

TEXTURE BASED DESCRIPTION OF MOVEMENTS FOR ACTIVITY ANALYSIS

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Abstract: Human motion can be seen as a type of moving texture pattern. In this paper, we propose a novel approach for activity analysis by describing human activities with texture features. Our approach extracts spatially enhanced local binary pattern (LBP) histograms from temporal templates (Motion History Images and Motion Energy Images) and models their temporal behavior with hidden Markov models. The description is useful for action modeling and is suitable for detecting and recognizing various kinds of activities. The method is computationally simple. We perform tests on two published databases and clearly show the good performance of our approach in classification and detection tasks. Furthermore, experimental results show that the approach performs robustly against irregularities in data, such as limping and walking with a dog, partial occlusions and low video quality.

1 INTRODUCTION

The detection and recognition of human activities from video data have gained a lot of interest in recent years. The potential application domains of human activity analysis include advanced human-computer interfaces, automated sign language interpretation, surveillance applications etc. All these domains have their own special demands, but in general, the designed algorithms must be able to detect and recognize various activities in real time. They should also cope with spatial and temporal differences in performance of actions as well as handle variation in the observed data due to difficult environment conditions.

Many approaches for human activity recognition have been proposed in the literature (Moeslund et al. 2006, Gavrilu 1999). Two typical approaches are to use either human pose information (Elgammal et al. 2003, Kellokumpu et al. 2005) or motion information (Efros et al. 2003).

The third common approach is to build templates of activities. Bobick and Davis (Bobick and Davis 2001) used Motion Energy Images (MEI) and Motion History Images (MHI) as temporal templates to recognize aerobics movements. Matching was done using seven Hu moments. 3D extension of the temporal templates was proposed by Weinland et al. (Weinland et al. 2006). They used multiple cameras

to build motion history volumes and performed action classification using Fourier analysis in cylindrical coordinates. Related 3D approaches have been used by Blank et al. (Blank et al. 2005) and Yilmaz and Shah (Yilmaz and Shah 2005) who utilized time as the third dimension and built space-time volumes in (x,y,t) space. Space time volumes were matched using features from Poisson equations and geometric surface properties, respectively.

Prior work with the temporal templates, motion history volumes and space time volumes are based on modeling the action as a whole. The choice of the appropriate action duration parameter is crucial because segmentation errors will lead to disastrous classification. Also, in the case of temporal templates and motion history volumes, actions that occupy the same space at different times cannot be modeled properly as the observed features will overlap and new observations will erase old features.

Instead of modeling the activity with one template we model the activities as a sequence of templates. Furthermore, as the local properties of the templates capture the essential information about human movements, we propose to use texture features for describing the templates. The local binary pattern (LBP) gives a description of local texture patterns and it has been successfully used in various applications, ranging from texture classification and segmentation to face recognition,

image retrieval and surface inspection. LBP features are fast to compute so they have been found to be suitable for real time applications.

In our method, we use the temporal templates as a preprocessing stage for a texture based description of human movements. We propose to extract spatially enhanced LBP histograms from the temporal templates to obtain our description. The temporal modeling is done with hidden Markov models (HMMs).

The proposed method describes human movements on two levels. The texture description calculated from MHI gives a good representation of motion, whereas the MEI based description characterizes shape information. One of the advantages of the method is that the texture based motion description is easy to compute compared to optical flow estimation, for example. By using local properties, our representation captures the essential information of human movements and allows variation in the performance of activities while still preserving discriminativity.

Section 2 describes the methodology in detail and Section 3 deals with experiments that illustrate the accuracy and robustness of our method. Section 4 concludes the paper.

2 TEXTURE DESCRIPTION OF MOVEMENTS

We introduce a new texture feature based description of human movements. The method employs temporal templates (Bobick and Davis 2001) as a preprocessing stage and uses LBP feature representation that encodes both motion and shape information of human movements. Finally, HMMs are used for modeling temporal behavior.

2.1 Temporal Templates

Motion templates, MEI and MHI, were introduced to describe motion information from images (Bobick



Figure 1: Illustration of the MHI (left) and MEI (right) in a case where a person is raising both hands.

and Davis 2001). MEI describes where motion occurred and MHI describes how the motion occurred. MEI is a binary representation of the areas of motion while MHI represents the history of motion so that more recent movements are shown with brighter values.

In our method, we use silhouettes as input for the system. MHI can be calculated from the silhouette representation as

$$MHI_{\tau}(x, y, t) = \begin{cases} \tau & \text{if } D(x, y, t) = 1 \\ \max(0, MHI_{\tau}(x, y, t-1) - 1) & \text{otherwise,} \end{cases} \quad (1)$$

where D is the silhouette difference between frames. The MEI, on the other hand, can be calculated directly from the silhouettes S :

$$MEI_{\tau}(x, y, t) = \bigcup_{i=0}^{\tau} S(x, y, t-i) \quad (2)$$

The formulation is similar to that of Bobick and Davis, but instead of silhouette difference, we chose to use the silhouette representation for the MEI calculation to get a better overall description of the human shape.

The duration of τ is critical and varies from activity to activity when MHI and MEI are used to represent an activity as a whole. Since we model movements as a sequence of templates, we can choose a fixed τ to give a short term motion representation. Figure 1 illustrates the templates.

2.2 Local Binary Pattern

LBP operator (Ojala et al. 2002) produces a binary code that describes the local texture pattern, which is built by thresholding a neighborhood of pixels by the grey value of its center pixel. The original LBP operator represents a 3x3 pixel neighborhood as a binary number. Figure 2 illustrates the basic LBP operator. When LBP operator is applied to an image, the image texture can be described with a histogram of the binary codes.

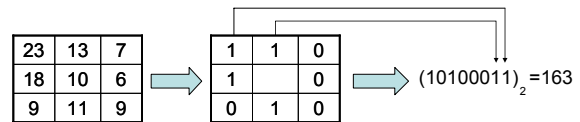


Figure 2: Illustration of basic LBP operator.

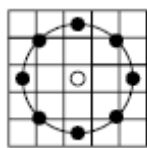


Figure 3: Circular (8,2) neighborhood. If the sampling point is not in the center of a pixel, the value at that point is bilinearly interpolated from the nearest pixels.

The LBP operator has also been extended to different kinds of neighborhoods. With a circular neighborhood and bilinear interpolation of pixels, any radius and number of sampling points in the neighborhood can be used. Figure 3 shows an example of the circular (8,2) neighborhood that has 8 sampling points and radius of 2.

We use the LBP description to characterize both MHI and MEI. This gives us a new texture based descriptor of human movements. From the definition of the MHI and MEI it can be seen that the LBP codes from MHI encode the information about the direction of motion whereas the MEI based LBP codes describe the combination of overall pose and shape of motion.

As changes in the gray levels of the MHI encode the motion, the outer edges of MHI may be misleading as texture is considered. In these areas there is no useful motion information and so the non-moving pixels having zero value should not be included in the calculation of the LBP codes. Therefore, calculation of LBP features is restricted to the nonmonotonous area within the MHI template.

Also, the LBP description of an image only contains information about the local spatial structures and does not give any information about the overall structure of motion. To preserve the rough structure of motion the MHI is divided into subregions. In our approach the division into four regions is done through the centroid of the silhouette. This division roughly separates the limbs. For many activities seen from the side view, for example sitting down, the division does not have any clear interpretation but it preserves the essential information about the movements. Our choice of division may not be optimal, and by choosing a more specified division scheme, one could increase the resolution of the description and model more specific activities.

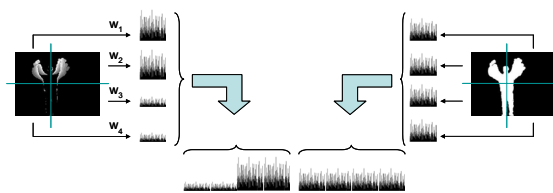


Figure 4: Illustration of the formation of the feature histogram. In this frame the top two subimages in MHI have high weights compared to the bottom two.

In many cases some of the MHI subimages contain much more motion than the others and thus provide more information. To give more focus on more meaningful areas of the images, we can perform spatial enhancement by assigning different weights to the subimages. Instead of using prior weights, we give weights online based on the relative amount of motion the subimage contains. The weights are given as the ratio of the area of nonzero pixels that the MHI subimage contains to the area of nonzero pixels in the whole image:

$$w_i = \frac{\text{area}(R_i)}{\sum_j \text{area}(R_j)} \quad (3)$$

Considering the texture of MEI images, it is easy to see that only the area around the boundaries gives meaningful description. The calculation of LBP features from MEI is performed only on these non-monotonous areas. Also, all subimage histograms are given equal weights.

All the MHI and MEI LBP features are concatenated into one histogram and normalized so that the sum of the histogram equals one. This is our description of the templates in each frame. Figure 4 illustrates the MHI and MEI, their division into subimages and the formation of LBP histograms.

2.3 Hidden Markov Models

The previously introduced LBP feature histograms are used to describe the human motion in every frame. The temporal modeling of the features is done by using HMMs. Our models are briefly described next but see tutorial (Rabiner 1989) for more details on HMMs. In our approach a HMM that has N states $\mathbf{Q} = \{q_1, q_2, \dots, q_N\}$ is defined with the triplet $\lambda = (\mathbf{A}, \boldsymbol{\pi}, \mathbf{H})$. Let the state at time step t be s_t , now the $N \times N$ state transition matrix \mathbf{A} is

$$\mathbf{A} = \{a_{ij} \mid a_{ij} = P(s_{t+1} = q_j \mid s_t = q_i)\}, \quad (4)$$

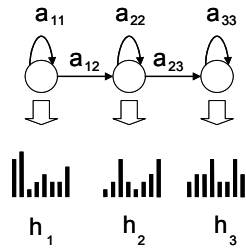


Figure 5: Illustration of a HMM. This example shows a 3 state left-to-right HMM with 8-bin feature histograms.

the initial state distribution vector π is

$$\pi = \{\pi_i \mid \pi_i = P(s_1 = q_i)\} \quad (5)$$

and the \mathbf{H} is the set of output histograms. The probability of observing an LBP histogram h_{obs} is the texture similarity between the observation and the model histograms. Histogram intersection was chosen as the similarity measure as it satisfies the probabilistic constraints. Thus, the probability of observing h_{obs} in state i is given as:

$$P(h_{obs} \mid s_i = q_i) = \sum \min(h_{obs}, h_i), \quad (6)$$

where the summation is done over the bins. Figure 5 illustrates a simple left-to-right HMM. HMMs can be used for activity classification by training a HMM for each action class. A new observed unknown feature sequence $\mathbf{H}_{obs} = \{h_{obs1}, h_{obs2}, \dots, h_{obsT}\}$ can be classified as belonging to the class of the model that maximizes $P(\mathbf{H}_{obs} \mid \lambda)$, the probability of observing \mathbf{H}_{obs} from the model λ . The model training is done using EM algorithm and the calculation of model probabilities can be done using forward algorithm.

3 EXPERIMENTS AND RESULTS

We use two different published databases for testing our method. The first database (Kellokumpu et al. 2005) contains 15 activities and the second database (Blank et al. 2005) 10 activities.

For the first database the original training material was not available so we used the leave one out strategy for the subjects in the test set. The comparisons of the results are only indicative but show that our method performs robustly. For the second database the input silhouettes are the same as the ones used in the original study.

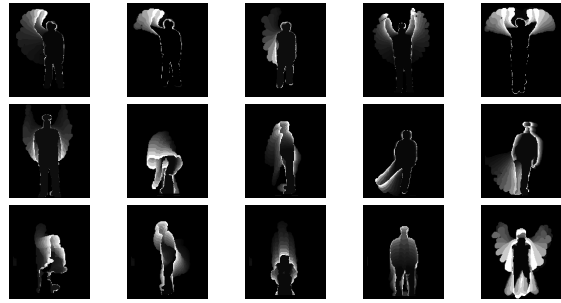


Figure 6: Illustration of the activity classes in the first database. Starting from the top left the activities are: Raising one hand, Waving one hand, Lowering one hand, Raising both hands, Waving both hands, Lowering both hands, Bending down, Getting up, Raising foot, Lowering foot, Sitting down, Standing up, Squatting, Up from squat, Jumping jack. Note that the MHI from the whole duration of the activity is shown to clarify the movements.

Tests with continuous video sequences of five persons performing 15 different activities were reported by (Kellokumpu et al. 2005). The activities in the database (later referred as ‘database A’) were: *Raising one hand, Waving one hand, Lowering one hand, Raising both hands, Waving both hands, Lowering both hands, Bending down, Getting up, Raising foot, Lowering foot, Sitting down, Standing up, Squatting, Up from squat, Jumping jack*. Each person performed the activities in different order without intentional pauses in between activities. The activities are illustrated using their MHIs in Figure 6.

The system (Kellokumpu et al 2005) used SVM to classify human pose in each frame and modeled activities with HMM as a sequence of postures. They experimented on continuous video data of human activities and reported results on activity detection and recognition. We will use the same silhouettes and compare results in subsection 3.3.

Blank et al. (Blank et al. 2005) reported tests on an online database that consists of two different parts. The first part (‘database B’) contains nine individuals performing ten different actions. The actions are temporally segmented, though the number of repetitions varied from person to person and from activity to activity. The actions in the database are: *Running, Walking, Jumping jack, Jumping forward on two legs, Jumping in place, Galloping sideways, Waving two hands, Waving one hand, Bending and Skipping*. The second part (‘robustness database’) is designed to test the robustness of an algorithm against high irregularities in performance of activities. The silhouettes in both parts of the database are of low resolution as the height of the subjects is roughly 70 pixels. The

silhouettes also contain leaks and intrusions because of imperfect background subtraction, shadows and color similarities with the background.

Blank et al. described human actions as three dimensional space-time shapes. They built a 3D representation of silhouettes in (x,y,t) space and described such a volume with features derived from the solution to Poisson equation. In practice, they do activity classification by dividing an example of an activity into overlapping space-time cubes of fixed length, and classify each cube individually with nearest neighbor procedure. The method uses aligned silhouettes and silhouettes are readily available in their database.

With these databases we were able to make four different experiment scenarios. In the first scenario, we show the proposed LBP-based features cluster even without a powerful modeling method. In the second scenario, we utilize the HMM modeling and experiment activity classification with temporally segmented data with databases A and B. We perform the temporal segmentation manually for the database A, whereas the database B consists of segmented data. In the third scenario, we experiment on continuous data and give activity detection and recognition results. This is done with the data from the database A. In the fourth scenario we use the robustness database and test our method against irregularities in the data such as walking in a skirt or limping as well as partially occluded legs or walking behind an occluding pole.

3.1 Feature Analysis

In this scenario we want to experiment on how the features behave in a simple case without a heavy modeling method. We first chose one sample from each person performing each of the 15 activities in database A. We calculated the LBP histogram descriptions for these samples and removed the time information by summing up the histograms over time and normalized the sum into one. Then we calculated the histogram intersection of these samples to all the other samples. Figure 7 illustrates the MHI based distances from sample to sample with τ set to four and circular (8,2) LBP neighborhood.

It can be seen that the samples clearly form clusters that represent the activity classes. This experiment was repeated with different template durations τ and LBP kernels and the distances always showed similar results. This scenario shows

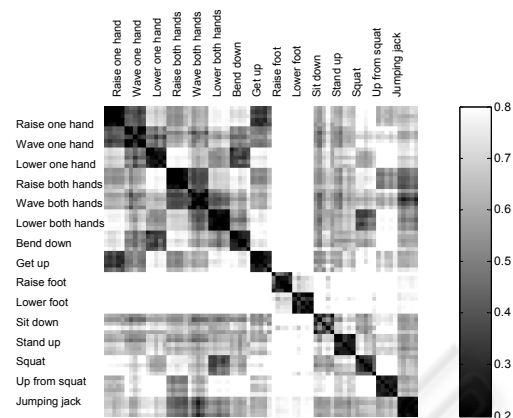


Figure 7: Illustration of the dissimilarity of the movement instances. Dark regions show high similarity and the diagonal dark squares show clustering of the activity classes.

that the proposed features are indeed very powerful in describing human movements.

It should be noted that the MEI based features will not behave well in this scenario as movements like *raising one hand* and *lowering one hand* will show exactly the same features when the time information is not used. In the next subsections we will also consider the temporal properties of the features and we perform modelling using HMM.

3.2 Activity Classification

We run the activity classification tests for the A and B databases using HMM modeling. For the database A, we again chose one example from each person performing each of the 15 activities. Using the leave one out approach, we used the examples of all but one person to train the models and used the one for testing. This was repeated for all the subjects in the database. The results presented here are achieved with τ set to four and with a circular (8,2)-LBP neighborhood.

The test was run with three different feature combinations. The MHI and MEI based LBP features were first used separately and then jointly. Both feature types were found to be useful. When using only MEI based features the classification accuracy was 90%. With MHI based features the classification accuracy was 99% as only one example was misclassified.

When MHI and MEI features were concatenated into one feature vector the description contained both the movement and shape information. Using these features all the examples were classified correctly. Although the recognition rate only

improved a little when the combination of features was used, the gap between the two most probable models also increased for examples that were already classified correctly making the classification more reliable. Result on this experiment scenario was not reported by Kellokumpu et al. (Kellokumpu et al. 2005) as they focused on continuous data. We will give results for that case in the next subsection.

Table 1: Results reported in the literature for database B. The first columns give the reference, number of classes, total number of sequences used and finally the classification result.

Ref.	Act.	Seq.	Res.
Our method	10	90	97,8%
Wang and Suter 2007	10	90	97,8%
Boiman and Irani 2006	9	81	97,5%
Niebles et al 2007	9	83	72,8%
Ali et al. 2007	9	81	92,6%
Scovanner et al. 2007	10	92	82,6%

The same leave one out strategy was used when the classification experiments were run on the database B. This database contains nine individuals performing ten different actions. As silhouettes in this database are much smaller in size we chose a smaller four point LBP neighborhood with radius of one. By using the combination of MHI and MEI based LBP features we were able to classify 88 out of the 90 segments correctly.

It should be noted that our way of representing the results is different from the way of Blank et al. who performed the classification of activities piecewise by partitioning each activity into many overlapping space-time cubes and classified the cubes with a nearest neighbor approach. Blank et al. did not give results on the skipping action, so their experiments consisted of 81 segments that were divided into 549 cubes from which they reported to misclassify only one space time cube.

Direct comparison of results to the original work is ambiguous, but results on the same database have been reported in the literature. Table 1 summarizes the achieved classification results. We can see that our method performs very well against various other methods.

3.3 Activity Detection

To further illustrate the discriminativity of our method, we performed the activity detection and recognition tests for the database A. We used the leave one out method on the test videos. We also adopted the same windowing approach for temporal

segmentation as (Kellokumpu et al. 2005) This resembles the exhaustive search used by Bobick and Davis (Bobick and Davis 2001).

Table 2: Confusion matrix of the continuous data experiment. The rows represent the detections and the columns represent the ground truth for the detection.

	Raising one hand	Waving one hand	Lowering one hand	Raising both hands	Waving both hands	Lowering both hands	Bending down	Getting up	Raising foot	Lowering foot	Sitting Down	Standing up	Squatting	Up from squat	Jumping jack	No movement
Raising one h	6	2														
Waving one h		5														1
Lowering one h	1	5														
Raising both h				6	1											
Waving both h					3											
Lowering both h				1	6											2
Bending down						5					2					
Getting up								5								
Raising foot									9							
Lowering foot										8						
Sitting Down											5					
Standing up												5				
Squatting													6			
Up from squat														6		
Jumping jack																16
No detection		1	1	4					1							

For this test scenario we used the combination of MHI and MEI based LBP features as they provided good classification results in the previous test scenario. The MHI based features were also tried alone, but the number of false alarms with this segmentation approach was much higher than with the combination of features. This shows that both motion and shape have a significant role in detecting and recognizing human activities.

The system described in (Kellokumpu et al. 2005) is invariant to handedness of performing activities, for example, raising the left hand is considered to be the same as raising the right hand. In our approach these activities show different features. As the database contains activities performed in two ways, we have to train one model for both cases. The training data on the second model is the same as for the first but mirrored. We did this for all actions where the handedness affects the features, thus instead of trying to detect 15 activities, we actually have to try to detect 24 different activities.

It should be noted that our detections give more information but we give the results in the same format as the reference work. The results for the tests are shown in Table 2. The number of activities in the database was 101 and our method recognized 96 correctly with 106 detections. This gives the

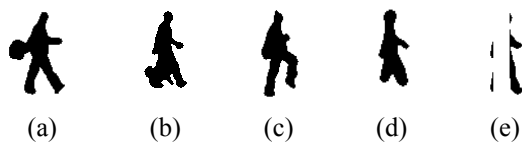


Figure 8: Example silhouettes from the robustness experiments. (a) Swinging bag (b) walking with a dog (c) knees up (d) occluded legs (e) walking behind pole.

$$\text{recognition rate} = \frac{\text{correct detections}}{\text{actions in db}} = \frac{96}{101} = 95\% \quad (7)$$

and

$$\text{accuracy} = \frac{\text{correct detections}}{\text{all detections}} = \frac{96}{106} = 91\% \quad (8)$$

A recognition rate of 90% and detection accuracy of 83% was reported by Kellokumpu et al. so our result is better.

It can be noticed from the confusion matrix in Table 2 that many of the false alarms come when the ground truth is waving one hand or both. Most of these false alarms actually are from one subject whose range of motion was much vaster than the others. This results in false detections of raising and lowering hand(s). Based on the training samples one could argue that the detections could be interpreted to be correct as well as the hands movement during waving hand(s) was quite similar to repeating raising and lowering hand(s) motions.

3.4 Robustness Experiments

We used the robustness database (Blank et al. 2005) to test our approach against irregularities in the data. The data used for training is the same that were used in the classification experiments on the database B. Some example silhouettes from the database are illustrated in Figure 8.

The results along with results by (Wang and Suter 2006) are given in Table 3. Our method can classify nine out of eleven cases correctly and in the two misclassified cases the correct class is the second most probable class. Blank et al. did not include the walking behind pole case and they were able to classify nine out of ten correctly. It should again be noted that Blank et al. partitioned the test segments into space time cubes and in this case made the classification based on median of test cube distances to the most similar cubes in the training data. This may help their classification as short difficult parts of the test segment do not necessarily affect the median value. In our experiment we used the whole segments for classification.

Table 3: Classification results for the robustness test. The first column describes the test scenario and the second column shows our classification result. The label side refers to the class *Gallopingsideways*. The two last columns show the result by two other methods.

Action	Our 1 st	Rank of walking Wang and Suter 2007	Rank of walking Blank et al. 2005
Normal walk	walk	1	1
Walking in a skirt	walk	1	1
Carrying briefcase	side	1	1
Knees up	side	1	1
Diagonal walk	walk	2	1
Limping man	walk	1	1
Occluded legs	walk	1	1
Swinging bag	walk	2	1
Sleepwalking	walk	>2	1
Walking with a dog	walk	>2	2
Walking behind pole	walk	-	-

This test scenario clearly shows that our approach can handle various kinds of difficult conditions and still perform robustly. Even though the matching strategy is different from the approach of Blank et al., we can see that our method performs very well and we can even classify correctly the difficult walking behind pole case.

4 CONCLUSIONS

In this paper, we have proposed a novel approach for human activity modeling that describes human movements as a moving texture pattern. Temporal templates are used as a preprocessing stage and their local characteristics are described with LBP features. Temporal aspects are modeled with HMMs. The method is computationally simple and can run in real time.

By using local properties, our representation captures the essential information of human movements and allows variation in the performance of activities while still preserving discriminativity. The new texture based description of movement is robust and we have shown experiments and comparison of results on activity recognition and detection. The tests clearly show good performance. We have also demonstrated that the method is robust against irregularities in the data as well as partial occlusions and low video quality.

Our representation encodes both shape and motion. In the experiments the proposed method was

used to model various kinds of activities with excellent results. This shows that our texture based description of movements is very useful for modeling activities. Also, choosing the subimage division scheme specifically for every action could improve the description and enable the modeling of very specific activities.

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