Angelo, H. S. Bernardino, and H. J. C. Barbosa, A differential evolution algorithm for bilevel problems including linear equality constraints, 2016 IEEE Congress on Evolutionary Computation (CEC), 2016, pp. 1885–1892.
- 706. F. Lagos, F. Ordóñez, and M. Labbé, A branch and price algorithm for a Stackelberg security game, Computers & Industrial Engineering 111 (2017), 216–227.
- 707. Y.-J. Lai, *Hierarchical optimization: a satisfactory solution*, Fuzzy Sets and Systems 77 (1996), 321–335.
- 708. L. Lampariello and S. Sagratella, A bridge between bilevel programs and Nash games, Journal of Optimization Theory and Applications (2017), 1–23.
- 709. _____, Numerically tractable optimistic bilevel problems, Tech. report, Roma Tre University, Department of Business Studies, 2017.
- 710. K.-M. Lan, U.-P. Wen, H.-S. Shih, and E.S. Lee, A hybrid neural network approach to bilevel programming problems, Applied Mathematics Letters 20 (2007), no. 8, 880–884.
- 711. Y. Lan, R. Zhao, and W. Tang, A bilevel fuzzy principal-agent model for optimal nonlinear taxation problems, Fuzzy Optimization and Decision Making 10 (2011), 211232.
- 712. M.-T. Laraba, M. Hovd, S. Olaru, and S.-I. Niculescu, A bilevel optimization approach for D-invariant set design, IFAC-PapersOnLine 49 (2016), no. 10, 235 – 240, 13th IFAC Workshop on Time Delay Systems TDS 2016.
- 713. H. Laux and H.Y. Schenk-Mathes, *Lineare und nichtlineare anreizsysteme*, Physica-Verlag, 1992.
- 714. D. Lavigne, R. Loulou, and G. Savard, Pure competition, regulated and Stackelberg equilibria: Application to the energy system of Quebec, European Journal of Operational Research 125 (200), 1–17.
- 715. S.M. Lavlinskii, A.A. Panin, and A.V. Plyasunov, A bilevel planning model for publicprivate partnership, Automation and Remote Control 76 (2015), no. 11, 1976–1987.
- 716. S. Lawphongpanich and D. W. Hearn, An MPEC approach to second-best toll pricing, Mathematical Programming 101 (2004), 33–55.
- 717. L. LeBlanc and D. Boyce, A bilevel programming algorithm for exact solution of the network design problem with user-optimal flows, Transportation Research **20** B (1986), 259–265.
- 718. E.S. Lee, Fuzzy multiple level programming, Applied Mathematics and Computation 120 (2001), no. 13, 79 – 90, The Bellman Continuum.
- 719. L. Lei and Y. Wei, Research of leader-follower problem to tradable emission permits, Management Science and Engineering, 2007. ICMSE 2007. International Conference on, IEEE, 2007, pp. 2184–2189.
- 720. M. Lei, J. Zhang, X. Dong, and J.J. Ye, Modeling the bids of wind power producers in the day-ahead market with stochastic market clearing, Sustainable Energy Technologies and Assessments 16 (2016), 151 – 161.

- 721. G. Leitman, On generalized Stackelberg strategies, Journal of Optimization Theory and Applications 26 (1978), 637 – 643.
- 722. J.M. Leleno and H.D. Sherali, A leader-follower model and analysis for a two-stage network of oligopolies, Annals of Operations Research **34** (1992), 37–72.
- 723. A. Leontiev and J. Herskovits, An interior point technique for solving bilevel programming problems, Optimization and Engineering 14 (2013), 381 394.
- 724. E.S. Levitin, Optimization problems with extremal constraints ii: Description as mathematical problem of systems analysis, Avtomatika i Telemekhanika 12 (1995), 16 – 31, (in Russian).
- 725. _____, Optimization problems with extremal constraints. Part I: General concepts, formulation, and main problems, Avtomatika i Telemekhanika **12** (1995), 1 – 15, (in Russian).
- 726. ____, Two-stage models of optimization, Matematiceskoje Modelirovanie 8 (1996), 45–54, (in Russian).
- 727. S. Leyffer and T. Munson, Solving multi-leader-common-follower games, Optimisation Methods & Software 25 (2010), no. 4, 601–623.
- 728. C. Li and L. Guo, A single-level reformulation of mixed integer bilevel programming problems, Operations Research Letters 45 (2017), no. 1, 1–5.
- 729. D. Li and J.B. Cruz, Information, decision-making and deception in games, Decision Support Systems 47 (2009), no. 4, 518–527.
- 730. G. Li, Z. Wan, J.-W. Chen, and X. Zhao, *Existence of solution and algorithms for a class of bilevel variational inequalities with hierarchical nesting structure*, Fixed Point Theory and Applications **2016** (2016), no. 1, 41.
- 731. H. Li, A genetic algorithm using a finite search space for solving nonlinear/linear fractional bilevel programming problems, Annals of Operations Research **235** (2015), no. 1, 543–558.
- 732. H. Li and L. Fang, An evolutionary algorithm for solving bilevel programming problems using duality conditions, Mathematical Problems in Engineering **2012** (2012).
- 733. H. Li and Y. Wang, A hybrid genetic algorithm for solving nonlinear bilevel programming problems based on the simplex method, Third International Conference on Natural Computation., vol. 4, IEEE, 2007, pp. 91–95.
- 734. _____, Exponential distribution-based genetic algorithm for solving mixed-integer bilevel programming problems, Journal of Systems Engineering and Electronics **19** (2008), no. 6, 1157–1164.
- 735. H. Li, Q. Zhang, Q. Chen, L. Zhang, and Y.-C. Jiao, Multiobjective differential evolution algorithm based on decomposition for a type of multiobjective bilevel programming problems, Knowledge-Based Systems 107 (2016), 271–288.
- 736. _____, Multiobjective differential evolution algorithm based on decomposition for a type of multiobjective bilevel programming problems, Knowledge-Based Systems 107 (2016), 271–288.
- 737. M. Li, D. Lin, and S. Wang, Solving a type of biobjective bilevel programming problem using NSGA-II., Comput. Math. Appl. 59 (2010), no. 2, 706–715.
- 738. X. Li, P. Tian, and X. Min, A hierarchical particle swarm optimization for solving bilevel programming problems, ICAISC 2006 (L. Rutkowski, ed.), Lect. Notes Artific. Intell., vol. 4029, Springer Verlag, Berlin, Heidelberg, 2006, pp. 1169–1178.
- 739. X.-Y. Li, X.-M. Li, X.-W. Li, and H.-T. Qiu, Multi-agent fare optimization model of two modes problem and its analysis based on edge of chaos, Physica A: Statistical Mechanics and its Applications 469 (2017), 405–419.
- 740. Z. Li, W. Shen, J. Xu, and B. Lev, Bilevel and multi-objective dynamic construction site layout and security planning, Automation in Construction 57 (2015), 1–16.
- 741. M.B. Lignola and J. Morgan, Topological existence and stability for Stackelberg problems, Journal of Optimization Theory and Applications 84 (1995), 145–169.
- 742. _____, Stability of regularized bilevel programming problems, Journal of Optimization Theory and Applications **93** (1997), 575–596.
- 743. _____, Existence of solutions to generalized bilevel programming problem, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 315–332.
- 744. _____, Well-posedness for optimization problems with constraints defined by variational inequalities having a unique solution, Journal of Global Optimization **16** (2000), 57–67.

- 745. _____, Existence for optimization problems with equilibrium constraints in reflexive Banach spaces, Optimization in Economics, Finance and Industry, Datanova, Milano 2002, 2002, pp. 15–36.
- 746. _____, Existence of solutions to bilevel variational problems in Banach spaces, Equilibrium Problems: Nonsmooth Optimization and Variational Inequality Models (F. Giannessi, A. Maugeri, and P.M. Pardalos, eds.), Kluwer Academic Publishers, Dordrecht et al., 2002.
- 747. M.B. Lignola and J. Morgan, Asymptotic behavior of semi-quasivariational optimistic bilevel problems in banach spaces, Journal of Mathematical Analysis and Applications 424 (2015), no. 1, 1–20.
- 748. _____, Inner regularizations and viscosity solutions for pessimistic bilevel optimization problems, Journal of Optimization Theory and Applications **173** (2017), 183 202.
- 749. C. Lim and J. C. Smith, Algorithms for discrete and continuous multicommodity flow network interdiction problems, IIE Transactions **39** (2007), no. 1, 15–26.
- 750. P. Limleamthong and G. Guilln-Goslbez, Rigorous analysis of pareto fronts in sustainability studies based on bilevel optimization: Application to the redesign of the uk electricity mix, Journal of Cleaner Production 164 (2017), 1602 – 1613.
- 751. D.-Y. Lin, A. Karoonsoontawong, and S.T. Waller, A Dantzig-Wolfe decomposition based heuristic scheme for bi-level dynamic network design problem, Networks and Spatial Economics 11 (2011), no. 1, 101–126.
- 752. G.-H. Lin, M. Xu, and J.J. Ye, On solving simple bilevel programs with a nonconvex lower level program, Mathematical Programming 144 (2014), no. 1-2, 277–305.
- 753. L.-J. Lin and H.J. Shie, Existence theorems of quasivariational inclusion problems with applications to bilevel problems and mathematical programs with equilibrium constraint, Journal of Optimization Theory and Applications **138** (2008), no. 3, 445–457.
- 754. L.J. Lin, Existence theorems for bilevel problem with applications to mathematical program with equilibrium constraint and semi-infinite problem, Journal of Optimization Theory and Applications 137 (2008), no. 1, 27–40.
- 755. M. Linnala, E. Madetoja, H. Ruotsalainen, and J. Hämäläinen, *Bi-level optimization for a dynamic multiobjective problem*, Engineering Optimization **44** (2012), no. 2, 195–207.
- 756. Y.-C. Liou, S. Schaible, and J.-C. Yao, Supply chain inventory management via a stackelberg equilibrium, Journal of Industrial & Management Optimization 2 (2006), no. 1, 81–94.
- 757. Y.-C. Liou, S.-Y. Wu, and J.-C. Yao, Bilevel decision with generalized semi-infinite optimization for fuzzy mappings as lower level problems, Fuzzy Optimization and Decision Making 4 (2005), 41–50.
- 758. Y.-C. Liou and J.-C. Yao, *Bilevel decision via variational inequalities*, Computers & Mathematics with Applications **49** (2005), no. 7, 1243 1253.
- 759. B. Liu, Stackelberg-Nash equilibrium for multilevel programming with multiple followers using genetic algorithms, Computers & Mathematics with Applications 36 (1998), no. 7, 79–89.
- 760. B. Liu, Z. Wan, J. Chen, and G. Wang, *Optimality conditions for pessimistic semivectorial bilevel programming problems*, Journal of Inequalities and Applications **41** (2014), 26 pages.
- 761. G. Liu and J. Han, Optimality conditions for nonconvex bilevel programming problems, Systems Science and Mathematical Sciences 10 (1997), 183–192.
- 762. G. Liu, J. Han, and S. Wang, A trust region algorithm for bilevel programming problems, Chinese Science Bulletin 43 (1998), 820–824.
- 763. G.-s. Liu, S.-q. Xu, and J.-y. Han, A trust region algorithm for solving bilevel programming problems, Acta Mathematicae Applicatae Sinica, English Series **29** (2013), no. 3, 491–498.
- 764. G.S. Liu, J.Y. Han, and J.Z. Zhang, Exact penalty functions for convex bilevel programming problems, Journal of Optimization Theory and Applications 110 (2001), 621–643.
- 765. J. Liu, T. Zhang, Y.-X. Fan, B. Han, and Y. Zheng, An objective penalty method for optimistic bilevel programming problems, Journal of the Operations Research Society of China (2018).
- 766. W. Liu and K.-Y. Zheng, Z.and Cai, Bi-level programming based real-time path planning for unmanned aerial vehicles, Knowledge-Based Systems 44 (2013), 34–47.
- 767. X. Liu, G. Du, and R.J. Jiao, Bilevel joint optimisation for product family architecting considering make-or-buy decisions, International Journal of Production Research 55 (2017), no. 20, 5916–5941.

- 768. Y. Liu, H. Xu, S.-J.S. Yang, and J. Zhang, Distributionally robust equilibrium for continuous games: Nash and Stackelberg models, European Journal of Operational Research 265 (2018), no. 2, 631 – 643.
- 769. Y.-H. Liu and S.M. Hart, Characterizing an optimal solution to the linear bilevel programming problem, European Journal of Operational Research 73 (1994), 164–166.
- 770. Y.-H. Liu and T.H. Spencer, Solving a bilevel linear program when the inner decision maker controls few variables, European Journal on Operational Research 81 (1995), 644–651.
- 771. Z. Liu and M. Ehrgott, Primal and dual algorithms for optimization over the efficient set, Optimization (2018), 1–26, electronic first publication.
- 772. A. Lodi, T.K. Ralphs, and G.J. Woeginger, Bilevel programming and the separation problem, Mathematical Programming 146 (2014), no. 1-2, 437–458.
- 773. S. Lohse, *Eine spezielle klasse von zwei-ebenen-optimierungsaufgaben*, Ph.D. thesis, TU Bergakademie Freiberg, 2011.
- 774. G. Londono and A. Lozano, A bilevel optimization program with equilibrium constraints for an urban network dependent on time, Transportation Research Procedia 3 (2014), 905–914.
- 775. J.M. López-Lezama, J. Cortina-Gómez, and N. Muñoz-Galeano, Assessment of the electric grid interdiction problem using a nonlinear modeling approach, Electric Power Systems Research 144 (2017), 243–254.
- 776. P. Loridan and J. Morgan, Approximate solutions for two-level optimization problems, Trends in Mathematical Optimization (K. Hoffman, J. Hiriart-Urruty, C. Lemarechal and J. Zowe, ed.), International Series of Numerical Mathematics, vol. 84, Birkhäuser Verlag, Basel, 1988, pp. 181–196.
- 777. ____, A sequential stability result for constrained Stackelberg problems, Richerche di Matematica **38** (1989), 19–32.
- 778. _____, A theoretical approximation scheme for Stackelberg problems, Journal of Optimization Theory and Applications **61** (1989), 95–110.
- 779. _____, New results on approximate solutions in two-level optimization, Optimization **20** (1989), 819–836.
- 780. _____, ε-regularized two-level optimization problems: approximation and existence results, Optimization – Fifth French-German Conference (Varez), Lecture Notes in Mathematics, Springer Verlag, Berlin, Nov. 1405, 1989, pp. 99–113.
- 781. _____, Quasi convex lower level problem and applications in two level optimization, Lecture Notes in Economics and Mathematical Systems, vol. 345, pp. 325–341, Springer-Verlag, Berlin, 1990.
- 782. _____, Regularization for two-level optimization problems, Advances in Optimization. Proceedings of the 6th French-German Conference on Optimization, Lambrecht, Springer Verlag, Berlin, 1991, pp. 239–255.
- 783. _____, Least-norm regularization for weak two-level optimization problems, Optimization, Optimal Control and Partial Differential Equations, International Series of Numerical Mathematics, vol. 107, Birkhäuser Verlag, Basel, 1992, pp. 307–318.
- 784. _____, On strict ε-solutions for a two-level optimization problem, Proceedings of the International Conference on Operations Research 90, Springer Verlag, Berlin, 1992, pp. 165– 172.
- 785. _____, Weak via strong Stackelberg problem: New results, Journal of Global Optimization 8 (1996), 263–287.
- 786. L. Lozano and J. Cole Smith, A value-function-based exact approach for the bilevel mixedinteger programming problem, Operations Research 65 (2017), no. 3, 768–786.
- 787. J. Lu, J. Han, Y. Hu, and G. Zhang, Multilevel decision-making: A survey, Information Sciences 346 - 347 (2016), 463–487.
- 788. J. Lu, C. Shi, and G. Zhang, On bilevel multi-follower decision making: General framework and solutions, Information Sciences 176 (2006), no. 11, 1607–1627.
- 789. J. Lu, C. Shi, G. Zhang, and T. Dillon, Model and extended Kuhn-Tucker approach for bilevel multi-follower decision making in a referential-uncooperative situation, Journal of Global Optimization 38 (2007), no. 4, 597–608.
- 790. J. Lu, C. Shi, G. Zhang, and D. Ruan, An extended branch and bound algorithm for bilevel multi-follower decision making in a referential-uncooperative situation, International Journal of Information Technology & Decision Making 6 (2007), no. 02, 371–388.

- 791. J. Lu, G. Zhang, J. Montero, and L. Garmendia, Multifollower trilevel decision making models and system, Industrial Informatics, IEEE Transactions on 8 (2012), no. 4, 974–985.
- 792. Y.-B. Lü and Z.-P. Wan, A smoothing method for solving bilevel multiobjective programming problems, Journal of the Operations Research Society of China 2 (2014), no. 4, 511–525.
- 793. Y.-B. Lü, Z.-P. Wan, and X.-N. Guo, Bilevel model of emission permits market trading, Xitong Gongcheng Lilun yu Shijian/System Engineering Theory and Practice 34 (2014), no. 2, 343–348.
- 794. Z. Lu, K. Deb, and A. Sinha, Finding reliable solutions in bilevel optimization problems under uncertainties, Proceedings of the 2016 on Genetic and Evolutionary Computation Conference, ACM, 2016, pp. 941–948.
- 795. R. Lucchetti, F. Mignanego, and G. Pieri, *Existence theorem of equilibrium points in Stack-elberg games with constraints*, Optimization **18** (1987), 857–866.
- 796. P.B. Luh, T.-S. Chang, and T. Ning, *Three-level Stackelberg decision problems*, IEEE Transactions on Automatic Control AC-29 (1984), 280 – 282.
- 797. _____, Pricing problems with a continuum of customers as stochastic Stackelberg games, Journal of Optimization Theory and Applications **55** (1987), 119–131.
- 798. Z. Lukač, K. Šorić, and V.V. Rosenzweig, Production planning problem with sequence dependent setups as a bilevel programming problem, European Journal of Operational Research 187 (2008), no. 3, 1504–1512.
- 799. Z.-Q. Luo, J.-S. Pang, and D. Ralph, *Mathematical programs with equilibrium constraints*, Cambridge University Press, Cambridge, 1996.
- 800. T. Lv, Q. Ai, and Y. Zhao, A bi-level multi-objective optimal operation of grid-connected microgrids, Electric Power Systems Research 131 (2016), 60–70.
- 801. Y. Lv and J. Chen, A discretization iteration approach for solving a class of semivectorial bilevel programming problem, Journal of Nonlinear Science and Applications 9 (2016), no. 5, 2888 – 2899.
- 802. Y. Lv, Z. Chen, and Z. Wan, A neural network for solving a convex quadratic bilevel programming problem, Journal of computational and applied mathematics 234 (2010), no. 2, 505–511.
- 803. Y. Lv, T. Hu, and Z. Wan, A penalty function method for solving weak price control problem, Applied Mathematics and Computation **186** (2007), no. 2, 1520 – 1525.
- 804. Y. Lv, T. Hu, G. Wang, and Z. Wan, A penalty function method based on Kuhn-Tucker condition for solving linear bilevel programming, Applied Mathematics and Computation 188 (2007), 808–813.
- 805. Y. Lv, T. Hu, G. Wang, and Z. Wan, A neural network approach for solving nonlinear bilevel programming problem, Computers & Mathematics with Applications 55 (2008), no. 12, 2823–2829.
- 806. Y. Lv and Z. Wan, A solution method for the optimistic linear semivectorial bilevel optimization problem, Journal of Inequalities and Applications 2014 (2014), no. 1, 164.
- 807. _____, Solving linear bilevel multiobjective programming problem via exact penalty function approach, Journal of Inequalities and Applications **2015** (2015), no. 1, 258.
- 808. _____, Linear bilevel multiobjective optimization problem: Penalty approach, Journal of Industrial & Management Optimization (2018), 484–495.
- 809. W. Ma, M. Wang, and X. Zhu, Improved particle swarm optimization based approach for bilevel programming problem-an application on supply chain model, International Journal of Machine Learning and Cybernetics 5 (2014), no. 2, 281–292.
- 810. Y. Ma, F. Yan, K. Kang, and X. Wei, A novel integrated production-distribution planning model with conflict and coordination in a supply chain network, Knowledge-Based Systems 105 (2016), 119–133.
- 811. C.M. Macal and A.P. Hurter, Dependence of bilevel mathematical programs on irrelevant constraints, Computers & Operations Research 24 (1997), 1129–1140.
- 812. G. Mahapatra and S. Banerjee, *Bilevel optimization using firefly algorithm*, Proceedings of the 1st International Science & Technology Congress (2014).
- 813. C. Makasu, A bilevel programming approach to double optimal stopping, Applied Mathematics and Computation 238 (2014), 393 396.
- 814. S. Maldonado-Pinto, M.-S. Casas-Ramírez, and J.-F. Camacho-Vallejo, Analyzing the performance of a hybrid heuristic for solving a bilevel location problem under different approaches to tackle the lower level, Mathematical Problems in Engineering **2016** (2016).

- 815. N. Malhotra and S.R. Arora, *Optimality conditions for linear fractional bilevel programs*, Indian journal of pure and applied mathematics **30** (1999), 373–384.
- 816. _____, Optimality conditions and an algorithm for linear-quadratic bilevel programming, Management Science and Financial Engineering 7 (2001), no. 1, 41–56.
- 817. L. Mallozzi and A.P. di Napoli, Optimal transport and a bilevel location-allocation problem, Journal of Global Optimization (2015), 1–15.
- 818. L. Mallozzi and J. Morgan, ε-mixed strategies for static continuous-kernel Stackelberg problems, Journal of Optimization Theory and Applications 78 (1993), 303–316.
- 819. ____, Weak Stackelberg problem and mixed solutions under data perturbations, Optimization **32** (1995), 269–290.
- 820. _____, On approximate mixed Nash equilibria and average marginal functions for a twostage three-players games, Optimization with Multivalued Mappings: Theory, Applications and Algorithms (S. Dempe and V. Kalashnikov, eds.), Optimization and its Applications, vol. 2, Springer Science+Business Media, LLC, New York, 2006, pp. 97–107.
- 821. Anton V Malyshev and Alexander S Strekalovsky, On global search for pessimistic solution in bilevel problems (*i* special issue; bilevel programming, optimization methods, and applications to economics), International Journal of Biomedical Soft Computing and Human Sciences: the official journal of the Biomedical Fuzzy Systems Association 18 (2013), no. 1, 57–61.
- 822. A.V. Malyshev and A.S. Strekalovsky, *Global search for pessimistic solution in bilevel problems*, Proceedings of the Toulouse global optimization workshop, 2010, pp. 77–80.
- 823. _____, Global search for guaranteed solutions in quadratic-linear bilevel optimization problems, Izvestiya Irkutskogo Gosudarstvennogo Universiteta. Seriya" Matematika" 4 (2011), no. 1, 73–82.
- O.L. Mangasarian, Misclassification minimization, Journal of Global Optimization 5 (1994), 309–323.
- 825. _____, Regularized linear programs with equilibrium constraints, Reformulation Nonsmooth, Piecewise Smooth, Semismooth and Smoothing Methods (M. Fukushima and L. Qi, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 259–268.
- 826. O.L. Mangasarian and J.-S. Pang, Exact penalty functions for mathematical programs with linear complemantarity constraints, Optimization 42 (1997), 1–8.
- 827. P. Marcotte, Network optimization with continuous control parameters, Transportation Science 17 (1983), 181–197.
- 828. ____, Network design problem with congestion effects: a case of bilevel programming, Mathematical Programming **34** (1986), 142–162.
- 829. ____, A note on a bilevel programming algorithm by LeBlanc and Boyce, Transportation Research **22** B (1988), 233–237.
- 830. P. Marcotte and G. Marquis, *Efficient implementation of heuristics for the continuous network design problem*, Annals of Operations Research **34** (1992), 163–176.
- 831. P. Marcotte, A. Mercier, G. Savard, and V. Verter, *Toll policies for mitigating hazardous materials transport risk*, Transportation Sci. **43** (2009), no. 2, 228–243.
- 832. P. Marcotte and G. Savard, A note on the Pareto optimality of solutions to the linear bilevel programming problem, Computers & Operations Research 18 (1991), 355–359.
- 833. ____, Novel approaches to the discrimination problem, Zeitschrift für Operations Research **36** (1992), 517–545.
- 834. _____, Bilevel programming: Applications, Encyclopedia of Optimization, Kluwer Academic Publishers, Dordrecht, 2001.
- 835. _____, Bilevel programming: a combinatorial perspective, Graph Theory and Combinatorial Optimization, GERAD 25th Anniv.Ser., no. 8, Springer, New York, 2005, pp. 191–217.
- 836. P. Marcotte, G. Savard, and D. Zhu, *Mathematical structure of a bilevel strategic pricing* model, European Journal of Operational Research **193** (2009), no. 2, 552–566.
- 837. P. Marcotte, G. Savard, and D.L. Zhu, A trust region algorithm for nonlinear bilevel programming, Operations Research Letters **29** (2001), 171–179.
- 838. P. Marcotte and D.L. Zhu, Exact and inexact penalty methods for the generalized bilevel programming problem, Mathematical Programming 74 (1996), 141–157.
- 839. V. Marianov and D. Serra, *Hierarchical location-allocation models for congested systems*, European Journal of Operational Research 135 (2001), no. 1, 195–208.

54

- 840. Y. Marinakis, A. Migdalas, and P.M. Pardalos, A new bilevel formulation for the vehicle routing problem and a solution method using a genetic algorithm, Journal of Global Optimization **38** (2007), no. 4, 555–580.
- 841. R. Mathieu, L. Pittard, and G. Anandalingam, Genetic algorithm based approach to bi-level linear programming, Recherche opérationelle/Operations Research 28 (1994), 1–21.
- 842. R. Mathieu, L. Pittard, and G. Anandalingam, Genetic algorithm based approach to bi-level linear programming., RAIRO. Recherche opérationnelle 28 (1994), 1 – 21.
- 843. K. Mathur and M.C. Puri, A bilevel linear programming problem with bottleneck objectives, Opsearch **31** (1994), 177–201.
- 844. ____, A bilevel bottleneck programming problem, European Journal of Operational Research 86 (1995), 337–344.
- 845. A. Maugeri and L. Scrimali, A new approach to solve convex infinite-dimensional bilevel problems: Application to the pollution emission price problem, Journal of Optimization Theory and Applications 169 (2016), no. 2, 370–387.
- 846. P. Mehlitz, Bilevel programming problems with simple convex lower level, Optimization 65 (2016), no. 6, 1203–1227.
- 847. _____, Contributions to complementarity and bilevel programming in Banach spaces, Ph.D. thesis, TU Bergakademie Freiberg, 2017.
- 848. P. Mehlitz and G. Wachsmuth, Weak and strong stationarity in generalized bilevel programming and bilevel optimal control, Optimization 65 (2016), no. 5, 907–935.
- 849. R. Menasri, A. Nakib, B. Daachi, H. Oulhadj, and P. Siarry, A trajectory planning of redundant manipulators based on bilevel optimization, Applied Mathematics and Computation 250 (2015), 934 – 947.
- 850. Z. Meng, C. Dang, R. Shen, and M. Jiang, An objective penalty function of bilevel programming, Journal of Optimization Theory and Applications **153** (2012), no. 2, 377–387.
- 851. A.G. Mersha, Solution methods for bilevel programming problems, Ph.D. thesis, TU Bergakademie Freiberg, 2008.
- 852. A.G. Mersha and S. Dempe, Linear bilevel programming with upper level constraints depending on the lower level solution, Applied Mathematics and Computation 180 (2006), no. 1, 247 - 254.
- 853. _____, Direct search algorithm for bilevel programming problems., Computational Optimization and Applications 49 (2011), no. 1, 1–15.
- 854. ____, Feasible direction method for bilevel programming problem., Optimization **61** (2012), no. 4–6, 597–616.
- 855. M. Mesanovic, D. Macko, and Y. Takahara, *Theory of hierarchical, multilevel systems*, Academic Press, New York and London, 1970.
- 856. B. Metev, Multiobjective optimization methods help to minimize a function over the efficient set, CYBERNETICS AND INFORMATION TECHNOLOGIES 7 (2007), no. 2.
- 857. C. Miao, G. Du, R.J. Jiao, and T. Zhang, Coordinated optimisation of platform-driven product line planning by bilevel programming, International Journal of Production Research 55 (2017), no. 13, 3808–3831.
- 858. A. Migdalas, Bilevel programming in traffic planning: Models, methods and challenge, Journal of Global Optimization 7 (1995), 381–405.
- 859. _____, When is Stackelberg equilibrium Pareto optimum?, Advances in Multicriteria Analysis (P. Pardalos et al., ed.), Kluwer Academic Publishers, Dordrecht, 1995.
- 860. A. Migdalas and P. Pardalos, *Editorial: Hierarchical and bilevel programming*, Journal of Global Optimization 8 (1996), 209–215.
- 861. A. Migdalas, P.M. Pardalos, and P. Värbrand (eds.), *Multilevel optimization: Algorithms and applications*, Kluwer Academic Publishers, Dordrecht, 1998.
- 862. F. Mignanego and A. Sciomachen, Incentive strategies with threats in dynamic constrained-Stackelberg problems. a bilevel programming approach, Optimization **38** (1996), 263–276.
- 863. T. Miller, T. Friesz, and R. Tobin, *Heuristic algorithms for delivered price spatially competitive network facility location problems*, Annals of Operations Research **34** (1992), 177–202.
- 864. T.C. Miller, R.L. Tobin, and T.L. Friesz, Stackelberg games on a network with Cournot-Nash oligopolistic competitors, Journal of Regional Science 31 (1991), no. 4, 435–454.
- 865. M. Miralinaghi, Y. Lou, B.B. Keskin, Y.-T. Hsu, and R. Shabanpour, Hydrogen refueling station location problem with traffic deviation considering route choice and demand uncertainty, International Journal of Hydrogen Energy 42 (2017), 3335 – 3351.

- 866. S. A. MirHassani, S. Raeisi, and A. Rahmani, Quantum binary particle swarm optimizationbased algorithm for solving a class of bi-level competitive facility location problems, Optimization Methods and Software **30** (2015), no. 4, 756–768.
- 867. J.A. Mirrlees, The theory of moral hazard and unobservable bevaviour: part I, Review of Economic Studies 66 (1999), 3–21.
- 868. S. Mishra, Weighting method for bi-level linear fractional programming problems, European Journal of Operational Research 183 (2007), no. 1, 296–302.
- 869. S. Mishra and A. Ghosh, Interactive fuzzy programming approach to bi-level quadratic fractional programming problems, Annals of Operations Research **143** (2006), 251–263.
- 870. A. Mitsos, *Global solution of bilevel mixed-integer nonlinear programs*, The 2008 Annual Meeting Computing and Systems Technology Division, Philadelphia, 2008, 2008.
- 871. _____, Global solution of nonlinear mixed-integer bilevel programs, Journal of Global Optimization 47 (2010), no. 4, 557–582.
- 872. A. Mitsos and P.I. Barton, A test set for bilevel programs, Tech. report, Massachusetts Institute of Technology, 2006.
- 873. A. Mitsos, G.M. Bollas, and P.I. Barton, Bilevel optimization formulation for parameter estimation in liquid?liquid phase equilibrium problems, Chemical Engineering Science 64 (2009), no. 3, 548 – 559.
- 874. A. Mitsos, B. Chachuat, and P. I. Barton, *Towards global bilevel dynamic optimization.*, Journal of Global Optimization **45** (2009), no. 1, 63–93.
- 875. A. Mitsos, P. Lemonidis, and P. I. Barton, *Global solution of bilevel programs with a non*convex inner program., Journal of Global Optimization **42** (2008), no. 4, 475–513 (English).
- 876. K. Mizukami and H. Xu, Closed-loop Stackelberg strategies for linear-quadratic descriptor systems, Journal of Optimization Theory and Applications 74 (1992), 151–170.
- 877. K. Mombaur, A. Truong, and J.-P. Laumond, From human to humanoid locomotion an inverse optimal control approach, Autonomous robots 28 (2010), no. 3, 369–383.
- 878. G.M. Moore, *Bilevel programming algorithms for machine learning model selection*, Ph.D. thesis, Rensselaer Polytechnic Institute Troy, NY, USA, 2010.
- 879. J. Moore, *Extensions to the multilevel linear programming problem*, Ph.D. thesis, Department of Mechanical Engineering, University of Texas, Austin, 1988.
- 880. J. Moore and J.F. Bard, *The mixed integer linear bilevel programming problem*, Operations Research **38** (1990), 911–921.
- 881. M. Moraal, Stackelberg solutions in linear programming problems, 6. Symposium on Operations Research, Univ. Augsburg, 1981, Part II, Methods of Operations Research, 1983, pp. 375 383.
- 882. B.S. Mordukhovich, Variational analysis and generalized differentiation I: Basic theory, Springer, 2006.
- 883. ____, Variational analysis and generalized differentiation, vol. 2: Applications, Springer Verlag, Berlin et al., 2006.
- 884. B.S. Mordukhovich, N.M. Nam, and H.M. Phan, Variational analysis of marginal functions with applications to bilevel programming, Journal of Optimization Theory and Applications 152 (2012), no. 3, 557–586.
- 885. B.S. Mordukhovich and J.V. Outrata, Coderivative analysis of quasi-variational inequalities with applications to stability and optimization, SIAM Journal on Optimization 18 (2007), no. 2, 389–412.
- 886. J. Morgan, Constrained well-posed two-level optimization problems, Nonsmooth Optimization and Related Topics (F.H. Clarke et al., ed.), Plenum Press, New York, 1989, pp. 307– 325.
- 887. J. Morgan and P. Loridan, Approximation of the Stackelberg problem and applications in control theory, Control application of nonlinear programming and optimization: Proceedings of the Fifth IFAC Workshop, Capri, Italy 11 14 June (G. Di Pillo, ed.), 1985, pp. 121–124.
- 888. K. Moshirvaziri, M.A. Amouzegar, and S. E. Jacobsen, *Test problem construction for linear bilevel programming problems.*, Journal of Global Optimization **8** (1996), no. 3, 235–243.
- 889. A. Moudafi, *Proximal methods for a class of bilevel monotone equilibrium problems*, Journal of Global Optimization **47** (2010), no. 2, 287–292.

- 890. R.E. Msigwa, Y. Lu, Y. Ge, and L. Zhang, A smoothing approach for solving transportation problem with road toll pricing and capacity expansions, Journal of Inequalities and Applications 2015 (2015), 237.
- 891. A. Mukherjee and L. Zhao, *Profit raising entry*, Journal of Industrial Economics 57 (2009), no. 4, 870.
- 892. L.D. Muu, On the construction of initial polyhedral convex set for optimization problems over the efficient set and bilevel linear programs, Vietnam Journal of Mathematics 28 (2000), 177–182.
- L.D. Muu and W. Oettli, Optimization over equilibrium sets, Optimization 49 (2001), 179– 189.
- 894. L.D. Muu and N.V. Quy, A global optimization method for solving convex quadratic bilevel programming problems, Journal of Global Optimization **26** (2003), 199–219.
- 895. S. Nagy, Stackelberg equilibria via variational inequalities and projections, Journal of Global Optimization 57 (2013), no. 3, 821–828.
- 896. J. Naoum-Sawaya and S. Elhedhli, Controlled predatory pricing in a multiperiod Stackelberg game: an MPEC approach, Journal of Global Optimization 50 (2011), no. 2, 345–362.
- 897. S. Narula and A. Nwosu, A dynamic programming solution for the hierarchical linear programming problem, Tech. Report 37–82, Department of Operations Research and Statistics, Rensselaer Polytechnic Institute, 1982.
- 898. _____, Two-level hierarchical programming problems, Essays and surveys on multiple criteria decision making (P. Hansen, ed.), Springer-Verlag, Berlin, 1983, pp. 290–299.
- 899. _____, An algorithm to solve a two-level resource control pre-emptive hierarchical programming problem, Mathematics of multiple-objective programming (P. Serafini, ed.), Springer-Verlag, Berlin, 1985.
- 900. _____, Two-level resource control pre-emptive hierarchical linear programming problem: a review, Recent developments in mathematical programming (S. Kumar, ed.), Gordon and Breach Sci. Publ., Philadelphia, 1991, pp. 29–43.
- 901. M. Nasri, Characterizing optimal wages in principal-agent problems without using the firstorder approach, Optimization **65** (2016), no. 2, 467–478.
- 902. N. Nezamoddini, S. Mousavian, and M. Erol-Kantarci, A risk optimization model for enhanced power grid resilience against physical attacks, Electric Power Systems Research 143 (2017), 329–338.
- 903. T.Q. Nguyen, M. Bouhtou, and J.-L. Lutton, DC approach to bilevel bilinear programming problem: application in telecommunication pricing, Optimization and Optimal Control, World Scientific, 2003, pp. 211–231.
- 904. M.G. Nicholls, Aluminium production modelling a non-linear bi-level programming approach, Operations Research 43 (1995), 208–218.
- 905. _____, The application of nonlinear bilevel programming to the aluminium industry, Journal of Global Optimization 8 (1996), 245–261.
- 906. _____, Developing an integrated model of an aluminium smelter incorporating sub-models with different time bases and levels of aggregation, European Journal of Operational Research **99** (1997), 477–490.
- 907. J. Nie, Optimality conditions and finite convergence of Lasserre's hierarchy, Mathematical programming 146 (2014), no. 1-2, 97–121.
- 908. J. Nie, L. Wang, and J. Ye, Bilevel polynomial programs and semidefinite relaxation methods, SIAM J. on Optimization 27 (2017), 1728 – 1757.
- 909. P.-Y. Nie, A note on bilevel optimization problems, International Journal of Applied Mathematical Sciences 2 (2005), 31–28.
- 910. _____, Dynamic discrete-time multi-leader-follower games with leaders in turn, Computers & Mathematics with Applications **61** (2011), no. 8, 2039–2043.
- 911. P.-Y. Nie, M.-Y. Lai, and S.-J. Zhu, Dynamic feedback Stackelberg games with non-unique solutions, Nonlinear Analysis: Theory, Methods & Applications 69 (2008), no. 7, 1904– 1913.
- 912. T. Nishi and O. Yoshida, Optimization of multi-period bilevel supply chains under demand uncertainty, Procedia CIRP **41** (2016), 508–513.
- 913. I. Nishizaki and M. Sakawa, *Stackelberg solutions to multiobjective two-level linear programming problems*, Journal of Optimization Theory and Applications **103** (1999), 161–182.

- 914. I. Nishizaki and M. Sakawa, Computational methods through genetic algorithms for obtaining Stackelberg solutions to two-level mixed zero-one programming problems, Cybernetics & Systems 31 (2000), no. 2, 203–221.
- 915. I. Nishizaki, M. Sakawa, and H. Katagiri, Stackelberg solutions to multiobjective two-level linear programming problems with random variable coefficients, Central European Journal of Operations Research 11 (2003), no. 3, 281 – 296.
- 916. A.J. Novak, G. Feichtinger, and G. Leitmann, A differential game related to terrorism: Nash and stackelberg strategies, Journal of Optimization Theory and Applications 144 (2010), no. 3, 533–555.
- 917. A. Nwosu, Pre-emptive hierarchical programming problem: a decentralized decision model, Ph.D. thesis, Department of Operations Research and Statistics, Rensselaer Polytechnic Institute, 1983.
- 918. R. Oberdieck, N. A Diangelakis, S. Avraamidou, and E.N. Pistikopoulos, On unbounded and binary parameters in multi-parametric programming: applications to mixed-integer bilevel optimization and duality theory, Journal of Global Optimization **69** (2017), 587 606.
- 919. P. Ochs, R. Ranftl, T. Brox, and T. Pock, Bilevel optimization with nonsmooth lower level problems, International Conference on Scale Space and Variational Methods in Computer Vision, Springer, 2015, pp. 654–665.
- 920. _____, Techniques for gradient-based bilevel optimization with non-smooth lower level problems, Journal of Mathematical Imaging and Vision 56 (2016), no. 2, 175–194.
- 921. V. Oduguwa and R. Roy, Bi-level optimisation using genetic algorithm, Artificial Intelligence Systems, 2002.(ICAIS 2002). 2002 IEEE International Conference on, IEEE, 2002, pp. 322–327.
- 922. W. Oeder, Ein Verfahren zur Lösung von Zwei-Ebenen-Optimierungsaufgaben in Verbindung mit der Untersuchung von chemischen Gleichgewichten, Ph.D. thesis, Technische Universität Karl-Marx-Stadt, 1988.
- 923. G. L. Olsder, *Phenomena in inverse Stackelberg games, part 1: Static problems*, Journal of Optimization Theory and Applications **143** (2009), 589–600.
- 924. _____, Phenomena in inverse Stackelberg games, part 2: Dynamic problems, Journal of Optimization Theory and Applications 143 (2009), 601–618.
- 925. H. Önal, Computational experience with a mixed solution method for bilevel linear/quadratic programs, Tech. report, University of Illinois at Urbana-Champaign, 1992.
- 926. _____, A modified simplex approach for solving bilevel linear programming problems, European Journal of Operational Research 67 (1993), 126–135.
- 927. H. Önal, D.H. Darmawan, and S.H. Johnson III, A multilevel analysis of agricultural credit distribution in East Java, Indonesia, Computers & Operations Research 22 (1995), 227– 236.
- 928. A.V. Orlov, Numerical solution of bilinear programming problems, Computational Mathematics and Mathematical Physics 48 (2008), no. 2, 225–241.
- 929. _____, Global search for optimistic solutions in bilevel problem of optimal tariff choice by telecommunication company, Izvestiya Irkutskogo Gosudarstvennogo Universiteta. Seriya" Matematika" 6 (2013), no. 1, 57–71.
- 930. A.V. Orlov and A.V. Malyshev, Test problem generation for quadratic-linear pessimistic bilevel optimization, Numerical Analysis and Applications 7 (2014), no. 3, 204–214.
- 931. M.S. Osman, M.A. Abo-Sinna, A.H. Amer, and O.E. Emam, A multi-level non-linear multiobjective decision-making under fuzziness, Applied Mathematics and Computation 153 (2004), no. 1, 239–252.
- 932. J.V. Outrata, A note on the usage of nondifferentiable exact penalties in some special optimization problems, Kybernetika 24 (1988), no. 4, 251–258.
- 933. J.V. Outrata, On the numerical solution of a class of Stackelberg problems, ZOR Mathematical Methods of Operations Research 34 (1990), 255–277.
- 934. _____, Necessary optimality conditions for Stackelberg problems, Journal of Optimization Theory and Applications **76** (1993), 305–320.
- 935. M. Pachter, *Linear-quadratic reversed Stackelberg differential games with incentives*, IEEE Transactions on Automatic Control **AC-29** (1984), 644–647.
- 936. B.B. Pal and B.N. Moitra, A fuzzy goal programming procedure for solving quadratic bilevel programming problems, International Journal of Intelligent Systems 18 (2003), no. 5, 529– 540.

- 937. K.D. Palagachev and M. Gerdts, Numerical approaches towards bilevel optimal control problems with scheduling tasks, Math for the Digital Factory, Springer, 2017, pp. 205–228.
- 938. M. Pan, P.S. Leung, and S.G. Pooley, A decision support model for fisheries management in Hawaii: a multilevel and multiobjective programming approach, North American Journal of Fisheries Management 21 (2001), no. 2, 293–309.
- 939. Q. Pan, Z. An, and H. Qi, *Exact penalty method for the nonlinear bilevel programming problem*, Wuhan University Journal of Natural Sciences **15** (2010), no. 6, 471–475.
- 940. P.D. Panagiotopoulos, E.S. Mistakidis, G.E. Stavroulakis, and O.K. Panagouli, *Multilevel optimization methods in mechanics*, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998.
- 941. J.-S. Pang and M. Fukushima, Quasi-variational inequalities, generalized Nash equilibria, and multi-leader-follower games, Comput. Manag. Sci. 2 (2005), no. 1, 21–56.
- 942. G. Papavassilopoulos, Algorithms for static Stackelberg games with linear costs and polyhedral constraints, Proceedings of the 21st IEEE Conference on Decisions and Control, 1982, pp. 647–652.
- 943. F. Parraga, *Hierarchical programming and applications to economic policy*, Ph.D. thesis, Systems and Industrial Engineering Department, University of Arizona, 1981.
- 944. M. Patriksson, On the applicability and solution of bilevel optimization models in transportation science: A study on the existence, stability and computation of optimal solutions to stochastic mathematical programs with equilibrium constraints, Transportation Research Part B: Methodological **42** (2008), no. 10, 843–860.
- 945. M. Patriksson and R.T. Rockafellar, A mathematical model and descent algorithm for bilevel traffic management, Transportation Science **36** (2002), no. 3, 271–291.
- 946. M. Patriksson and L. Wynter, *Stochastic nonlinear bilevel programming*, Tech. report, PRISM, Université de Versailles Saint Quentin en Yvelines, Versailles, France, 1997.
- 947. ____, Stochastic mathematical programs with equilibrium constraints, OR Letters 25 (1999), 159–167.
- 948. R. Paulavicius and C.S. Adjiman, *BASBL: branch-and-sandwich bilevel solver. i. theoretical advances and algorithmic improvements*, Tech. report, Imperial College London, 2017.
- 949. R. Paulavicius, P.M. Kleniati, and C.S. Adjiman, Global optimization of nonconvex bilevel problems: implementation and computational study of the branch-and-sandwich algorithm, Computer Aided Chemical Engineering **38** (2016), 1977–1982.
- 950. _____, BASBL: branch-and-sandwich bilevel solver. ii. implementation and computational study with the basbl test set, Tech. report, Imperial College London, 2017.
- 951. K. Pavlova, T. Stoilov, and K. Stoilova, *Bi-level model for public rail transportation under incomplete data*, Cybernetics and Information Technologies **17** (2017), no. 3, 75–91.
- 952. R. Peng, X. Rui-hua, and Q. Jin, Bi-level simulated annealing algorithm for facility location problem, Information Management, Innovation Management and Industrial Engineering, 2008. ICIII'08. International Conference on, vol. 3, IEEE, 2008, pp. 17–22.
- 953. A.A. Pessoa, M. Poss, M.C. Roboredo, and L. Aizemberg, Solving bilevel combinatorial optimization as bilinear min-max optimization via a branch-and-cut algorithm, Anais do XLV Simp{\{}'o}sio Brasileiro de Pesquisa Operacional (2013).
- 954. T. Petersen, Optimale Anreizsysteme, Gabler Verlag, Wiesbaden, 1989.
- 955. A. G. Petoussis, Supply function equilibrium analysis for electricity markets, Ph.D. thesis, University of Warwick, 2009.
- 956. E.G. Petrova and T.V. Gruzdeva, *The linear bilevel problems via nonconvex constraint problems*, Proceedings of the Toulouse Global Optimization workshop : TOGO10 : Toulouse, France, August-September 2010 (C. Cafieri, E.M.T. Hendrix, L. Liberti, and F. Messine, eds.), 2010, pp. 123–126.
- 957. E.G. Petrova and A.S. Strekalovsky, The quadratic-linear bilevel problems solving via nonconvex constraint problems (*i* special issue; bilevel programming, optimization methods, and applications to economics), International Journal of Biomedical Soft Computing and Human Sciences: the official journal of the Biomedical Fuzzy Systems Association 18 (2013), no. 1, 63–67.
- 958. G. Peyré and J. M Fadili, Learning analysis sparsity priors, Sampta'11, 2011.

- 959. P. Pharkya, A.P. Burgard, and C.D. Maranas, Exploring the overproduction of amino acids using the bilevel optimization framework OptKnock, Biotechnology and Bioengineering 84 (2003), no. 7, 887 – 899, Application in bioengineering.
- 960. G. Pieri, Sufficient conditions for the existence of the solution for bilevel minimization problems with constraints in banach spaces, Rivista di matematica pura ed applicata 5 (1989), 41–48.
- 961. C. O. Pieume, *Multiobjective optimization approaches in bilevel optimization*, Ph.D. thesis, Université de Yaounde I, 2011.
- 962. C. O. Pieume, L. P. Fotso, and P. Siarry, Solving bilevel programming problems with multicriteria optimization techniques, Opsearch 46 (2009), 169–183.
- 963. C. O. Pieume, P. Marcotte, L. P. Fotso, and P. Siarry, *Solving bilevel linear multiobjective programming problems*, American Journal of Operations Research 1 (2011), 214–219.
- 964. M. Pilecka, *Combined reformulation of bilevel programming problems*, Master's thesis, TU Bergakademie Freiberg, Fakultät für Mathematrik und Informatik, 2011.
- 965. _____, Combined reformulation of bilevel programming problems, Schedae Informaticae **2012** (2012), no. Volume 21, 65–79.
- 966. ____, Set valued optimization and its application to bilevel optimization, Ph.D. thesis, TU Bergakademie Freiberg, 2016.
- 967. E.A. Pilotta and G.A. Torres, An inexact restoration package for bilevel programming problems, Applied Mathematics 2012 (2012), no. 3, 1252–1259.
- 968. S. Pineda, H. Bylling, and J.M. Morales, Efficiently solving linear bilevel programming problems using off-the-shelf optimization software, Optimization and Engineering (2017), 1–25.
- 969. _____, Efficiently solving linear bilevel programming problems using off-the-shelf optimization software, Optimization and Engineering **19** (2018), no. 1, 187–211.
- 970. P. Pisciella, Methods for evaluation of business models for provision of advanced mobile services under uncertainty, Ph.D. thesis, Norvegian University of Science and Technology, 2012.
- 971. P. Pisciella and A.A. Gaivoronski, Stochastic programming bilevel models for service provision with a balancing coordinator, IMA Journal of Management Mathematics (2015), 22, doi:10.1093/imaman/dpv023.
- 972. E.N. Pistikopoulos, V. Dua, and J.-H. Ryu, Global optimization of bilevel programming problems via parametric programming, Frontiers in global optimization, Springer, 2004, pp. 457–476.
- 973. F. Plastria and L. Vanhaverbeke, Discrete models for competitive location with foresight, Computers & Operations Research 35 (2008), no. 3, 683–700.
- 974. A.V. Plyasunov, A polynomially solvable class of two-level nonlinear programming problems, Diskretnyj Analiz i Issledovanie Operatsii , Seriya 2 7 (2000), 89–113, in russian.
- 975. _____, A two-level linear programming problem with a multivariant knapsack at the lower level, Diskretnyi Analiz i Issledovanie Operatsii **10** (2003), no. 1, 44–52.
- 976. P.-L. Poirion, S. Toubaline, C. D' Ambrosio, and L. Liberti, *Bilevel mixed-integer linear programs and the zero forcing set*, Tech. report, École Polytechnique, Palaiseau, France, 2016.
- 977. D. Pozo, E. Sauma, and J. Contreras, Basic theoretical foundations and insights on bilevel models and their applications to power systems, Annals of Operations Research (2017), 1-32.
- 978. S. Pramanik, Bilevel programming problem with fuzzy parameters: A fuzzy goal programing approach, Journal of Applied Quantitative Methods 1 (2011), no. 7, 9–24.
- 979. S. Pramanik and T.K. Roy, *Fuzzy goal programming approach to multilevel programming problems*, European Journal of Operational Research **176** (2007), no. 2, 1151–1166.
- 980. X. Qiu and G.Q. Huang, Storage pricing, replenishment, and delivery schedules in a supply hub in industrial park: A bilevel programming approach, International Journal of Production Research 51 (2013), no. 23–24, 6950–6971.
- 981. X. Qiu and W. Kern, Improved approximation algorithms for a bilevel knapsack problem, Theoretical computer science **595** (2015), 120–129.
- 982. A. Rahmani and S.A. MirHassani, Lagrangean relaxation-based algorithm for bi-level problems, Optimization Methods and Software **30** (2015), no. 1, 1–14.

- 983. A. Rahmani and M. Yousefikhoshbakht, An effective branch-and-cut algorithm in order to solve the mixed integer bi-level programming, International Journal of Production Management and Engineering 5 (2017), no. 1, 1–10.
- 984. J. Rajesh, K. Gupta, H.S. Kusumakar, V.K. Jayaraman, and B.D. Kulkarni, A tabu search based approach for solving a class of bilevel programming problems in chemical engineering, Journal of Heuristics 9 (2003), no. 4, 307–319.
- 985. R. Ranftl and T. Pock, A deep variational model for image segmentation, Pattern Recognition, Springer, 2014, pp. 107–118.
- 986. R. Rees, The theory of principal and agent. part 1, Bulletin of Economic Research 37 (1985), 3-26.
- 987. ____, The theory of principal and agent. part 2, Bulletin of Economic Research **37** (1985), 75–95.
- 988. A. Ren, A novel method for solving the fully fuzzy bilevel linear programming problem, Mathematical Problems in Engineering **2015** (2015), 11 pages.
- 989. _____, Solving the fully fuzzy bilevel linear programming problem through deviation degree measures and a ranking function method, Mathematical Problems in Engineering **2016** (2016).
- 990. A. Ren and Y. Wang, A cutting plane method for bilevel linear programming with interval coefficients, Annals of Operations Research **223** (2014), no. 1, 355–378.
- 991. _____, A novel penalty function method for semivectorial bilevel programming problem, Applied Mathematical Modelling **40** (2016), no. 1, 135–149.
- 992. ____, An approach based on reliability-based possibility degree of interval for solving general interval bilevel linear programming problem, Soft Computing (2017).
- 993. _____, A new approach based on possibilistic programming technique and fractile optimization for bilevel programming in a hybrid uncertain circumstance, Applied Intelligence (2018), 1–15.
- 994. A. Ren, Y. Wang, and X. Xue, Interactive programming approach for solving the fully fuzzy bilevel linear programming problem, Knowledge-Based Systems 99 (2016), 103–111.
- 995. _____, A novel approach based on preference-based index for interval bilevel linear programming problem, Journal of Inequalities and Applications **2017** (2017), no. 1, 112.
- 996. A. Ren and X. Xue, A new solution method for a class of fuzzy random bilevel programming problems, International Conference on Intelligent Information Hiding and Multimedia Signal Processing, Springer, 2017, pp. 233–241.
- 997. _____, Solution strategy for bilevel linear programming in fuzzy random circumstances, Computational Intelligence and Security (CIS), 2017 13th International Conference on, IEEE, 2017, pp. 508–511.
- 998. G. Ren, Z. Huang, Y. Cheng, X. Zhao, and Y. Zhang, An integrated model for evacuation routing and traffic signal optimization with background demand uncertainty, Journal of Advanced Transportation 47 (2013), no. 1, 4–27.
- 999. H.-L. Ren, Origin-destination demands estimation in congested dynamic transit networks, Management Science and Engineering, 2007. International Conference on ICMSE 2007., IEEE, 2007, pp. 2247–2252.
- 1000. H. Riahi, Z. Chbani, and M.-T. Loumi, Weak and strong convergences of the generalized penalty forward forward and forward backward splitting algorithms for solving bilevel hierarchical pseudomonotone equilibrium problems, Optimization (2018), 1–23, e-first publication.
- 1001. M.J. Rider, J.M. López-Lezama, J. Contreras, and A. Padilha-Feltrin, Bilevel approach for optimal location and contract pricing of distributed generation in radial distribution systems using mixed-integer linear programming, IET Generation, Transmission & Distribution 7 (2013), no. 7, 724–734.
- 1002. G. Ridinger, R.S. John, M. McBride, and N. Scurich, Attacker deterrence and perceived risk in a stackelberg security game, Risk Analysis **36** (2016), no. 8, 1666–1681.
- 1003. R.M. Rizk-Allah and M.A. Abo-Sinna, Integrating reference point, Kuhn-Tucker conditions and neural network approach for multi-objective and multi-level programming problems, OPSEARCH (2017), 1–21.
- 1004. M.J. Robbins and B.J. Lunday, A bilevel formulation of the pediatric vaccine pricing problem, European Journal of Operational Research **248** (2016), no. 2, 634–645.
- 1005. A.J. Robson, Stackelberg and marshall, The American Economic Review (1990), 69–82.

- 1006. S. Roch, P. Marcotte, and G. Savard, *Design and analysis of an approximation algorithm* for Stackelberg network pricing, Citeseer, 2003.
- 1007. S. Roch, G. Savard, and P. Marcotte, An approximation algorithm for Stackelberg network pricing., Networks 46 (2005), no. 1, 57–67.
- 1008. R. Rog, Lösungsalgorithmen für die KKT-Transformation von Zwei-Ebenen-Optimierungsaufgaben, Master's thesis, TU Bergakademie Freiberg, Fakultät für Mathematik und Informatik, 2017.
- 1009. W.P. Rogerson, *The first-order approach to principal-agent problems*, Econometrica: Journal of the Econometric Society (1985), 1357–1367.
- 1010. E. Roghanian, M.B. Aryanezhad, and S.J. Sadjadi, Integrating goal programming, Kuhn-Tucker conditions, and penalty function approaches to solve linear bi-level programming problems, Applied Mathematics and Computation 195 (2008), no. 2, 585 – 590.
- 1011. E. Roghanian, S.J. Sadjadi, and M.-B. Aryanezhad, A probabilistic bi-level linear multiobjective programming problem to supply chain planning, Applied Mathematics and Computation 188 (2007), no. 1, 786–800.
- 1012. S.A. Ross, The economic theory of agency: the principal's problem, AER **63** (1973), 134–139.
- 1013. G. Ruan, The properties for the linear bilevel programming problem, Natural Science Journal of Xiangtan University 15 (1993), 5–9, in chinese.
- 1014. _____, An algorithm for the linear bilevel programming problem, Natural Science Journal of Xiangtan University 16 (1994), 1–5, in chinese.
- 1015. G.Z. Ruan, S.Y. Wang, Y. Yamamoto, and S.S. Zhu, Optimality conditions and geometric properties of a linear multilevel programming problem with dominated objective functions, Journal of optimization theory and applications 123 (2004), no. 2, 409–429.
- 1016. S. Ruuska, K. Miettinen, and M.M. Wiecek, Connections between single-level and bilevel multiobjective optimization, Journal of Optimization Theory and Applications 153 (2012), no. 1, 60–74.
- 1017. A. Ruziyeva, Fuzzy bilevel programming, Ph.D. thesis, TU Bergakademie Freiberg, 2013.
- 1018. J.-H. Ryu, V. Dua, and E.N. Pistikopoulos, A bilevel programming framework for enterprise-wide process networks under uncertainty, Computers & Chemical Engineering 28 (2004), no. 6-7, 1121–1129.
- 1019. S. Sabach and S. Shtern, A first order method for solving convex bilevel optimization problems, SIAM Journal on Optimization 27 (2017), no. 2, 640–660.
- 1020. R. Saboiev, Solution methods for linear bilevel optimization problems, Ph.D. thesis, TU Bergakademie Freiberg, 2016.
- 1021. S.M. Sadatrasou, M.R. Gholamian, and K. Shahanaghi, An application of data mining classification and bi-level programming for optimal credit allocation, Decision Science Letters 4 (2015), 35–50.
- 1022. S. Sadeghi, A. Seifi, and E. Azizi, *Trilevel shortest path network interdiction with partial fortification*, Computers & Industrial Engineering **106** (2017), 400–411.
- 1023. A.S. Safaei, S. Farsad, and M.M. Paydar, *Robust bi-level optimization of relief logistics* operations, Applied Mathematical Modelling **56** (2018), 359–380.
- 1024. K.S. Sagyngaliev, Coordinated resource allocation in a three-level active system, Avtomatika i Telemechanika **10** (1986), 81–88, russ.
- 1025. G.K. Saharidis and M.G. Ierapetritou, Resolution method for mixed integer bi-level linear problems based on decomposition technique, Journal of Global Optimization 44 (2009), no. 1, 29–51.
- 1026. G.K.D. Saharidis, A.J. Conejo, and G. Kozanidis, Exact solution methodologies for linear and (mixed) integer bilevel programming, Metaheuristics for Bi-level Optimization, Springer, 2013, pp. 221–245.
- 1027. K.H. Sahin and A.R. Ciric, A dual temperature simulated annealing approach for solving bilevel programming problems, Computers and Chemical Engineering 23 (1998), 11–25.
- 1028. M.E. Sáiz, E.M. T. Hendrix, J. Fernández, and B. Pelegrín, On a branch-and-bound approach for a huff-like Stackelberg location problem, OR Spectrum **31** (2009), no. 3, 679–705.
- 1029. M. Sakawa, Genetic algorithms and fuzzy multiobjective optimization, vol. 14, Springer Science & Business Media, 2012.

- 1030. M. Sakawa and H. Katagiri, *Stackelberg solutions for fuzzy random two-level linear programming through level sets and fractile criterion optimization*, Central European Journal of Operations Research **20** (2012), no. 1, 101–117.
- 1031. M. Sakawa, H. Katagiri, and T. Matsui, Stackelberg solutions for fuzzy random two-level linear programming through probability maximization with possibility, Fuzzy Sets and Systems 188 (2012), no. 1, 45–57.
- 1032. M. Sakawa and I. Nishizaki, Interactive fuzzy programming for multi-level nonconvex nonlinear programming problems through genetic algorithms, Dynamical Aspects in Fuzzy Decision Making, Springer, 2001, pp. 99–116.
- 1033. _____, Interactive fuzzy programming for two-level nonconvex programming problems with fuzzy parameters through genetic algorithms, Fuzzy Sets and Systems **127** (2002), no. 2, 185–197.
- 1034. _____, Cooperative and noncooperative multi-level programming, vol. 48, Springer Science & Business Media, 2009.
- 1035. _____, Interactive fuzzy programming for multi-level programming problems: a review, International Journal of Multicriteria Decision Making 2 (2012), no. 3, 241–266.
- 1036. M. Sakawa, I. Nishizaki, and M. Hitaka, Interactive fuzzy programming for multi-level 0-1 programming problems through genetic algorithms, European Journal of Operational Research **114** (1999), no. 3, 580–588.
- 1037. _____, Interactive fuzzy programming for multi-level 0-1 programming problems with fuzzy parameters through genetic algorithms, Fuzzy Sets and Systems **117** (2001), no. 1, 95-111.
- 1038. M. Sakawa, I. Nishizaki, and Y. Uemura, Interactive fuzzy programming for multilevel linear programming problems, Computers & Mathematics with Applications 36 (1998), no. 2, 71– 86.
- 1039. _____, Interactive fuzzy programming for multi-level linear programming problems with fuzzy parameters, Fuzzy Sets and Systems **109** (2000), no. 1, 3–19.
- 1040. _____, Interactive fuzzy programming for two-level linear and linear fractional production and assignment problems: a case study, European Journal of Operational Research 135 (2001), 142–157.
- 1041. S.S. Sana, A production-inventory model of imperfect quality products in a three-layer supply chain, Decision Support Systems **50** (2011), no. 2, 539–547.
- 1042. N.G.F. Sancho, A suboptimal solution to a hierarchical network design problem using dynamic programming, European Journal of Operational Research 83 (1995), 237–244.
- 1043. M. Saraj and S. Sadeghi, Quadratic bi-level programming problems: a fuzzy goal programming approach, International Journal of Applied Operational Research 4 (2014), no. 2, 83–88.
- 1044. S. Saranwong and C. Likasiri, Bi-level programming model for solving distribution center problem: A case study in northern Thailands sugarcane management, Computers & Industrial Engineering 103 (2017), 26–39.
- 1045. M. Sasaki, J.F. Campbell, M. Krishnamoorthy, and A.T. Ernst, A Stackelberg hub arc location model for a competitive environment, Computers & Operations Research 47 (2014), 27–41.
- 1046. G. Savard, *Contribuitions à la programmation mathématique à deux niveaux*, Ph.D. thesis, École Polytechnique, Université de Montréal, 1989.
- 1047. G. Savard and J. Gauvin, The steepest descent direction for the nonlinear bilevel programming problem, Operations Research Letters 15 (1994), 265–272.
- 1048. M.P. Scaparra and R.L. Church, A bilevel mixed-integer program for critical infrastructure protection planning, Computers & Operations Research **35** (2008), no. 6, 1905–1923.
- 1049. _____, Protecting supply systems to mitigate potential disaster: a model to fortify capacitated facilities, International Regional Science Review **35** (2012), no. 2, 188–210.
- 1050. H. Scheel and S. Scholtes, Mathematical programs with equilibrium constraints: stationarity, optimality, and sensitivity, Mathematics of Operations Research 25 (2000), 1–22.
- 1051. G. Schenk, A multilevel programming model for determining regional effluent charges, Master's thesis, Department of Industrial Engineering, State University of New York at Buffalo, 1980.
- 1052. H. Schmidt, Zwei-Ebenen-Opitmierungsaufgaben mit mehrelementiger Lösung der unteren Ebenen, Ph.D. thesis, TU Chemnitz, 1996.

- 1053. J. Schulte, N. Feldkamp, S. Bergmann, and V. Nissen, Bilevel innovization: knowledge discovery in scheduling systems using evolutionary bilevel optimization and visual analytics, Proceedings of the Genetic and Evolutionary Computation Conference Companion, ACM, 2018, pp. 197–198.
- 1054. R. Segall, *Bi-level geometric programming: a new optimization model*, Tech. report, Department of Mathematics, University of Lowell Olsen Hall, 1989.
- 1055. R.S. Segall, Using branch-and-bound to solve bi-level geometric programming problems: A new optimization model, Applied Mathematical Modelling **14** (1990), no. 5, 271–274.
- 1056. _____, An update on bi-level geometric programming: A new optimization model, Applied mathematical modelling **17** (1993), no. 4, 219–222.
- 1057. S.P. Sethi and Q. Zhang, Multilevel hierarchical open-loop and feedback controls in stochastic marketing-production systems, IEEE Transactions on Robotics and Automation 10 (1994), no. 6, 831–839.
- 1058. Y.V. Shamardin, Three-level problems of allocation of the production, Tech. Report 47, Russian Academy of Sciences, Siberian Branch, Insitut of Mathemetics, Novosibirsk, 1998, (in Russian).
- 1059. ____, On a two-level location problem with constraints on the volume of production, Diskretnyi Analiz i Issledovanie Operatsii 7 (2000), no. 2, 114–118.
- 1060. H. Shao, W.H.K. Lam, A. Sumalee, A. Chen, and M.L. Hazelton, Estimation of mean and covariance of peak hour origin-destination demands from day-to-day traffic counts, Transportation Research Part B: Methodological 68 (2014), 52-75.
- 1061. A. Sharma, V. Verma, P. Kaur, and K. Dahiya, An iterative algorithm for two level hierarchical time minimization transportation problem, European Journal of Operational Research 246 (2015), no. 3, 700–707.
- 1062. V. Sharma, K. Dahiya, and V. Verma, A class of integer linear fractional bilevel programming problems, Optimization 63 (2014), no. 10, 1565–1581.
- 1063. Y. Sharma and D.P. Williamson, Stackelberg thresholds in network routing games or the value of altruism, Games and Economic Behavior 67 (2009), no. 1, 174 – 190, Special Section of Games and Economic Behavior Dedicated to the 8th ACM Conference on Electronic Commerce.
- 1064. J. Shaw, A parametric complementary pivot approach to multilevel programming, Master's thesis, Department of Industrial Engineering, State University of New York at Buffalo, 1980.
- 1065. H. Sherali, A multiple leader Stackelberg model and analysis, Operations Research 32 (1984), 390–404.
- 1066. H.D. Sherali, A.L. Soyster, and F.H. Murphy, *Stackelberg-Nash-Cournot equilibria: Char*acterizations and Computations, Operations Research **31** (1983), 253–276.
- 1067. C. Shi, J. Lu, and G. Zhang, An extended Kuhn-Tucker approach for linear bilevel programming, Applied Mathematics and Computation 162 (2005), 51–63.
- 1068. C. Shi, J. Lu, and G. Zhang, An extended Kth-best approach for linear bilevel programming, Applied Mathematics and Computation 164 (2005), no. 3, 843–855.
- 1069. C. Shi, J. Lu, G. Zhang, and H. Zhou, An extended branch and bound algorithm for linear bilevel programming, Applied Mathematics and Computation 180 (2006), no. 2, 529–537.
- 1070. C. Shi, G. Zhang, and J. Lu, *The k-th-best approach for linear bilevel multi-follower pro*gramming, Journal of Global Optimization **33** (2005), no. 4, 563–578.
- 1071. C. Shi, G. Zhang, and J. Lu, On the definition of linear bilevel programming solution, Applied Mathematics and Computation 160 (2005), 169–176.
- 1072. C. Shi, H. Zhou, J. Lu, G. Zhang, and Z. Zhang, The kth-best approach for linear bilevel multifollower programming with partial shared variables among followers, Applied Mathematics and Computation 188 (2007), no. 2, 1686–1698.
- 1073. C. Shi, H. Zhou, J. Lu, G. Zhang, and Z. Zhang, The kth-best approach for linear bilevel multifollower programming with partial shared variables among followers, Applied Mathematics and Computation 188 (2007), no. 2, 1686 – 1698.
- 1074. H.-S. Shih, Y.-L. Lai, and E. S. Lee, *Fuzzy approach for multilevel programming problems*, Computers & Operations Research **23** (1996), 73–91.
- 1075. H.-S. Shih, U.-P. Wen, S. Lee, K.-M. Lan, and H.-C. Hsiao, A neural network approach to multiobjective and multilevel programming problems, Computers & Mathematics with Applications 48 (2004), no. 1, 95–108.

- 1076. H.S. Shih, C.B. Cheng, U.P. Wen, Y.C. Huang, and M.Y. Peng, Determining a subsidy rate for taiwan's recycling glass industry: an application of bi-level programming, Journal of the Operational Research Society 63 (2012), no. 1, 28–37.
- 1077. K. Shimizu, Two-level decision problems and their new solution methods by a penalty method, Control science and technology for the progress of society, vol. 2, pp. 1303–1308, IFAC, 1982.
- 1078. K. Shimizu and E. Aiyoshi, A new computational method for Stackelberg and min-max problems by use of a penalty method, IEEE Transactions on Automatic Control 26 (1981), 460–466.
- 1079. K. Shimizu and Y. Ishizuka, Optimality conditions and algorithms for parameter design problems with two-level structure, IEEE Transactions on Automatic Control 30 (1985), no. 10, 986–993.
- 1080. K. Shimizu, Y. Ishizuka, and J.F. Bard, Nondifferentiable and two-level mathematical programming, Kluwer Academic Publishers, Dordrecht, 1997.
- 1081. K. Shimizu and M. Lu, A global optimization method for the Stackelberg problem with convex functions via problem transformations and concave programming, IEEE Transactions on Systems, Man, and Cybernetics 25 (1995), 1635–1640.
- 1082. C. Shouhua, Y. Zhenzhou, L. Yanhong, and W. Xianyu, Model for road network stochastic user equilibrium based on bi-level programming under the action of the traffic flow guidance system, Journal of Transportation Systems Engineering and Information Technology 7 (2007), no. 4, 36–42.
- 1083. S.A. Siddiqui, Solving two-level optimization problems with applications to robust design and energy markets, Ph.D. thesis, University of Maryland, 2011.
- 1084. M. Simaan, *Stackelberg optimization of two-level systems*, IEEE Transactions on Systems, Man, and Cybernetics **7** (1977), 554–557.
- 1085. M. Simaan and J.B. Cruz, On the Stackelberg strategy in nonzero-sum games, Journal Optimization Theory and Applications 11 (1973), 533 555.
- 1086. M. Simaan and Jr. Cruz, J.B., On the Stackelberg Strategy in Nonzero-Sum Games, Multicriteria Decision Making and Differential Games (George Leitmann, ed.), Mathematical Concepts and Methods in Science and Engineering, Springer US, 1976, pp. 173–195.
- 1087. B. Sinclair-Desagne, The first-order approach to multi-signal principal-agent systems, Econometrica **62** (1994), 459–465.
- 1088. S. Singh, An approach to solve bilevel quadratic-linear programming problems, Proceedings of the International MultiConference of Engineers and Computer Scientists, vol. 2, 2012.
- 1089. V.P. Singh and D. Chakraborty, Solving bi-level programming problem with fuzzy random variable coefficients, Journal of Intelligent & Fuzzy Systems **32** (2017), no. 1, 521–528.
- 1090. A. Sinha and K. Deb, Towards understanding evolutionary bilevel multi-objective optimization algorithm, IFAC Proceedings Volumes 42 (2009), no. 2, 338–343.
- 1091. A. Sinha, P. Malo, and K. Deb, An improved bilevel evolutionary algorithm based on quadratic approximations, IEEE Congress on Evolutionary Computation (CEC), IEEE, 2014, pp. 1870–1877.
- 1092. ____, Test problem construction for single-objective bilevel optimization, Evolutionary computation **22** (2014), no. 3, 439–477.
- 1093. _____, Towards understanding bilevel multi-objective optimization with deterministic lower level decisions, International Conference on Evolutionary Multi-Criterion Optimization, Springer, 2015, pp. 426–443.
- 1094. _____, Transportation policy formulation as a multi-objective bilevel optimization problem, IEEE Congress on Evolutionary Computation (CEC), IEEE, 2015, pp. 1651–1658.
- 1095. _____, Solving optimistic bilevel programs by iteratively approximating lower level optimal value function, IEEE Congress on Evolutionary Computation (CEC), IEEE, 2016, pp. 1877–1884.
- 1096. _____, Approximated set-valued mapping approach for handling multiobjective bilevel problems, Computers & Operations Research 77 (2017), 194–209.
- 1097. _____, Approximated set-valued mapping approach for handling multiobjective bilevel problems, Computers & Operations Research 77 (2017), 194–209.
- 1098. _____, Evolutionary algorithm for bilevel optimization using approximations of the lower level optimal solution mapping, European Journal of Operational Research 257 (2017), no. 2, 395–411.

- 1099. _____, Evolutionary bilevel optimization: An introduction and recent advances, Recent Advances in Evolutionary Multi-objective Optimization, Springer, 2017, pp. 71–103.
- 1100. _____, A review on bilevel optimization: From classical to evolutionary approaches and applications, IEEE Transactions on Evolutionary Computation (2017).
- 1101. A. Sinha, P. Malo, K. Deb, P. Korhonen, and J. Wallenius, Solving bilevel multicriterion optimization problems with lower level decision uncertainty, IEEE Transactions on Evolutionary Computation 20 (2016), no. 2, 199–217.
- 1102. A. Sinha, P. Malo, A. Frantsev, and K. Deb, Multi-objective Stackelberg game between a regulating authority and a mining company: A case study in environmental economics, IEEE Congress on Evolutionary Computation (CEC), IEEE, 2013, pp. 478–485.
- 1103. _____, Finding optimal strategies in a multi-period multi-leader-follower Stackelberg game using an evolutionary algorithm, Computers & Operations Research 41 (2014), 374–385.
- 1104. A. Sinha, P. Malo, P. Xu, and K. Deb, A bilevel optimization approach to automated parameter tuning, Proceedings of the 2014 Annual Conference on Genetic and Evolutionary Computation, ACM, 2014, pp. 847–854.
- 1105. A. Sinha, T. Soun, and K. Deb, Using karush-kuhn-tucker proximity measure for solving bilevel optimization problems, Swarm and Evolutionary Computation (2018).
- 1106. S. Sinha, A comment on Anandalingam (1988). A mathematical programming model of decentralized multi-level systems, The Journal of the Operational Research Society 52 (2001), no. 5, 594–596.
- 1107. _____, Fuzzy mathematical programming applied to multi-level programming problems, Computers & Operations Research **30** (2003), 1259–1268.
- 1108. ____, Fuzzy mathematical programming applied to multi-level programming problems, Computers & Operations Research **30** (2003), no. 9, 1259–1268.
- 1109. _____, Fuzzy programming approach to multi-level programming problems, Fuzzy Sets and Systems **136** (2003), 189–202.
- 1110. O. Skulovich, L. Perelman, and A. Ostfeld, Bi-level optimization of closed surge tanks placement and sizing in water distribution system subjected to transient events, Procedia Engineering 89 (2014), 1329–1335.
- 1111. J.C. Smith and C. Lim, Algorithms for network interdiction and fortification games, Pareto optimality, game theory and equilibria **17** (2008), 609–644.
- 1112. W.R. Smith and R.W. Missen, *Chemical reaction equilibrium analysis: theory and algorithms*, John Wiley & Sons, New York, 1982.
- 1113. M. Soismaa, A note on efficient solutions for the linear bilevel programming problem, European Journal of Operational Research **112** (1999), 427–431.
- 1114. M.V. Solodov, A bundle method for a class of bilevel nonsmooth convex minimization problems, SIAM J. on Optimization 18 (2007), 242–259.
- 1115. _____, An explicit descent method for bilevel convex optimization, Journal of Convex Analysis 14 (2007), no. 2, 227–237.
- 1116. H.-M. Song, H. Yang, and A. Bensoussan, Optimizing production and inventory decisions in a supply chain with lot size, production rate and lead time interactions, Applied Mathematics and Computation 224 (2013), 150 – 165.
- 1117. Sonia, A. Khandelwal, and M.C. Puri, *Bilevel time minimizing transportation problem*, Discrete Optimization **5** (2008), no. 4, 714–723.
- 1118. Sonia and M.C. Puri, Two level hierarchical time minimizing transportation problem, Top 12 (2004), no. 2, 301–330.
- 1119. ____, Bilevel time minimizing assignment problem, Applied Mathematics and Computation 183 (2006), no. 2, 990 999.
- 1120. W. Sosa and F. Raupp, On optimization over weakly efficient sets, Optimization 56 (2007), 207–219.
- 1121. R. Sousa, N. Shah, and L.G. Papageorgiou, Supply chain design and multilevel planningan industrial case, Computers & Chemical Engineering 32 (2008), no. 11, 2643–2663.
- 1122. P. Sprechmann, A.M. Bronstein, and G. Sapiro, Supervised non-euclidean sparse nmf via bilevel optimization with applications to speech enhancement, Hands-free Speech Communication and Microphone Arrays (HSCMA), 2014 4th Joint Workshop on, IEEE, 2014, pp. 11–15.
- 1123. S. Srivastava and S.K. Sahana, Nested hybrid evolutionary model for traffic signal optimization, Applied Intelligence 46 (2017), no. 1, 113–123.

- 1124. H.v. Stackelberg, *Marktform und Gleichgewicht*, Springer-Verlag, Berlin, 1934, engl. transl.: The Theory of the Market Economy, Oxford University Press, 1952.
- 1125. W. Stanford, Pure strategy nash equilibria and the probabilistic prospects of stackelberg players, Operations Research Letters **38** (2010), no. 2, 94–96.
- 1126. T. Starostina and S. Dempe, *Sensitivity analysis for fuzzy shortest path problem*, Computational Intelligence, Theory and Applications, Springer, 2005, pp. 695–702.
- 1127. S. Steffensen, *Global solution of bilevel programming problems*, Operations Research Proceedings 2014, Springer, 2016, pp. 575–580.
- 1128. O. Stein, *Bi-level strategies in semi-infinite programming*, Kluwer Akademic Publishers, Boston, 2003.
- 1129. O. Stein and G. Still, Working paper on generalized semi-infinite optimization and bilevel optimization, Tech. report, Faculty of Mathematical Sciences, University of Twente, 1999.
- 1130. _____, On generalized semi-infinite optimization and bilevel optimization, European Journal of Operational Research **142** (2002), no. 3, 444 – 462.
- 1131. W.J. Steiner, A Stackelberg-Nash model for new product design., OR Spectrum 32 (2010), no. 1, 21–48.
- 1132. G. Still, Linear bilevel problems: genericity results and an efficient method for computing local minima., Math. Methods Oper. Res. 55 (2002), no. 3, 383–400.
- 1133. K. Stoilova, *Fast resource allocation by bilevel programming problem*, International IFAC workshop DECOM-TT 2004, Bansko, Bulgaria, 2004, pp. 249–254.
- 1134. K. Stoilova, T. Stoilov, and V. Ivanov, Bi-level optimization as a tool for implementation of intelligent transportation systems, Cybernetics and Information Technologies 17 (2017), no. 2, 97–105.
- 1135. K. Stoilova and T.Stoilov, *Predictive coordination in two level hierarchical systems*, IEEE Symposium Intelligent Systems, 10–12 September 2002, Varna, vol. I, 2002, pp. 332–337.
- 1136. A. Street, A. Moreira, and J.M. Arroyo, Energy and reserve scheduling under a joint generation and transmission security criterion: An adjustable robust optimization approach, IEEE Transactions on Power Systems 29 (2014), no. 1, 3–14.
- 1137. A.S. Strekalovskii, A.V. Orlov, and A.V. Malyshev, A local search for the quadratic-linear bilevel programming problem, Sibirskii Zhurnal Vychislitel'noi Matematiki 13 (2010), no. 1, 75–88.
- 1138. _____, Numerical solution of a class of bilevel programming problems, Sibirskii Zhurnal Vychislitel'noi Matematiki **13** (2010), no. 2, 201–212.
- 1139. A.S. Strekalovsky, *Methods for solving the bilevel optimization problems*, Proc. of the II Intern. Conf. OPTIMA-2011 (Petrovac, Montenegro, 2011, pp. 205–208.
- 1140. A.S. Strekalovsky, A.V. Orlov, and A.V. Malyshev, *Local search in a quadratic-linear bilevel programming problem*, Numerical Analysis and Applications **3** (2010), no. 1, 59–70.
- 1141. _____, Numerical solution of a class of bilevel programming problems, Numerical Analysis and Applications **3** (2010), no. 2, 165–173.
- 1142. _____, On computational search for optimistic solutions in bilevel problems, Journal of Global Optimization **48** (2010), no. 1, 159–172.
- 1143. S. Suh and T. Kim, Solving nonlinear bilevel programming models of the equilibrium network design problem: a comparative review, Annals of Operations Research **34** (1992), 203–218.
- 1144. H. Sun, Z. Gao, and J. Wu, A bi-level programming model and solution algorithm for the location of logistics distribution centers, Applied Mathematical Modelling 32 (2008), no. 4, 610–616.
- 1145. S. K. Suneja and B. Kohli, Optimality and duality results for bilevel programming problem using convexifactors, Journal of Optimization Theory and Applications 150 (2011), no. 1, 1–19.
- 1146. C. Suwansirikul, T. Friesz, and R. Tobin, Equilibrium decomposed optimization: a heuristic for the continuous equilibrium network design problem, Transportation Science 21 (1987), 254–263.
- 1147. A.F. Taha, N.A. Hachem, and J.H. Panchal, A quasi-feed-in-tariff policy formulation in micro-grids: A bi-level multi-period approach, Energy Policy **71** (2014), 63–75.
- 1148. A. Takeda and M. Kojima, Successive convex relaxation approach to bilevel quadratic optimization problems, Complementarity: applications, algorithms and extensions, Kluwer, Dordrecht, 2001, pp. 317–340.

- 1149. E.-G. Talbi (ed.), *Metaheuristics for bi-level optimization*, Studies in Computational Intelligence, no. 482, Springer-Verlag Berlin Heidelberg, 2013.
- 1150. M.L. Tam and W.H.K. Lam, Balance of car ownership under user demand and road network supply conditions?case study in hong kong, Journal of urban planning and development 130 (2004), no. 1, 24–36.
- 1151. R.R. Tan, K.B. Aviso, J.B. Cruz, and A.B. Culaba, A note on an extended fuzzy bi-level optimization approach for water exchange in eco-industrial parks with hub topology, Process Safety and Environmental Protection 89 (2011), no. 2, 106–111.
- 1152. Y. Tang, J.-P.P. Richard, and J.C. Smith, A class of algorithms for mixed-integer bilevel min-max optimization, Journal of Global Optimization (2015), 1–38.
- 1153. Pham Dinh Tao, Nam Nguyen Canh, Nguyen Van Thoai, et al., Dc programming techniques for solving a class of nonlinear bilevel programs, Journal of Global Optimization 44 (2009), no. 3, 313.
- 1154. Z. Tao, A stochastic bilevel programming model for the iron and steel production optimization problem under carbon trading mechanism, Proceedings of the Tenth International Conference on Management Science and Engineering Management, Springer, 2017, pp. 699– 710.
- 1155. C. Tawfik and S. Limbourg, *Bilevel optimization in the context of intermodal pricing: state of art*, Transportation Research Procedia **10** (2015), 634–643.
- 1156. A. Tesoriere, Stackelberg equilibrium with multiple firms and setup costs, Journal of Mathematical Economics **73** (2017), 86–102.
- 1157. P.T. Thach and T.V. Thang, Problems with resource allocation constraints and optimization over the efficient set, Journal of Global Optimization **58** (2014), no. 3, 481–495.
- 1158. J. Thai, R. Hariss, and A. Bayen, A multi-convex approach to latency inference and control in traffic equilibria from sparse data, American Control Conference (ACC), 2015, IEEE, 2015, pp. 689–695.
- 1159. H.A. Le Thi, T.P. Dinh, and L.D. Muu, Simplicially-constrained d.c. optimization over efficient and weakly efficient sets, Journal of Optimization Theory and Applications 117 (2003), 503–531.
- 1160. D. Thirwani and S.R. Arora, An algorithm for the integer linear fractional bilevel programming problem., Optimization **39** (1997), no. 1, 53–67.
- 1161. N.V. Thoai, Reverse convex programming approach in the space of extreme criteria for optimization over efficient sets, Journal of optimization theory and applications 147 (2010), no. 2, 263–277.
- 1162. L.Q. Thuy and T.N. Hai, A projected subgradient algorithm for bilevel equilibrium problems and applications, Journal of Optimization Theory and Applications **175** (2017), 411–431.
- 1163. F. Tiryaki, Interactive compensatory fuzzy programming for decentralized mult-level linear programming (DMLLP) problems, Fuzzy Sets and Systems 157 (2006), 3072–3090.
- 1164. R. Tobin and T. Friesz, Spatial competition facility location models: definition, formulation and solution approach, Annals of Operations Research 6 (1986), 49–74.
- 1165. R.L. Tobin, Uniqueness results and algorithms for Stackelberg-Cournot-Nash equilibrium, Annals of Operations Research **34** (1992), 21–36.
- 1166. B. Tolwinski, Closed-loop Stackelberg solution to a multistage linear-quadratic game, Journal of Optimization Theory and Applications 34 (1981), 485–501.
- 1167. C.A. Tovey, Asymmetric probabilistic prospects of Stackelberg players, Journal of Optimization Theory and Applications **68** (1991), 139–159.
- 1168. F. Tramontana, L. Gardini, and T. Puu, Mathematical properties of a discontinuous CournotStackelberg model, Chaos, Solitons & Fractals 44 (2011), no. 1, 58 70.
- 1169. R. Trujillo-Cortez and S. Zlobec, Bilevel convex programming models, Optimization 58 (2009), no. 8, 1009–1028.
- 1170. A. Tsoukalas, B. Rustem, and E.N. Pistikopoulos, A global optimization algorithm for generalized semi-infinite, continuous minimax with coupled constraints and bi-level problems, Journal of Global Optimization 44 (2009), no. 2, 235–250.
- 1171. A. Tsoukalas, W. Wiesemann, and B. Rustem, *Global optimisation of pessimistic bi-level* problems, Lectures on global optimization **55** (2009), 215–243.
- 1172. _____, Global optimisation of pessimistic bi-level problems, Lectures on global optimization 55 (2009), 215–243.

- 1173. T.V. Tu, Optimization over the efficient set of a parametric multiple objective linear programming problem, European Journal of Operational Research **122** (2000), 570–583.
- 1174. H. Tuy, Bilevel linear programming, multiobjective programming, and monotonic reverse convex programming, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 295–314.
- 1175. H. Tuy and S. Ghannadan, A new branch and bound method for bilevel linear programs, Multilevel Optimization: Algorithms and Applications (A. Migdalas, P.M. Pardalos, and P. Värbrand, eds.), Kluwer Academic Publishers, Dordrecht, 1998, pp. 231–249.
- 1176. H. Tuy, A. Migdalas, and N.T. Hoai-Phuong, A novel approach to bilevel nonlinear programming., Journal of Global Optimization **38** (2007), no. 4, 527–554.
- 1177. H. Tuy, A. Migdalas, and P. Värbrand, A global optimization approach for the linear twolevel program, Journal of Global Optimization **3** (1993), 1–23.
- 1178. _____, A quasiconcave minimization method for solving linear two-level programs, Journal of Global Optimization 4 (1994), 243–263.
- 1179. F. Ugranli, E. Karatepe, and A.H. Nielsen, MILP approach for bilevel transmission and reactive power planning considering wind curtailment, IEEE Transactions on Power Systems 32 (2017), no. 1, 652–661.
- 1180. S. Ukkusuri, K. Doan, and H.M.A. Aziz, A bi-level formulation for the combined dynamic equilibrium based traffic signal control, Procedia-Social and Behavioral Sciences 80 (2013), 729–752.
- 1181. G. Ünlü, A linear bilevel programming algorithm based on bicriteria programming, Computers & Operations Research 14 (1987), 173–179.
- 1182. T. Uno, H. Katagiri, and K. Kato, An evolutionary multi-agent based search method for Stackelberg solutions of bilevel facility location problems, International Journal of Innovative Computing, Information and Control 4 (2008), no. 5, 1033–1042.
- 1183. B. Vahdani, M. Soltani, M. Yazdani, and S.M. Mousavi, A three level joint locationinventory problem with correlated demand, shortages and periodic review system: Robust meta-heuristics, Computers & Industrial Engineering (2017), accepted for publication.
- 1184. M. Vahid-Ghavidel, N. Mahmoudi, and B. Mohammadi-Ivatloo, Self-scheduling of demand response aggregators in short-term markets based on information gap decision theory, IEEE Transactions on Smart Grid (2018).
- 1185. B. Van Dinh and L.D. Muu, On penalty and gap function methods for bilevel equilibrium problems, Journal of Applied Mathematics **2011** (2011).
- 1186. M. Červinka, Oligopolistic markets in terms of equilibrium problems with equilibrium constraints, Tech. report, Charles University in Prague, Faculty of Social Sciences, 2006, Bachelor Thesis.
- 1187. L. Vicente, *Bilevel programming*, Master's thesis, Department of Mathematics, University of Coimbra, 1992, in portuguese.
- 1188. L.N. Vicente, Bilevel programming: introduction, history, and overviev, Encyclopedia of Optimization (P.M. Pardalos et al., ed.), Kluwer Academic Publishers, Dordrecht, 2001, pp. 178–180.
- 1189. L.N. Vicente and P.H. Calamai, *Bilevel and multilevel programming: A bibliography review.*, Journal of Global Optimization **5** (1994), no. 3, 291–306.
- 1190. _____, Geometry and local optimality conditions for bilevel programs with quadratic strictly convex lower levels, Minimax and Applications (D.-Z. Du and P.M.Pardalos, eds.), Dordrecht: Kluwer Academic Publishers, 1995, pp. 141–151.
- 1191. L.N. Vicente, G. Savard, and J.J. Júdice, Descent approaches for quadratic bilevel programming, Journal of Optimization Theory and Applications 81 (1994), no. 2, 379–399.
- 1192. _____, Discrete linear bilevel programming problem., Journal of Optimization Theory and Applications 89 (1996), no. 3, 597–614.
- 1193. S. Vogel, Zwei-Ebenen-Optimierungsaufgaben mit nichtkonvexer Zielfunktion in der unteren Ebene: Pfadverfolgung und Spruenge, Ph.D. thesis, TU Bergakademie Freiberg, 2002.
- 1194. S. Vogel and S. Dempe, Pathfollowing and jumps in bilevel programming, Operations Research Proceedings 1999 (K. Inderfurth et al., ed.), Springer Verlag, Berlin et al., 2000, pp. 30–35.
- 1195. V.Visweswaran, C.A. Floudas, M.G. Ierapetritou, and E.N.Pistikopoulos, A decompositionbased global optimization approach for solving bilevel linear and quadratic programs, State
of the Art in Global Optimization: Computational Methods and Applications (C.A. Floudas and P.M. Pardalos, eds.), Kluwer Academic Publishers, Dordrecht, 1996.

- 1196. Z. Wan, Some approximating results on bilevel programming problems, Journal of systems science and systems engineering **20** (2000), 289–294.
- 1197. Z. Wan and J.-W. Chen, On bilevel variational inequalities, Journal of the Operations Research Society of China 1 (2013), no. 4, 483–510.
- 1198. Z. Wan, M. Jiang, and T. Hu, Approximate decomposition algorithm for solving the bilevel programming with the minimum risk, Journal of Engineering Mathematics (Xi'an) 17 (2000), 25–30.
- 1199. Z. Wan, L. Mao, and G. Wang, *Estimation of distribution algorithm for a class of nonlinear bilevel programming problems*, Information Sciences **256** (2014), 184–196.
- 1200. Z. Wan, G. Wang, and Y. Lv, A dual-relax penalty function approach for solving nonlinear bilevel programming with linear lower level problem, Acta Mathematica Scientia **31** (2011), no. 2, 652–660.
- 1201. Z. Wan, G. Wang, and B. Sun, A hybrid intelligent algorithm by combining particle swarm optimization with chaos searching technique for solving nonlinear bilevel programming problems, Swarm and Evolutionary Computation 8 (2013), 26–32.
- 1202. Z. Wan and S. Zhou, The convergence of approach penalty function method for approximate bilevel programming problem, Acta mathematica scientia, Series B, English Edition 21 (2001), 69–76.
- 1203. B. Wang, X.-Z. Zhou, and J. Watada, A unit commitment-based fuzzy bilevel electricity trading model under load uncertainty, Fuzzy Optimization and Decision Making 15 (2016), no. 1, 103–128.
- 1204. F.-S. Wang, Nested differential evolution for mixed-integer bi-level optimization for genome-scale metabolic networks, Differential Evolution in Chemical Engineering: Developments and Applications 6 (2017), 352.
- 1205. G. Wang, L. Ma, and J. Chen, A bilevel improved fruit fly optimization algorithm for the nonlinear bilevel programming problem, Knowledge-Based Systems 138 (2017), no. Supplement C, 113 – 123.
- 1206. G. Wang, Z. Wan, X. Wang, and Y. Lv, Genetic algorithm based on simplex method for solving linear-quadratic bilevel programming problem, Computers & Mathematics with Applications 56 (2008), no. 10, 2550–2555.
- 1207. G. Wang, X. Wang, Z. Wan, and Y. Lv, A globally convergent algorithm for a class of bilevel nonlinear programming problem, Applied Mathematics and Computation 188 (2007), no. 1, 166–172.
- 1208. G.-M. Wang, Z. Wan, and X.-J. Wang, Bibliography on bilevel programming, Advances in Mathematics 36 (2007), no. 5, 513–529.
- 1209. J.Y.T. Wang, M. Ehrgott, K.N. Dirks, and A. Gupta, A bilevel multi-objective road pricing model for economic, environmental and health sustainability, Transportation Research Procedia 3 (2014), 393–402.
- 1210. L. Wang and P. Xu, The watermelon algorithm for the bilevel integer linear programming problem, SIAM Journal on Optimization **27** (2017), no. 3, 1403–1430.
- 1211. M. Wang, R. Zhang, and X. Zhu, A bi-level programming approach to the decision problems in a vendor-buyer eco-friendly supply chain, Computers & Industrial Engineering (2017).
- 1212. Q. Wang and S. Wang, *Bilevel programs with multiple potential reactions*, Journal of Systems Science and Systems Engineering **3** (1994), no. 3.
- 1213. S. Wang and F.A. Lootsma, A hierarchical optimization model of resource allocation, Optimization 28 (1994), 351–365.
- 1214. S. Wang, Q. Meng, and H. Yang, *Global optimization methods for the discrete network design problem*, Transportation Research Part B: Methodological **50** (2013), 42–60.
- 1215. S. Wang, Q. Wang, and S. Romano-Rodriquez, Optimality conditions and an algorithm for linear-quadratic bilevel programming, Optimization **31** (1994), 127–139.
- 1216. S.-Y. Wang, Q. Wang, and L.C. Uria, A stability theorem in nonlinear bilevel programming, Questiió: Quaderns d'Estadística, Sistemes, Informatica i Investigació Operativa 20 (1996), no. 2.
- 1217. X. Wang and P.M. Pardalos, A modified active set algorithm for transportation discrete network design bi-level problem, Journal of Global Optimization 67 (2017), no. 1-2, 325– 342.

- 1218. Y. Wang, Y. Dvorkin, R. Fernandez-Blanco, B. Xu, T. Qiu, and D. Kirschen, *Look-ahead bidding strategy for energy storage*, IEEE Transactions on Sustainable Energy (2017).
- 1219. Y. Wang, Y.-C. Jiao, and H. Li, An evolutionary algorithm for solving nonlinear bilevel programming based on a new constraint-handling scheme, IEEE Transactions on Systems, Man, and Cybernetics, Part C: Applications and Reviews 35 (2005), no. 2, 221–232.
- 1220. Y. Wang, H. Li, and C. Dang, A new evolutionary algorithm for a class of nonlinear bilevel programming problems and its global convergence, INFORMS Journal on Computing 23 (2011), no. 4, 618–629.
- 1221. Y. Wang, S. Liu, and B. Zeng, Capacity expansion planning of wind power generation in a market environment with topology control, arXiv preprint arXiv:1701.03172 (2017).
- 1222. Y.B. Wang, D. Liu, X.C. Cao, Z.Y. Yang, J.F. Song, D.Y. Chen, and S.K. Sun, Agricultural water rights trading and virtual water export compensation coupling model: A case study of an irrigation district in china, Agricultural Water Management 180 (2017), 99–106.
- 1223. Z.-W. Wang, H. Nagasawa, and N. Nishiyama, An algorithm for a multiobjective, multilevel linear programming, Journal of the Operations Research Society of Japan 39 (1996), no. 2, 176–187.
- 1224. R. Wangkeeree and P. Yimmuang, Existence and algorithms for the bilevel new generalized mixed equilibrium problems in banach spaces, Applied Mathematics and Computation 219 (2012), no. 6, 3022 - 3038.
- 1225. J.D. Weber and T.J. Overbye, A two-level optimization problem for analysis of market bidding strategies, Power Engineering Society Summer Meeting, 1999. IEEE, vol. 2, IEEE, 1999, pp. 682–687.
- 1226. H.M. Wee, M.C. Lee, P.C. Yang, and R.L. Chung, *Bi-level vendorbuyer strategies for a time-varying product price*, Applied Mathematics and Computation **219** (2013), no. 18, 9670 9680.
- 1227. M. Weibelzahl and A. Märtz, Optimal storage and transmission investments in a bilevel electricity market model, Tech. report, RWTH Aachen, 2017.
- 1228. U. Wen, Mathematical methods for multilevel linear programming, Ph.D. thesis, Department of Industrial Engineering, State University of New York at Buffalo, 1981.
- 1229. _____, The "Kth-Best" algorithm for multilevel programming, Tech. report, Department of Operations Research, State University of New York at Buffalo, 1981.
- 1230. _____, A solution procedure for the resource control problem in two-level hierarchical decision processes, Journal of Chinese Institute of Engineers 6 (1983), 91–97.
- 1231. U. Wen and W. Bialas, The hybrid algorithm for solving the three-level linear programming problem, Computers & Operations Research 13 (1986), 367–377.
- 1232. U. Wen and S. Hsu, A note on a linear bilevel programming algorithm based on bicriteria programming, Computers & Operations Research 16 (1989), 79–83.
- 1233. _____, Linear bi-level programming problems a review, Journal of the Operational Research Society **42** (1991), 125–133.
- 1234. _____, Efficient solutions for the linear bilevel programming problem, European Journal of Operational Research 62 (1992), 354–362.
- 1235. U. Wen and S.-F. Lin, Finding an efficient solution to linear bilevel programming problem: An effective approach, Journal of Global Optimization 8 (1996), 295–306.
- 1236. U. Wen and Y. Yang, Algorithms for solving the mixed integer two-level linear programming problem, Computers & Operations Research 17 (1990), 133–142.
- 1237. U.P. Wen and A.D. Huang, A simple tabu search method to solve the mixed-integer linear bilevel programming problem, European Journal of Operational Research 88 (1996), 563– 571.
- 1238. A. Werner, Bilevel stochastic programming problems: Analysis and application to telecommunications, Ph.D. thesis, Section of Investment, Finance and Accounting, Department of Industrial Economics and Technology Management, Norwegian University of Science and Technology, Trondheim, Norway, 2005.
- 1239. D.J. White, *Multilevel programming, rational reaction sets, and efficient solutions*, Journal of Optimization Theory and Applications 87 (1995), 727–746.
- 1240. _____, Penalty function approach to linear trilevel programming, Journal of Optimization Theory and Applications **93** (1997), 183–197.
- 1241. D.J. White and G. Anandalingam, A penalty function approach for solving bi-level linear programs, Journal of Global Optimization **3** (1993), 397–419.

- 1242. G. Whittaker, R. Färe, S. Grosskopf, B. Barnhart, M.B. Bostian, G. Muller-Warrant, and S. Griffith, Spatial targeting of agri-environmental policy using bilevel evolutionary optimization, Omega 66 (2017), 15–27.
- 1243. W. Wiesemann, A. Tsoukalas, P.-M. Kleniati, and B. Rustem, *Pessimistic bilevel optimiza*tion, SIAM Journal on Optimization **23** (2013), 353 – 380.
- 1244. R. Winter, Zwei-Ebenen-Optimierung mit stetigem Knapsack-Problem in der unteren Ebene: Optimistischer und pessimistischer Zugang, Bachelorarbeit, TU Bergakademie Freiberg, 2010, 2010.
- 1245. R.K. Wood, *Deterministic network interdiction*, Mathematical and Computer Modelling 17 (1993), no. 2, 1–18.
- 1246. _____, Bilevel network interdiction models: Formulations and solutions, Wiley Encyclopedia of Operations Research and Management Science (J.J. Cochran, L.A. Cox, P. Keskinocak, J.P. Kharoufeh, and J.C. Smith, eds.), John Wiley & Sons, Inc., 2010.
- 1247. C. Wu and Y. Ji, Resource allocation in multiple product design projects: A bi-level programming approach, International Journal of Control and Automation 9 (2016), 271 – 280.
- 1248. S. Wu, Y. Chen, and P. Marcotte, A cutting plane method for linear bilevel programming, Systems Science and Mathematical Science **11** (1998), 125–133.
- 1249. Y. Xiang and L. Wang, A game-theoretic study of load redistribution attack and defense in power systems, Electric Power Systems Research 151 (2017), 12–25.
- 1250. G. Xianlong, C. Yang, and W. Weixin, Model and algorithm for inventory-transportation integrated optimization based on bi-level programming., International Journal of Advancements in Computing Technology 5 (2013), no. 5.
- 1251. W. Xiao, G. Du, Y. Zhang, and X. Liu, Coordinated optimization of low-carbon product family and its manufacturing process design by a bilevel game-theoretic model, Journal of Cleaner Production 184 (2018), 754–773.
- 1252. F. Xie, M.M. Butt, and Z. Li, A feasible flow-based iterative algorithm for the two-level hierarchical time minimization transportation problem, Computers & Operations Research (2017).
- 1253. H. Xiong, M. Chen, Y. Lin, N. Lv, X. Yan, K. Xu, and C. Wu, *Bi-level programming based* contra flow optimization for evacuation events, Kybernetes **39** (2010), no. 8, 1227–1234.
- 1254. C. Xu and T. Chen, *Incentive strategies with many followers*, Acta Automatica Sinica 17 (1991), 577–581, in chinese.
- 1255. G. Xu and Y. Li, Steady-state optimization of biochemical systems by bi-level programming, Computers & Chemical Engineering **106** (2017), 286 – 296, SI: ESCAPE-26.
- 1256. H. Xu, An MPCC approach for stochastic Stackelberg-Nash-Cournot equilibrium, Optimization 54 (2005), no. 1, 27–57.
- 1257. J. Xu and J. Gang, Multi-objective bilevel construction material transportation scheduling in large-scale construction projects under a fuzzy random environment, Transportation Planning and Technology 36 (2013), no. 4, 352–376.
- 1258. J. Xu, Z. Li, and Z. Tao, *Bi-level decision making in random phenomenon*, pp. 77–197, Springer Singapore, Singapore, 2016.
- 1259. ____, Bi-level decision making in random phenomenon, pp. 77–197, Springer Singapore, Singapore, 2016.
- 1260. J. Xu, Y. Tu, and Z. Zeng, Bilevel optimization of regional water resources allocation problem under fuzzy random environment, Journal of Water Resources Planning and Management 139 (2012), no. 3, 246–264.
- 1261. M. Xu and J.J. Ye, A smoothing augmented lagrangian method for solving simple bilevel programs, Computational Optimization and Applications 59 (2014), no. 1-2, 353–377.
- 1262. M. Xu, J.J. Ye, and L. Zhang, Smoothing augmented lagrangian method for nonsmooth constrained optimization problems, Journal of Global Optimization 62 (2015), no. 4, 675– 694.
- 1263. _____, Smoothing SQP methods for solving degenerate nonsmooth constrained optimization problems with applications to bilevel programs, SIAM Journal on Optimization 25 (2015), no. 3, 1388–1410.
- 1264. P. Xu, *Three essays on bilevel optimization algorithms and applications*, Ph.D. thesis, Iowa State University, U.S.A., 2012.

- 1265. P. Xu and L. Wang, An exact algorithm for the bilevel mixed integer linear programming problem under three simplifying assumptions, Computers & Operations Research 41 (2014), 309–318.
- 1266. X. Xu, Z. Meng, and R. Shen, A tri-level programming model based on conditional valueat-risk for three-stage supply chain management, Computers & Industrial Engineering 66 (2013), no. 2, 470–475.
- 1267. Z.K. Xu, Deriving the properties of linear bilevel programming via a penalty function approach, Journal of Optimization Theory and Applications 103 (1999), 441–456.
- 1268. M. Yamagishi and I. Yamada, Nonexpansiveness of a linearized augmented lagrangian operator for hierarchical convex optimization, Inverse Problems **33** (2017), no. 4, 044003.
- 1269. H. Yan and W.H. Lam, Optimal road tolls under conditions of queueing and congestion, Transportation Research A 30A (1996), 319–332.
- 1270. X. Yan, An augmented Lagrangian-based parallel splitting method for a one-leader-twofollower game, Journal of Industrial and Management Optimization 12 (2016), no. 3, 879 – 890.
- 1271. X. Yan and R. Wen, A new parallel splitting augmented lagrangian-based method for a Stackelberg game, Journal of Inequalities and Applications **2016** (2016), no. 1, 1–14.
- 1272. D. Yang, J. Jiao, Y. Ji, G. Du, P. Helo, and A. Valente, Joint optimization for coordinated configuration of product families and supply chains by a leader-follower Stackelberg game, European Journal of Operational Research 246 (2015), no. 1, 263 – 280.
- 1273. H. Yang and M.G.H. Bell, Transportation bilevel programming problems: Recent methodological advances, Transportation Research, Part B **35** (2001), 1–4.
- 1274. H. Yang, T. Sasaki, and Y. Iida, Estimation of origin-destination matrices from link traffic counts on congested networks, Transportation Research Part B: Methodological 26 (1992), no. 6, 417 – 434.
- 1275. H. Yang and S. Yagar, Traffic assignment and signal control in saturated road networks, Transportation Research Part A: Policy and Practice **29** (1995), no. 2, 125–139.
- 1276. L. Yang, R. Mahadevan, and W.R. Cluett, A bilevel optimization algorithm to identify enzymatic capacity constraints in metabolic networks, Computers & Chemical Engineering 32 (2008), no. 9, 2072–2085.
- 1277. Q. Yang, A note on constrained qualification for bilevel programming, Journal of Mathematical Research and Exposition 19 (1999), 359–366.
- 1278. D.-Q. Yao and J.J. Liu, Competitive pricing of mixed retail and e-tail distribution channels, Omega **33** (2005), no. 3, 235–247.
- 1279. Y. Yao, T. Edmunds, D. Papageorgiou, and R. Alvarez, *Trilevel optimization in power net-work defense*, IEEE Transactions on Systems, Man, and Cybernetics, Part C: Applications and Reviews **37** (2007), no. 4, 712–718.
- 1280. J.J. Ye, Necessary conditions for bilevel dynamic optimization problems, Decision and Control, 1994., Proceedings of the 33rd IEEE Conference on, vol. 1, IEEE, 1994, pp. 507–512.
- 1281. _____, Necessary conditions for bilevel dynamic optimization problems, SIAM Journal on Control and Optimization **33** (1995), no. 4, 1208 1223.
- 1282. _____, Necessary optimality conditions for bilevel dynamic problems, Decision and Control, 1997., Proceedings of the 36th IEEE Conference on, vol. 2, IEEE, 1997, pp. 1405–1410.
- 1283. _____, Optimal strategies for bilevel dynamic problems, SIAM Journal on Control and Optimization **35** (1997), 512–531.
- 1284. _____, Optimal strategies for bilevel dynamic problems, SIAM journal on control and optimization **35** (1997), no. 2, 512–531.
- 1285. _____, Nondifferentiable multiplier rules for optimization and bilevel optimization problems, SIAM Journal on Optimization 15 (2004), 252–274.
- 1286. _____, Constraint qualifications and KKT conditions for bilevel programming problems, Mathematics of Operations Research **31** (2006), 811–824.
- 1287. _____, Necessary optimality conditions for multiobjective bilevel programs, Mathematics of Operations Research **36** (2011), no. 1, 165–184.
- 1288. J.J. Ye and X.Y. Ye, Necessary optimality conditions for optimization problems with variational inequality constraints, Mathematics of Operations Research 22 (1997), no. 4, 977– 997.

- 1289. J.J. Ye and D. Zhu, New necessary optimality conditions for bilevel programs by combining the MPEC and value function approaches, SIAM Journal on Optimization 20 (2010), no. 4, 1885–1905.
- 1290. J.J. Ye, D. Zhu, and Q. Zhu, *Generalized bilevel programming problems*, Tech. Report DMS-646-IR, University of Victoria, Department of Mathematics and Statistics, 1993.
- 1291. J.J. Ye and D.L. Zhu, Optimality conditions for bilevel programming problems, Optimization 33 (1995), 9–27, with correction in Optimization 39(1997), pp. 361–366.
- 1292. ____, A note on optimality conditions for bilevel programming problems, Optimization **39** (1997), 361–366.
- 1293. J.J. Ye, D.L. Zhu, and Q.J. Zhu, Exact penalization and necessary optimality conditions for generalized bilevel programming problems, SIAM Journal on Optimization 7 (1997), 481–507.
- 1294. A. Yezza, First-order necessary optimality conditions for general bilevel programming problems, Journal of Optimization Theory and Applications 89 (1996), 189–219.
- 1295. W. Yi, L. Nozick, R. Davidson, B. Blanton, and B. Colle, Optimization of the issuance of evacuation orders under evolving hurricane conditions, Transportation Research Part B: Methodological 95 (2017), 285–304.
- 1296. P.-Y. Yin, Multilevel minimum cross entropy threshold selection based on particle swarm optimization, Applied Mathematics and Computation 184 (2007), no. 2, 503 513.
- 1297. Y. Yin, Genetic-algorithms-based approach for bilevel programming models, Journal of transportation engineering **126** (2000), no. 2, 115–120.
- 1298. _____, Multiobjective bilevel optimization for transportation planning and management problems, Journal of advanced transportation **36** (2002), no. 1, 93–105.
- 1299. J. Yu and H.L. Wang, An existence theorem for equilibrium points for multi-leader-follower games, Nonlinear Analysis: Theory, Methods & Applications 69 (2008), no. 5, 1775–1777.
- 1300. Y. Yu, F. Chu, and H. Chen, A Stackelberg game and its improvement in a VMI system with a manufacturing vendor, European Journal of Operational Research 192 (2009), no. 3, 929–948.
- 1301. D. Yue, J. Gao, B. Zeng, and F. You, A projection-based reformulation and decomposition algorithm for global optimization of a class of mixed integer bilevel linear programs, Journal of Global Optimization (2018), 1–31.
- 1302. D. Yue and F. You, Projection-based reformulation and decomposition algorithm for a class of mixed-integer bilevel linear programs, Computer Aided Chemical Engineering, vol. 38, Elsevier, 2016, pp. 481–486.
- 1303. _____, Stackelberg-game-based modeling and optimization for supply chain design and operations: A mixed integer bilevel programming framework, Computers & Chemical Engineering **102** (2017), 81–95.
- 1304. M. F. Zaman, S. M. Elsayed, T. Ray, and R. A. Sarker, A co-evolutionary approach for optimal bidding strategy of multiple electricity suppliers, Evolutionary Computation (CEC), 2016 IEEE Congress on, IEEE, 2016, pp. 3407–3715.
- 1305. A. J. Zaslavski, Necessary optimality conditions for bilevel minimization problems, Nonlinear Analysis: Theory, Methods & Applications **75** (2012), no. 3, 1655–1678.
- 1306. P. Zeephongsekul, *Stackelberg strategy solution for optimal software release policies*, Journal of Optimization Theory and Applications **91** (1996), 215–233.
- 1307. A. B. Zemkoho, *Multicriteria approach to bilevel programming*, Master's thesis, Universite de Yaounde I, Cameroon, 2007, in french.
- 1308. A.B. Zemkoho, *Bilevel programming: Reformulations, regularity, and stationarity*, Ph.D. thesis, TU Bergakademie Freiberg, 2012.
- 1309. Alain B Zemkoho, Solving ill-posed bilevel programs, Set-Valued and Variational Analysis 24 (2016), no. 3, 423–448.
- 1310. B. Zeng and Y. An, Solving bilevel mixed integer program by reformulations and decomposition, Optimization On-line (2014).
- 1311. D. Zhang and G.-H. Lin, Bilevel direct search method for leader-follower problems and application in health insurance, Computers & Operations Research 41 (2014), 359–373.
- 1312. G. Zhang, J. Han, and J. Lu, *Fuzzy bi-level decision-making techniques: A survey*, International Journal of Computational Intelligence Systems **9** (2016), no. sup1, 25–34.

- 1313. G. Zhang, C. Jiang, X. Wang, and B. Li, *Risk assessment and bi-level optimization dispatch of virtual power plants considering renewable energy uncertainty*, IEEJ Transactions on Electrical and Electronic Engineering (2017).
- 1314. G. Zhang and J. Lu, The definition of optimal solution and an extended Kuhn-Tucker approach for fuzzy linear bilevel programming., IEEE Intelligent Informatics Bulletin 6 (2005), no. 2, 1–7.
- 1315. _____, Fuzzy bilevel programming with multiple objectives and cooperative multiple followers, Journal of Global Optimization 47 (2010), no. 3, 403–419.
- 1316. G. Zhang, J. Lu, and T. Dillon, An approximation branch-and-bound algorithm for fuzzy bilevel decision making problems, Proceedings of The 1st International Symposium Advances in Artificial Intelligence and Applications, Poland, Citeseer, 2006.
- 1317. _____, An extended branch-and-bound algorithm for fuzzy linear bilevel programming, Applied Artificial Intelligence: Proceedings of the 7th International FLINS Conference, Genova, Italy, 29-31 August 2006, World Scientific, 2006, p. 291.
- 1318. _____, Decentralized multi-objective bilevel decision making with fuzzy demands, Knowledge-Based Systems **20** (2007), no. 5, 495–507.
- 1319. _____, Fuzzy linear bilevel optimization: Solution concepts, approaches and applications, Fuzzy Logic (P.P. Wang, D. Ruan, and E.E. Kerre, eds.), Studies in Fuzziness and Soft Computing, vol. 215, Springer Berlin Heidelberg, 2007, pp. 351–379.
- 1320. _____, Models and algorithm for fuzzy multi-objective multi-follower linear bilevel programming, IEEE International Fuzzy Systems Conference, 2007. FUZZ-IEEE 2007., IEEE, 2007, pp. 1–6.
- 1321. _____, Solution concepts and an approximation Kuhn-Tucker approach for fuzzy multiobjective linear bilevel programming, Pareto optimality, game theory and equilibria 17 (2008), 457.
- 1322. G. Zhang, J. Lu, and Y. Gao, An algorithm for fuzzy multi-objective multi-follower partial cooperative bilevel programming, Journal of Intelligent & Fuzzy Systems 19 (2008), no. 4, 5, 303–319.
- 1323. ____, Multi-level decision making: Models, methods and applications, vol. 82, Springer, 2015.
- 1324. G. Zhang, J. Lu, J. Montero, and Y. Zeng, *Model, solution concept, and kth-best algorithm* for linear trilevel programming, Information Sciences **180** (2010), no. 4, 481–492.
- 1325. G. Zhang, J. Lu, and X. Zeng, Models and algorithms for fuzzy multi-objective multifollower linear bilevel programming in a partial cooperative situation, International Conference on Intelligent Systems and Knowledge Engineering 2007, Atlantis Press, 2007.
- 1326. G. Zhang, G. Zhang, Y. Gao, and J. Lu, A bilevel optimization model and a pso-based algorithm in day-ahead electricity markets, IEEE International Conference on Systems, Man and Cybernetics, 2009. SMC 2009., IEEE, 2009, pp. 611–616.
- 1327. _____, Competitive strategic bidding optimization in electricity markets using bilevel programming and swarm technique, IEEE Transactions on Industrial Electronics 58 (2011), no. 6, 2138–2146.
- 1328. H. Zhang and Z. Gao, Bilevel programming model and solution method for mixed transportation network design problem, Journal of Systems Science and Complexity 22 (2009), no. 3, 446–459.
- 1329. J. Zhang, Approximating the two-level facility location problem via a quasi-greedy approach, Mathematical Programming **108** (2006), no. 1, 159–176.
- 1330. _____, Enhanced optimality conditions and new constraint qualifications for nonsmooth optimization problems, Ph.D. thesis, University of Victoria, 2014.
- 1331. J. Zhang, Y. Qiu, M. Li, and M. Xu, Sequential multi-objective optimization for lubrication system of gasoline engines with bilevel optimization structure, Journal of Mechanical Design 139 (2017), no. 2, 021405.
- 1332. J. Zhang, H. Wang, and Y. Sun, A note on the optimality condition for a bilevel programming, Journal of Inequalities and Applications **2015** (2015), no. 1, 1.
- 1333. J. Zhang and C. Xu, *Inverse optimization for linearly constrained convex separable pro*gramming problems, European Journal of Operational Research **200** (2010), no. 3, 671–679.
- 1334. J. Zhang, L. Zhang, H. Huang, X. Wang, C. Gu, and Z. He, A unified algorithm for virtual desktops placement in distributed cloud computing, Mathematical Problems in Engineering 2016 (2016).

- 1335. J.-Z. Zhang and D.-T. Zhu, A bilevel programming method for pipe network optimization, SIAM Journal on Optimization 6 (1996), 838–857.
- 1336. R. Zhang, Problems of hierarchical optimization in finite dimensions, SIAM Journal on Optimization 4 (1994), 521–536.
- 1337. _____, Multistage bilevel programming problems, Optimization 52 (2003), 605–616.
- 1338. T. Zhang, T. Hu, X. Guo, Z. Chen, and Y. Zheng, Solving high dimensional bilevel multiobjective programming problem using a hybrid particle swarm optimization algorithm with crossover operator, Knowledge-Based Systems **53** (2013), 13–19.
- 1339. T. Zhang, T. Hu, Y. Zheng, and X. Guo, An improved particle swarm optimization for solving bilevel multiobjective programming problem., J. Appl. Math. **2012** (2012), 13.
- 1340. X. Zhao, Z.-Y. Feng, Y. Li, and A. Bernard, *Evacuation network optimization model with lane-based reversal and routing*, Mathematical Problems in Engineering **2016** (2016).
- 1341. Y. Zheng and T. Basar, Existence and derivation of optimal affine incentive schemes for Stackelberg games with partial information: a geometric approach, International Journal of Control 35 (1982), no. 6, 997–1011.
- 1342. Y. Zheng, D. Fang, and Z. Wan, A solution approach to the weak linear bilevel programming problems, Optimization 65 (2016), no. 7, 1437–1449.
- 1343. _____, A solution approach to the weak linear bilevel programming problems, Optimization (2016), 1–13.
- 1344. Y. Zheng, G. Lei, and X. Cao, A method for a ε-global optimal solution of linear bilevel programming., J. Math., Wuhan Univ. 33 (2013), no. 5, 941–945 (Chinese).
- 1345. Y. Zheng, J. Liu, and Z. Wan, Interactive fuzzy decision making method for solving bilevel programming problem, Applied Mathematical Modelling **38** (2014), no. 13, 3136 3141.
- 1346. Y. Zheng and Z. Wan, A solution method for semivectorial bilevel programming problem via penalty method., J. Appl. Math. Comput. **37** (2011), no. 1–2, 207–219.
- 1347. Y. Zheng, Z. Wan, S. Jia, and G. Wang, A new method for strong-weak linear bilevel programming problem, Journal of Industrial and Management Optimization 11 (2015), no. 2, 529–547.
- 1348. Y. Zheng, Z. Wan, and Y. Lü, A global convergent method for nonlinear bilevel programming problems., J. Syst. Sci. Math. Sci. 32 (2012), no. 5, 513–521 (Chinese).
- 1349. Y. Zheng, Z.-P. Wan, and Z. Hao, An objective penalty function method for a class of nonlinear bilevel programming problems., J. Syst. Sci. Math. Sci. 33 (2013), no. 10, 1156– 1163 (Chinese).
- 1350. Y. Zheng, Z.-P. Wan, K. Sun, and T. Zhang, An exact penalty method for weak linear bilevel programming problem., J. Appl. Math. Comput. 42 (2013), no. 1–2, 41–49.
- 1351. Y. Zheng, Z.-P. Wan, and G.-M. Wang, A fuzzy interactive method for a class of bilevel multiobjective programming problem, Expert Systems with Applications 38 (2011), no. 8, 10384–10388.
- 1352. Y. Zheng, Z.-P. Wan, and L.-Y. Yuan, Coordination problem of the principal-agent based on bilevel programming, Xitong Gongcheng Lilun yu Shijian/System Engineering Theory and Practice 34 (2014), no. 1, 77–83.
- 1353. Y. Zheng, G. Zhang, J. Han, and J. Lu, *Pessimistic bilevel optimization model for risk*averse production-distribution planning, Information Sciences **372** (2016), 677 – 689.
- 1354. Y. Zheng, G. Zhang, Z. Zhang, and J. Lu, A reducibility method for the weak linear bilevel programming problems and a case study in principal-agent, Information Sciences 454-455 (2018), 46 - 58.
- 1355. Y. Zheng, Z. Zhu, and L. Yuan, Partially-shared pessimistic bilevel multi-follower programming: concept, algorithm, and application, Journal of Inequalities and Applications 2016 (2016), no. 1, 1–13.
- 1356. Y. Zheng, X. Zhuo, and J. Chen, Maximum entropy approach for solving pessimistic bilevel programming problems, Wuhan University Journal of Natural Sciences 22 (2017), no. 1, 63-67.
- 1357. Y. Zhou, S. Kwong, H. Guo, W. Gao, and X. Wang, *Bilevel optimization of block compressive sensing with perceptually nonlocal similarity*, Information Sciences **360** (2016), 1–20.
- 1358. _____, Bilevel optimization of block compressive sensing with perceptually nonlocal similarity, Information Sciences **360** (2016), 1 – 20.

- 1359. X. Zhu and P. Guo, Approaches to four types of bilevel programming problems with nonconvex nonsmooth lower level programs and their applications to newsvendor problems, Mathematical Methods of Operations Research 86 (2017), 255 – 275.
- 1360. X. Zhu, Q. Yu, and X. Wang, A hybrid differential evolution algorithm for solving nonlinear bilevel programming with linear constraints, 5th IEEE International Conference on Cognitive Informatics., vol. 1, IEEE, 2006, pp. 126–131.
- 1361. X. Zhuge, H. Jinnai, R.E. Dunin-Borkowski, V. Migunov, S. Bals, P. Cool, A.-J. Bons, and K.J. Batenburg, Automated discrete electron tomography-towards routine high-fidelity reconstruction of nanomaterials, Ultramicroscopy 175 (2017), 87–96.
- 1362. M. Zugno, J.M. Morales, P. Pinson, and H. Madsen, A bilevel model for electricity retailers' participation in a demand response market environment, Energy Economics 36 (2013), 182– 197.

TU BERGAKADEMIE FREIBERG E-mail address: dempe@tu-freiberg.de